

# Chem 352 – Lecture 4

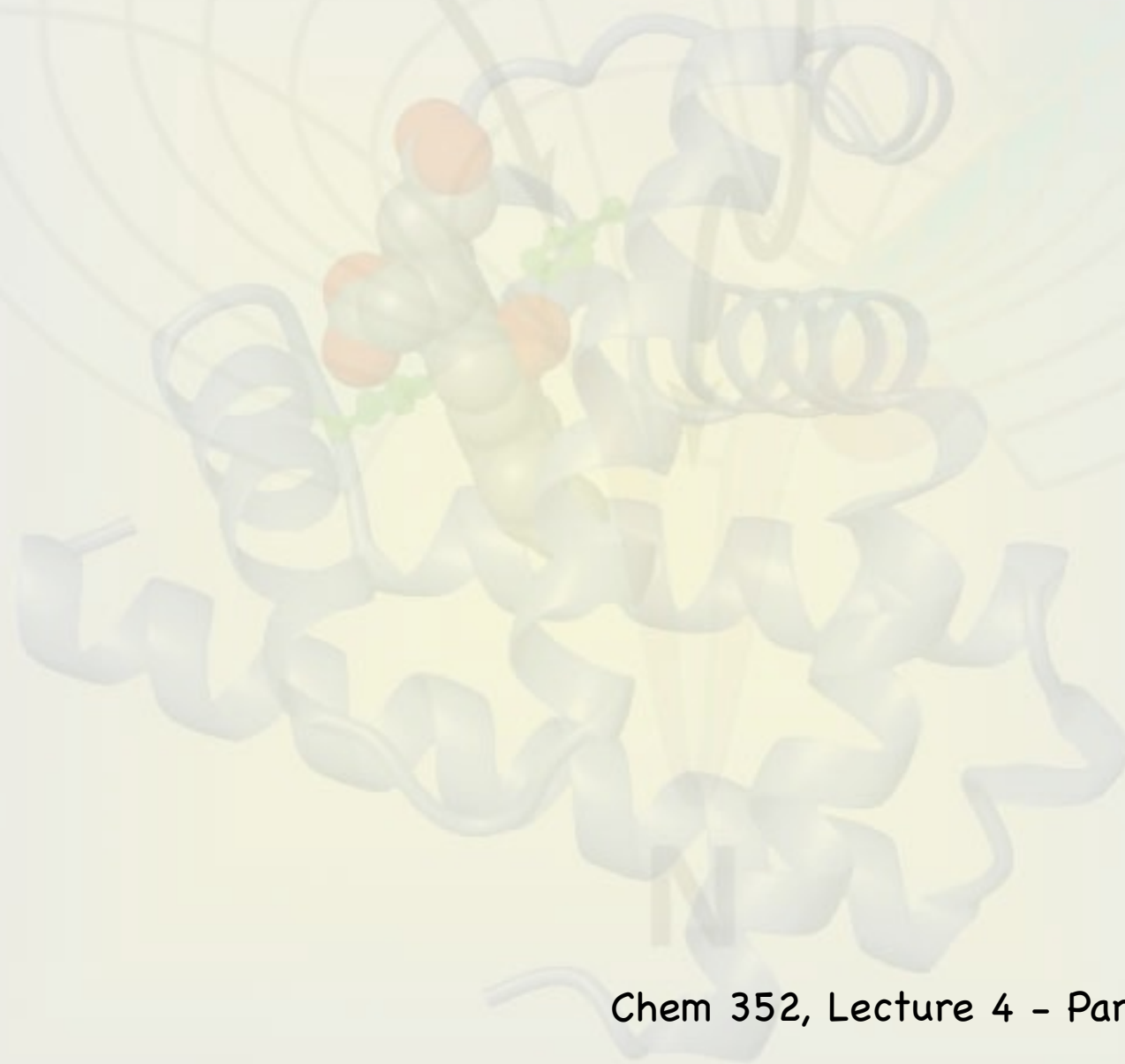
## Part I: Enzyme Properties

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**Question for the Day:** Describe how to easily determine the number of reactions that one enzyme molecule is capable catalyzing in one second.

# Introduction to Enzymes

- Enzymes are biological **catalysts**



# Introduction to Enzymes

- Enzymes are biological **catalysts**

catalyst |'katl-ist|

noun

a substance that increases the rate of a chemical reaction without itself undergoing any permanent chemical change.

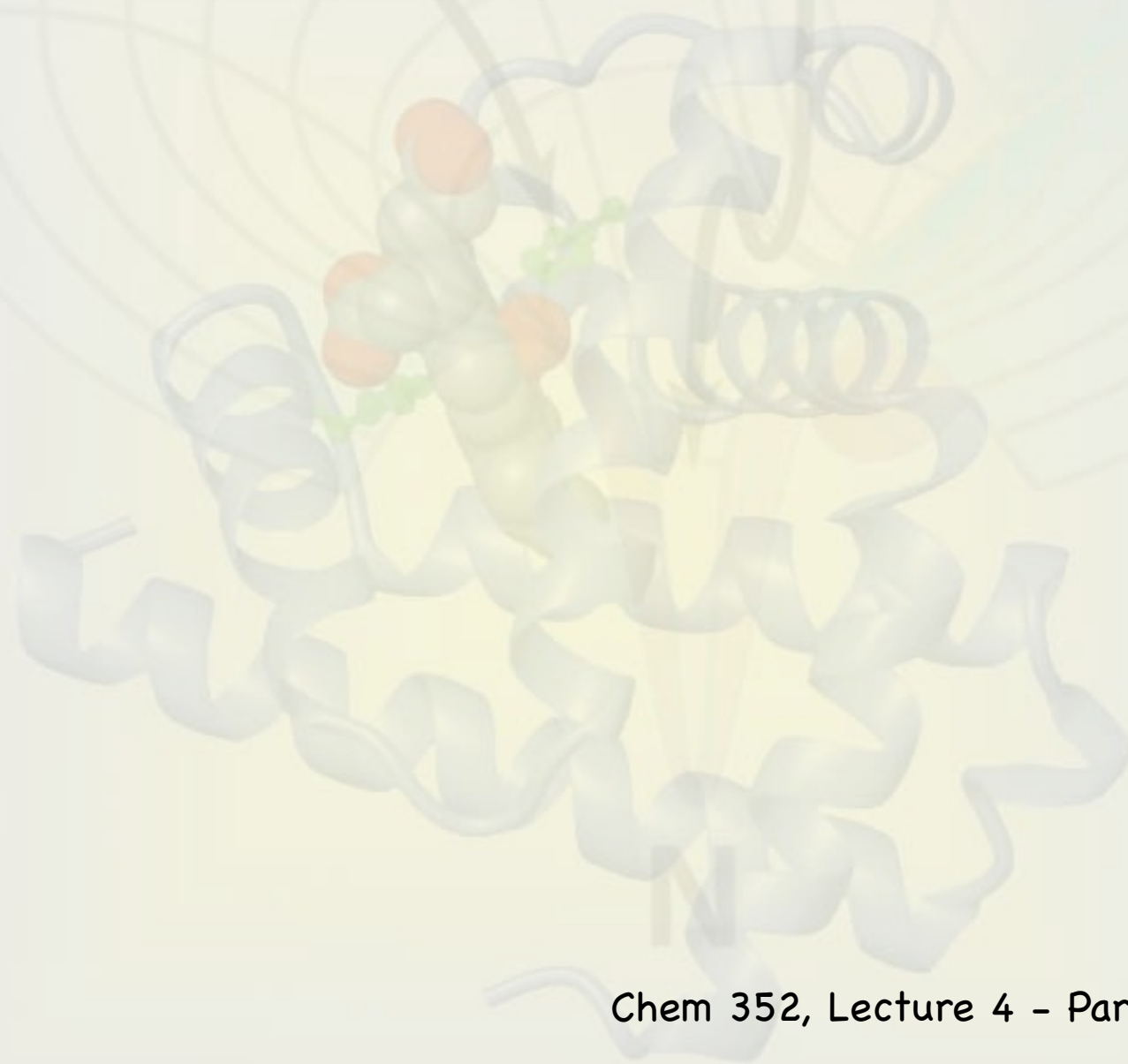
- figurative a person or thing that precipitates an event : *the governor's speech acted as a catalyst for debate.*

ORIGIN early 20th cent.: from **catalysis** , on the pattern of *analyst*.

(New Oxford American Dictionary)

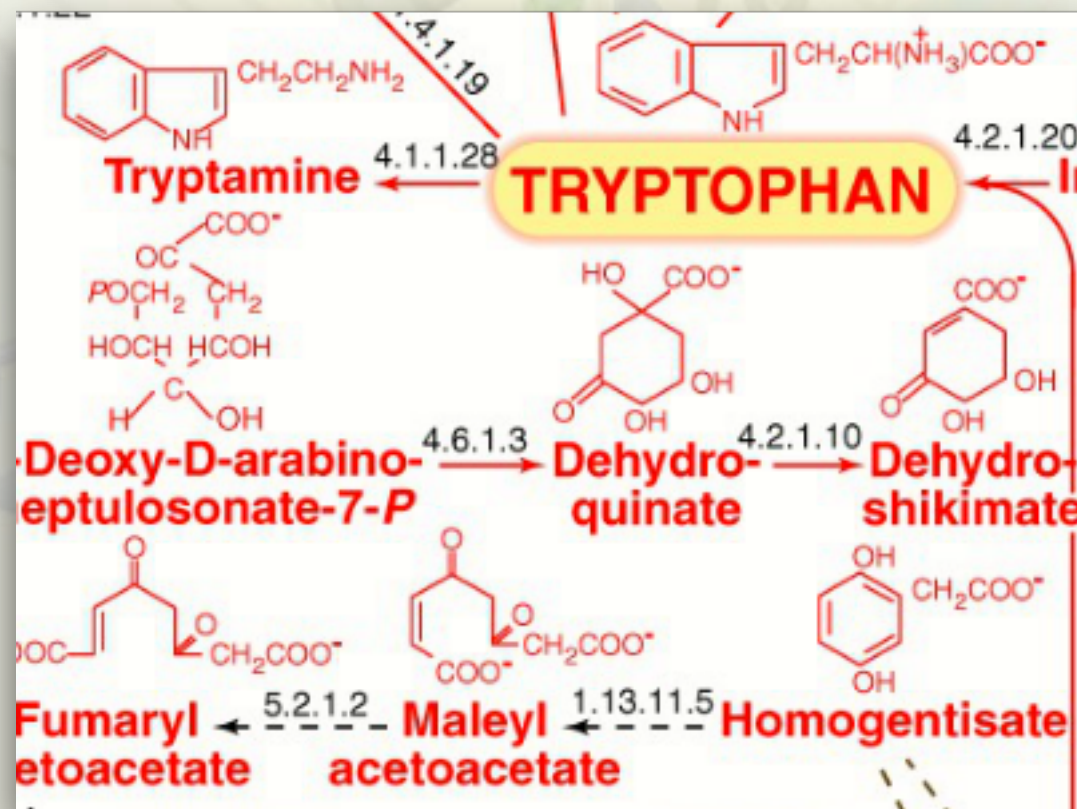
# Introduction to Enzymes

- Enzyme are biological **catalysts**



# Introduction to Enzymes

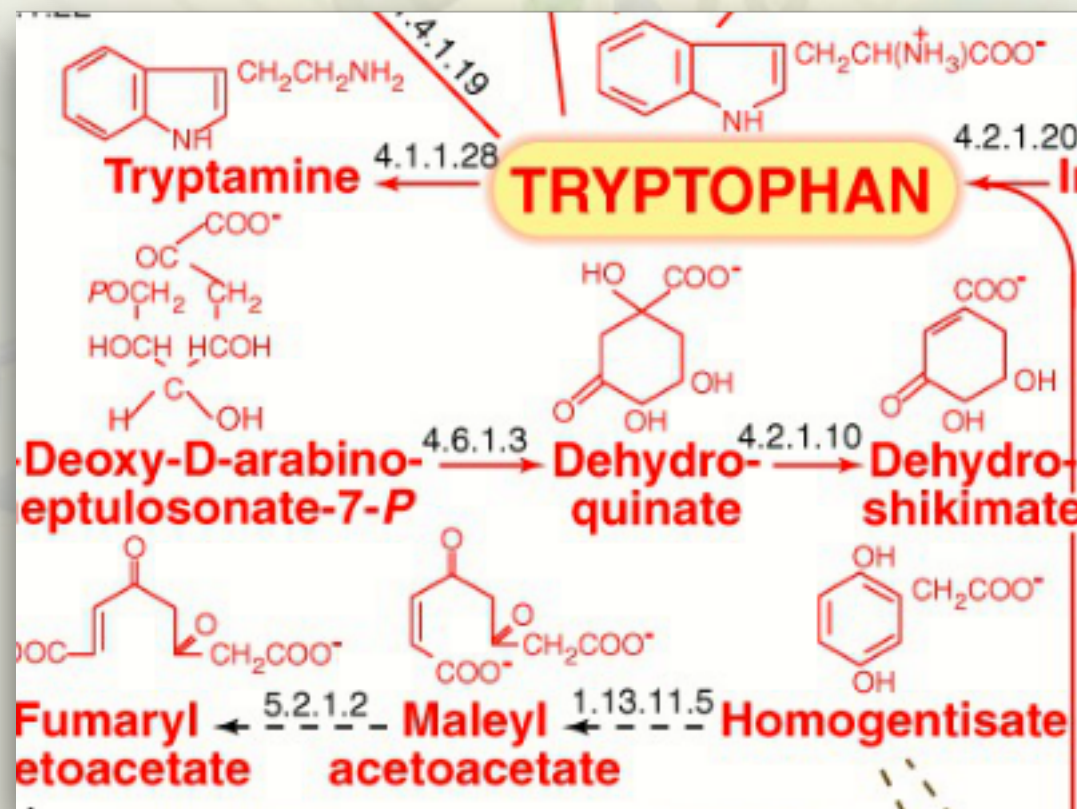
- Enzymes are biological **catalysts**
  - ✦ Nearly every reaction in a living cell is catalyzed by an enzyme.





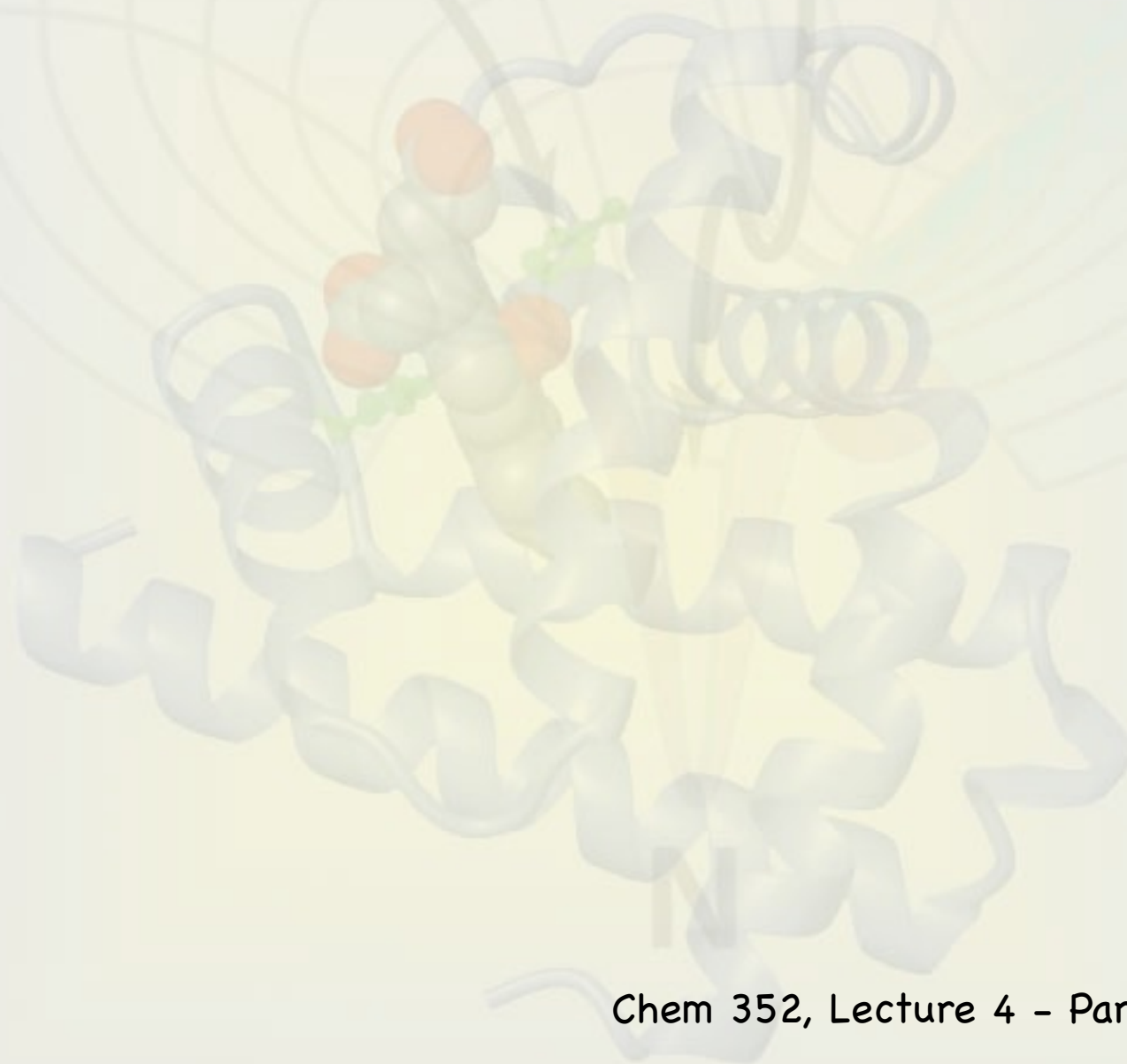
# Introduction to Enzymes

- Enzymes are biological **catalysts**
  - ✦ Nearly every reaction in a living cell is catalyzed by an enzyme.
  - ✦ Most enzymes are proteins.



# Introduction to Enzymes

- Enzymes can exhibit:



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- Enzymes can exhibit:
  - ✦ High specificity
    - High substrate specificity
    - High reaction specificity



# Introduction to Enzymes

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- ✦ High specificity

- High substrate specificity
    - High reaction specificity
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  - ✦ They serve as control points in metabolic pathways.

# Introduction to Enzymes

## Question:

Explain why it should be a relatively simple task for an enzyme to distinguish between L-alanine and D-alanine.

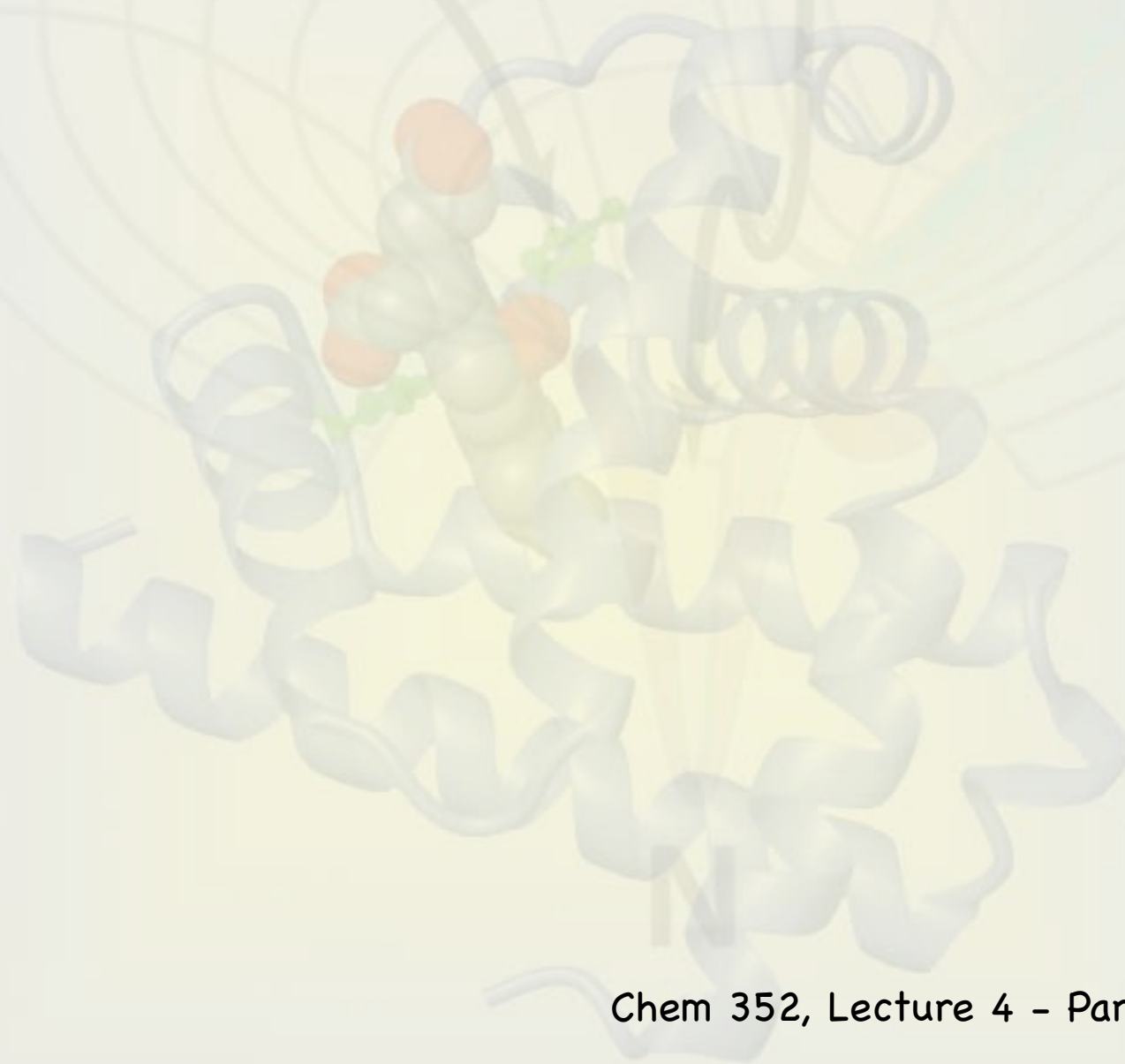
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# Introduction to Enzymes

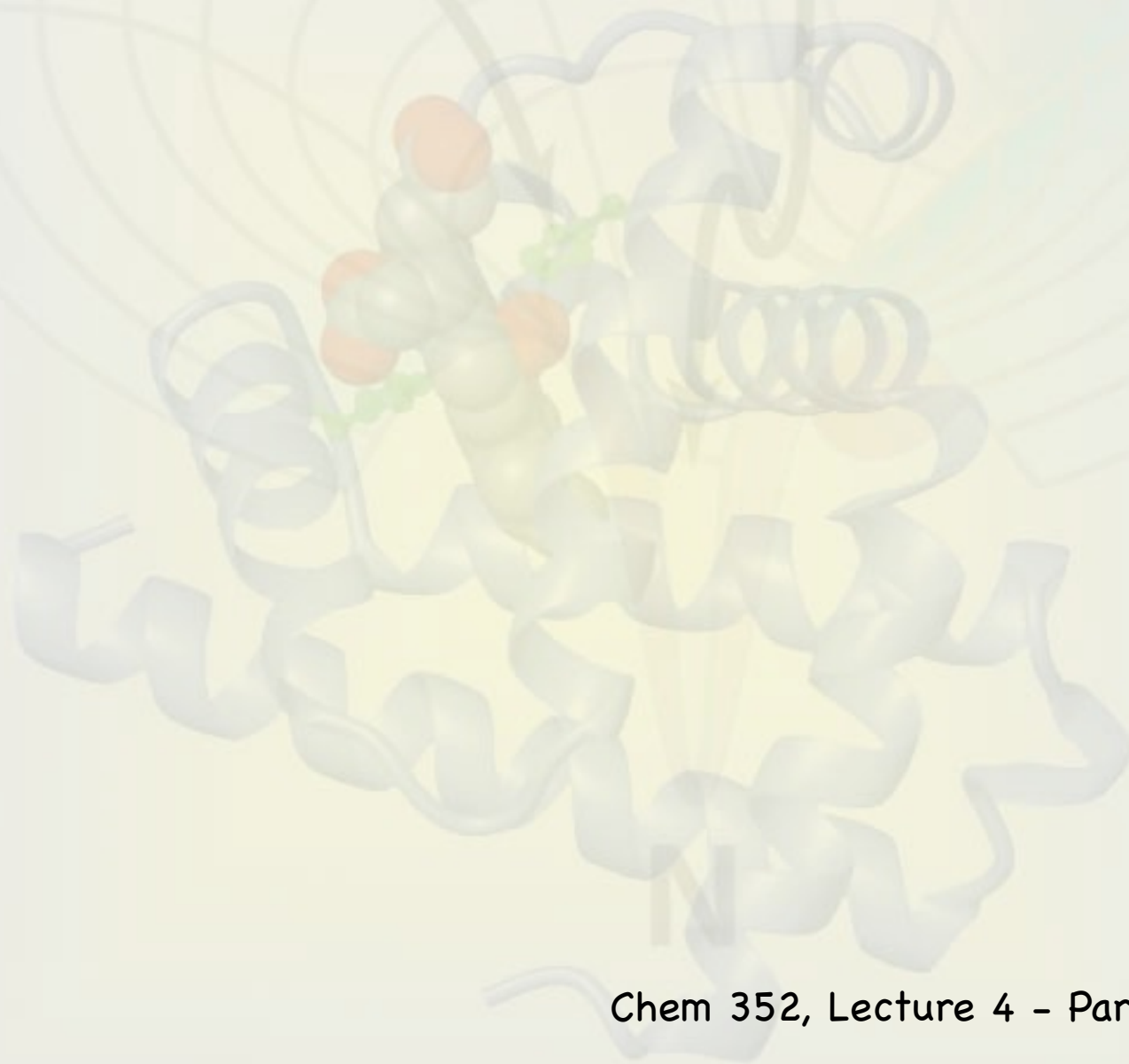
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# Introduction to Enzymes

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- ✦ The analysis of the **kinetics** of enzyme-catalyzed reactions
  - and learn what this can tell us about the mechanisms of enzyme catalyzed reactions.

# Introduction to Enzymes

In this lecture will discuss

- ✦ The **classification** and **nomenclature** of enzymes
- ✦ The analysis of the **kinetics** of enzyme-catalyzed reactions
  - and learn what this can tell us about the mechanisms of enzyme catalyzed reactions.
- ✦ The **regulation** of enzyme activity by inhibitors and activators

# Myoglobin and Hemoglobin

While neither of these proteins are enzymes, they nicely illustrate some of the recurring themes that we will see in our discussion on enzymes.

- Hyperbolic and sigmoidal binding behaviors
- Allosteric behaviors

(Moran et al. Section 4.14)



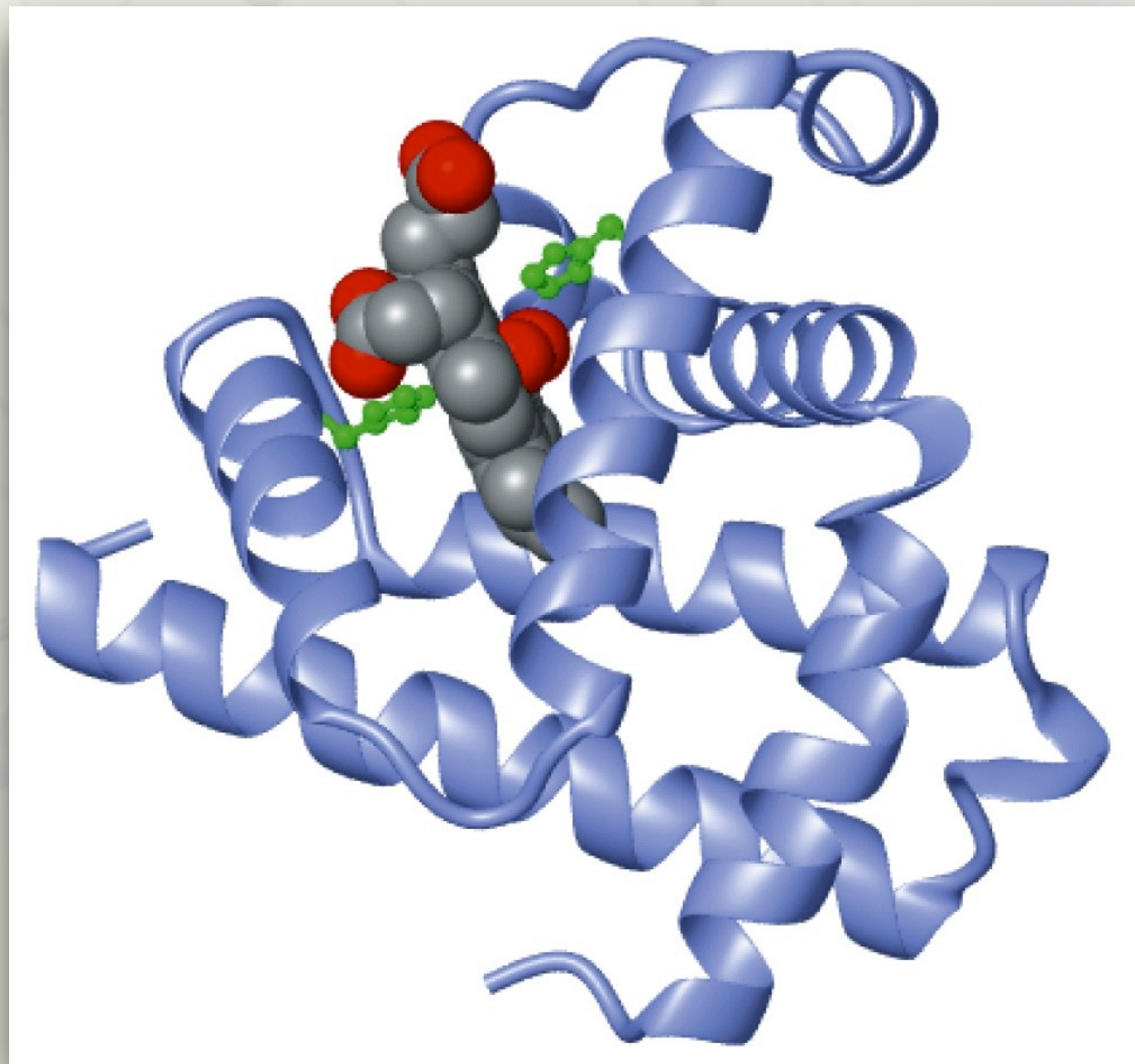
# Myoglobin and Hemoglobin

Both these proteins function to bind and transport molecular oxygen.

- ✦ But they have distinctly different roles
  - **Hemoglobin (Hb)** transports oxygen from the lungs to the tissues.
  - **Myoglobin (Mb)** accepts the oxygen from Hb and stores it in the tissues

# Myoglobin and Hemoglobin

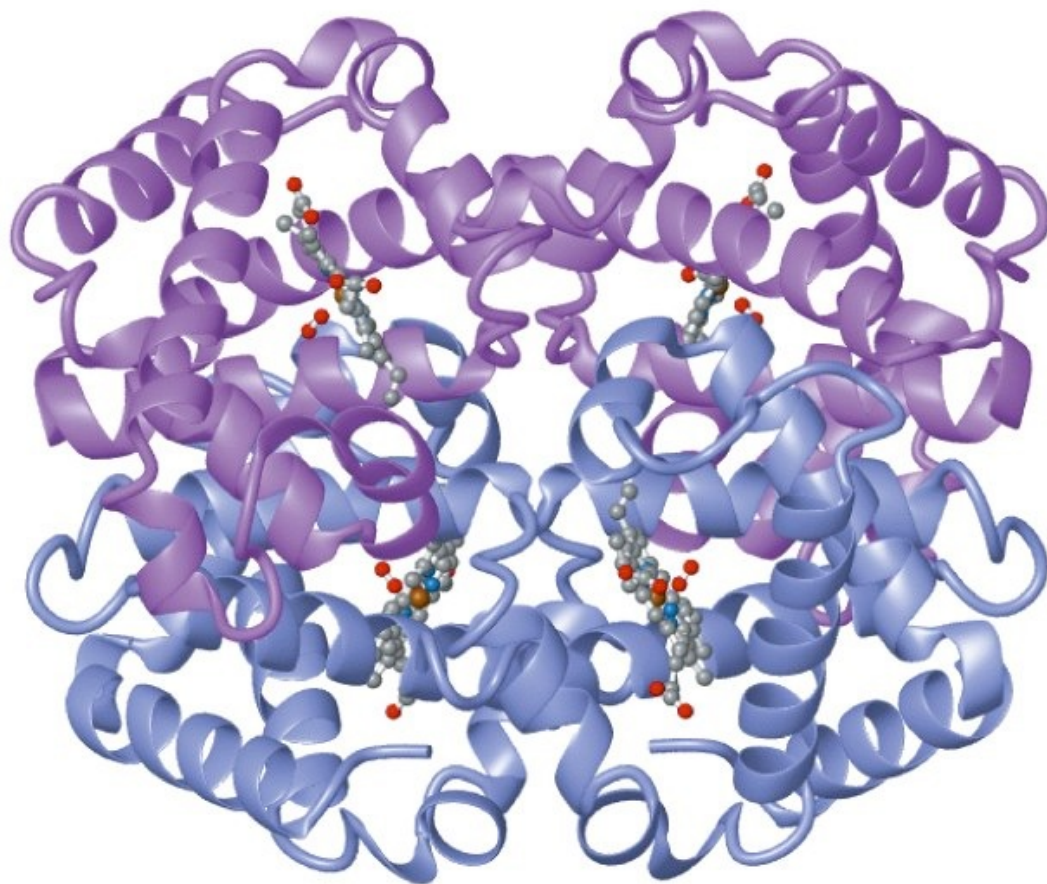
Hb and Mb share similar I°, II° and III° structures



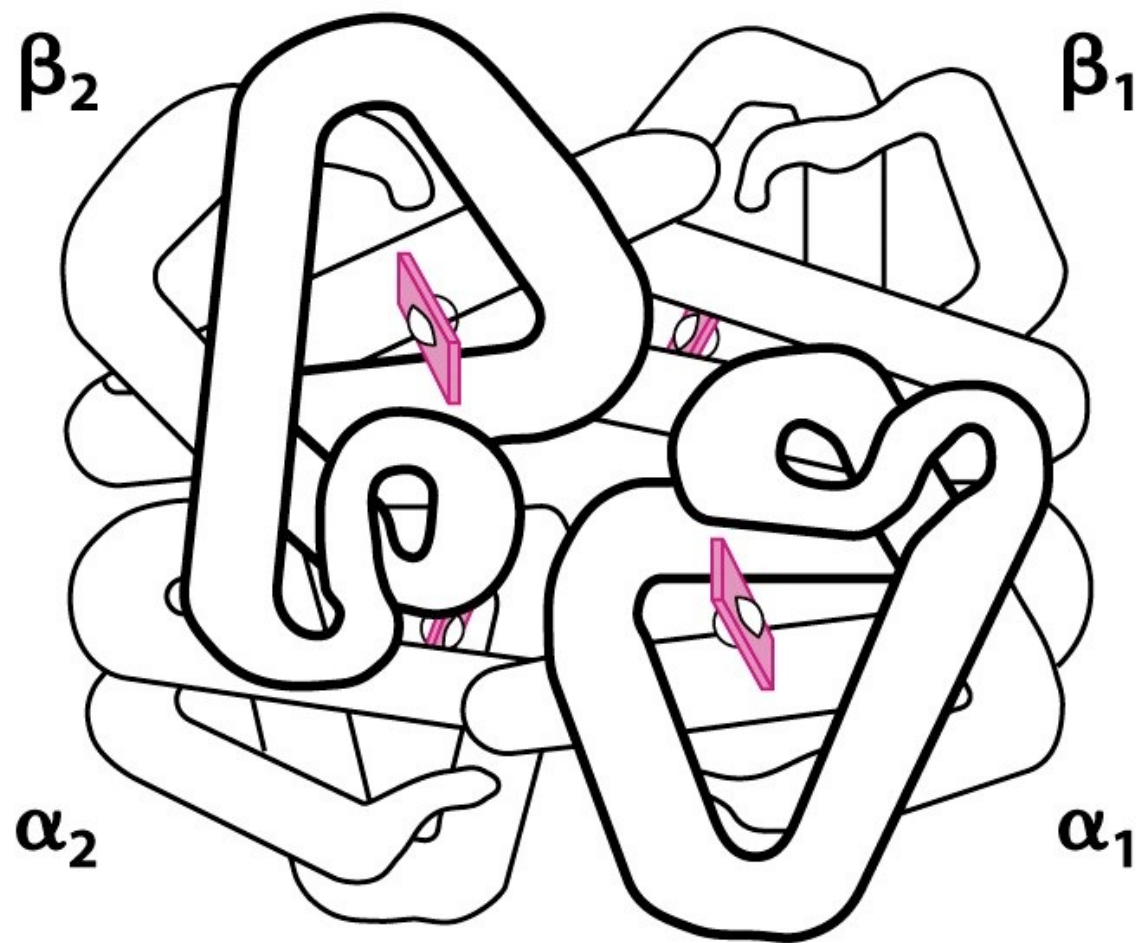
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Hb and Mb share similar I°, II° and III° structures

(a) Hb also has IV° structure



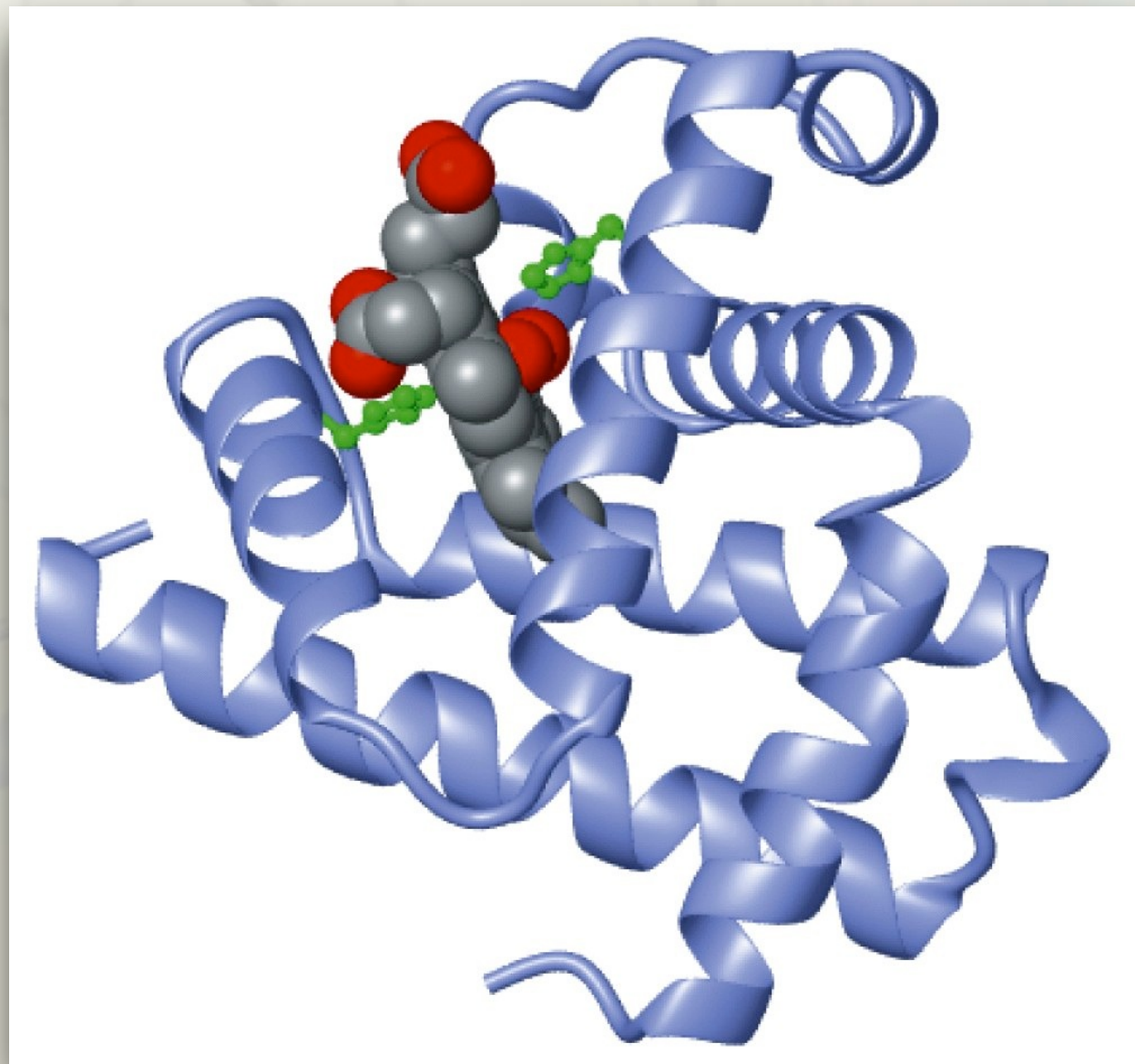
(b)





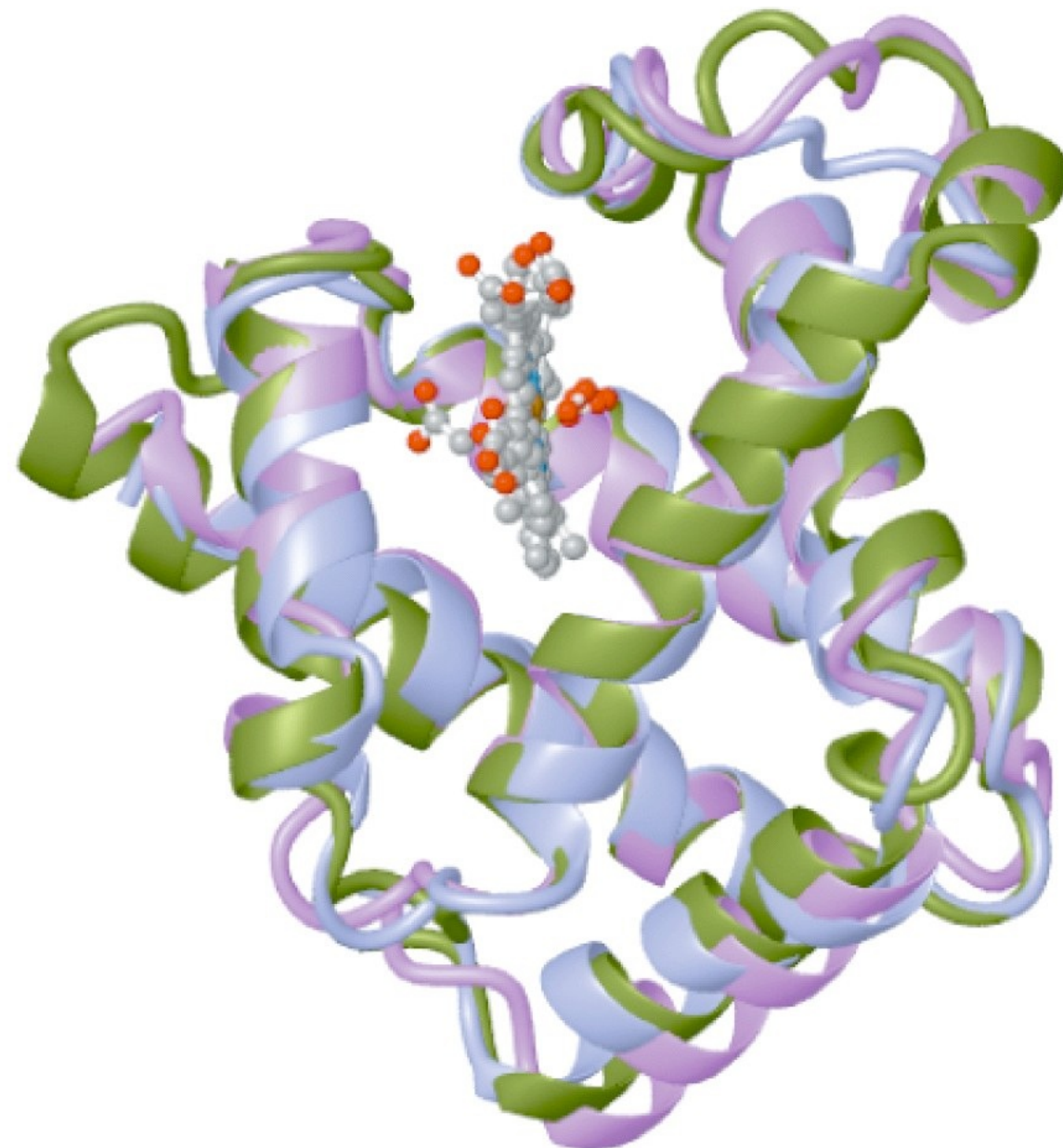
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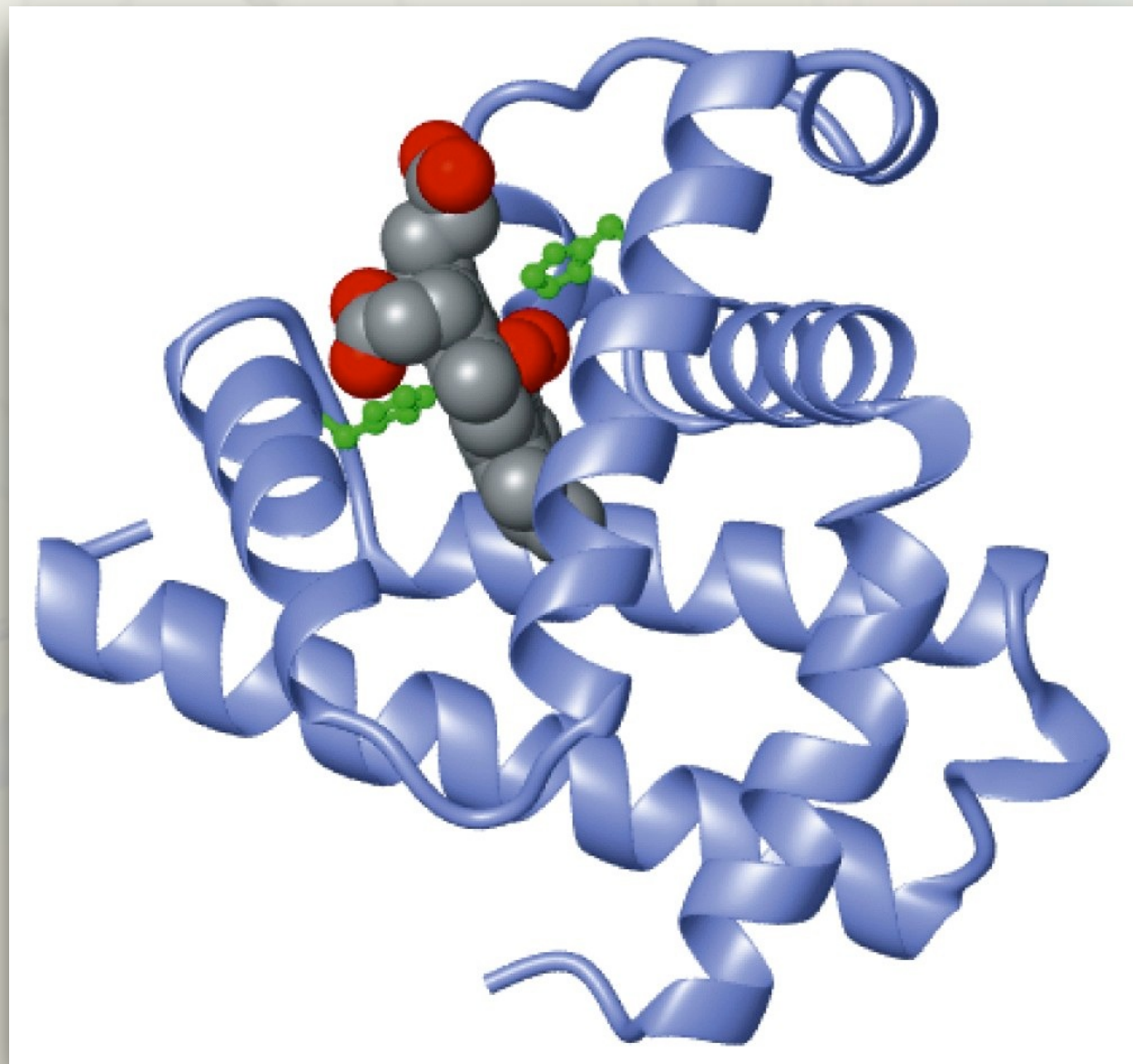
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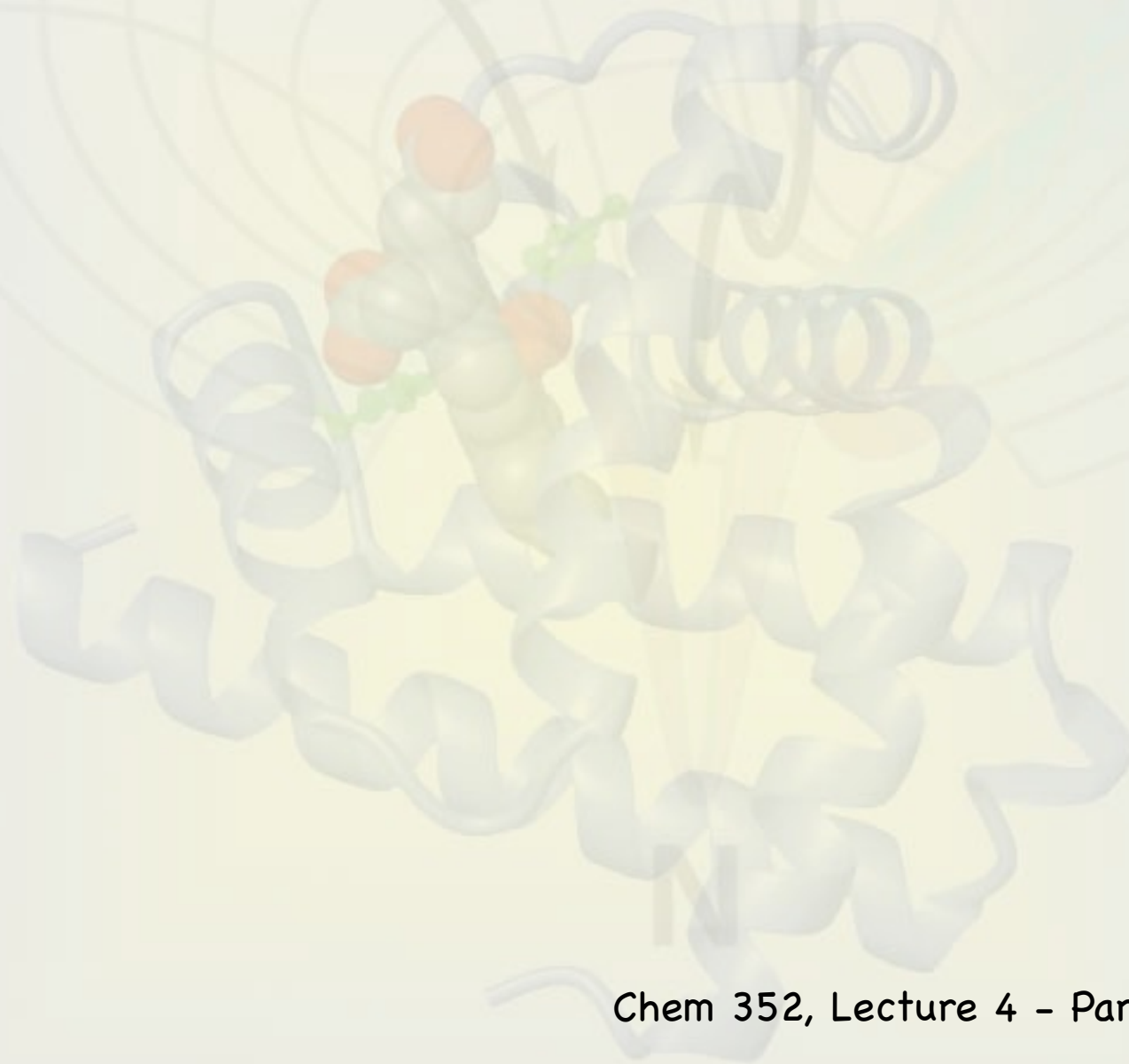
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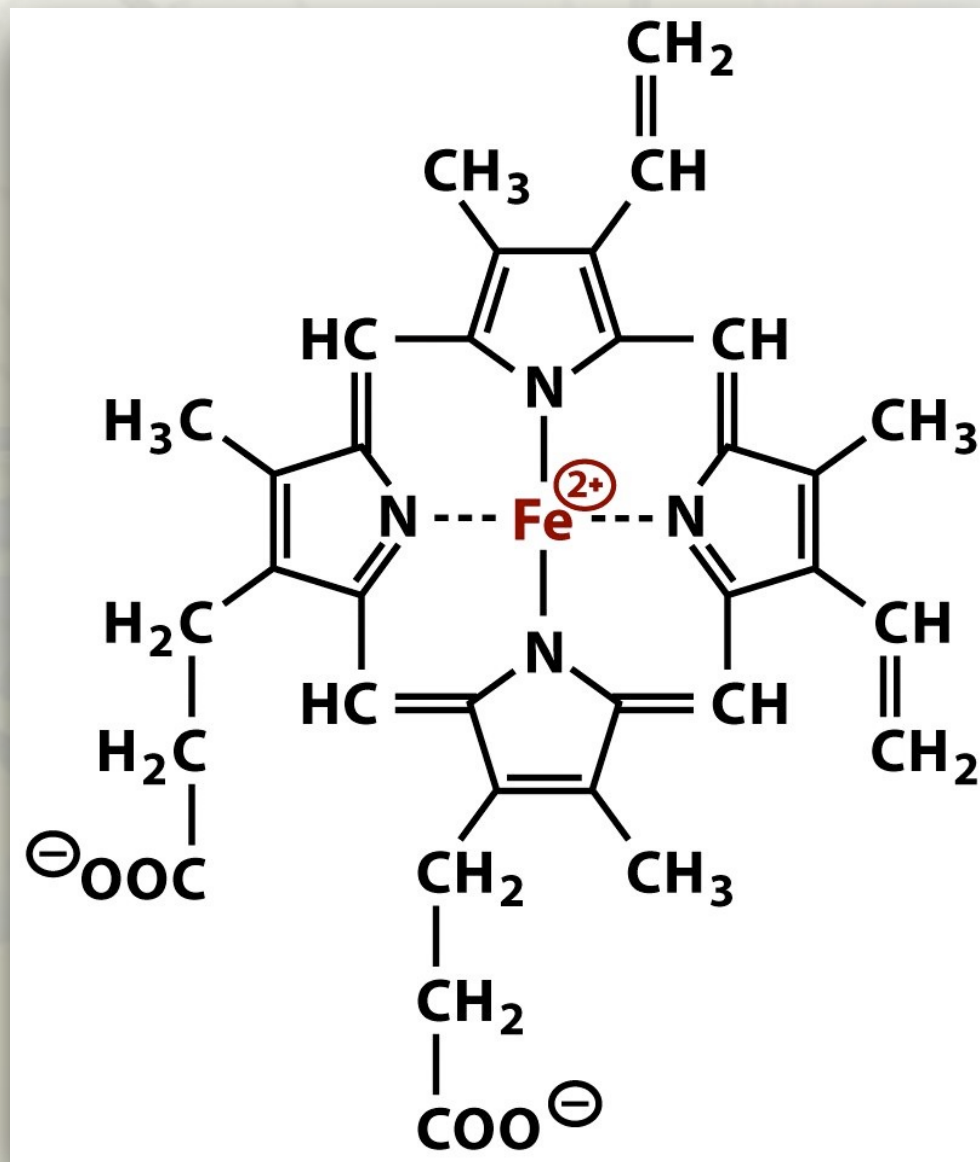
# Myoglobin and Hemoglobin

For both, oxygen binding occurs using a heme prosthetic group (cofactor).



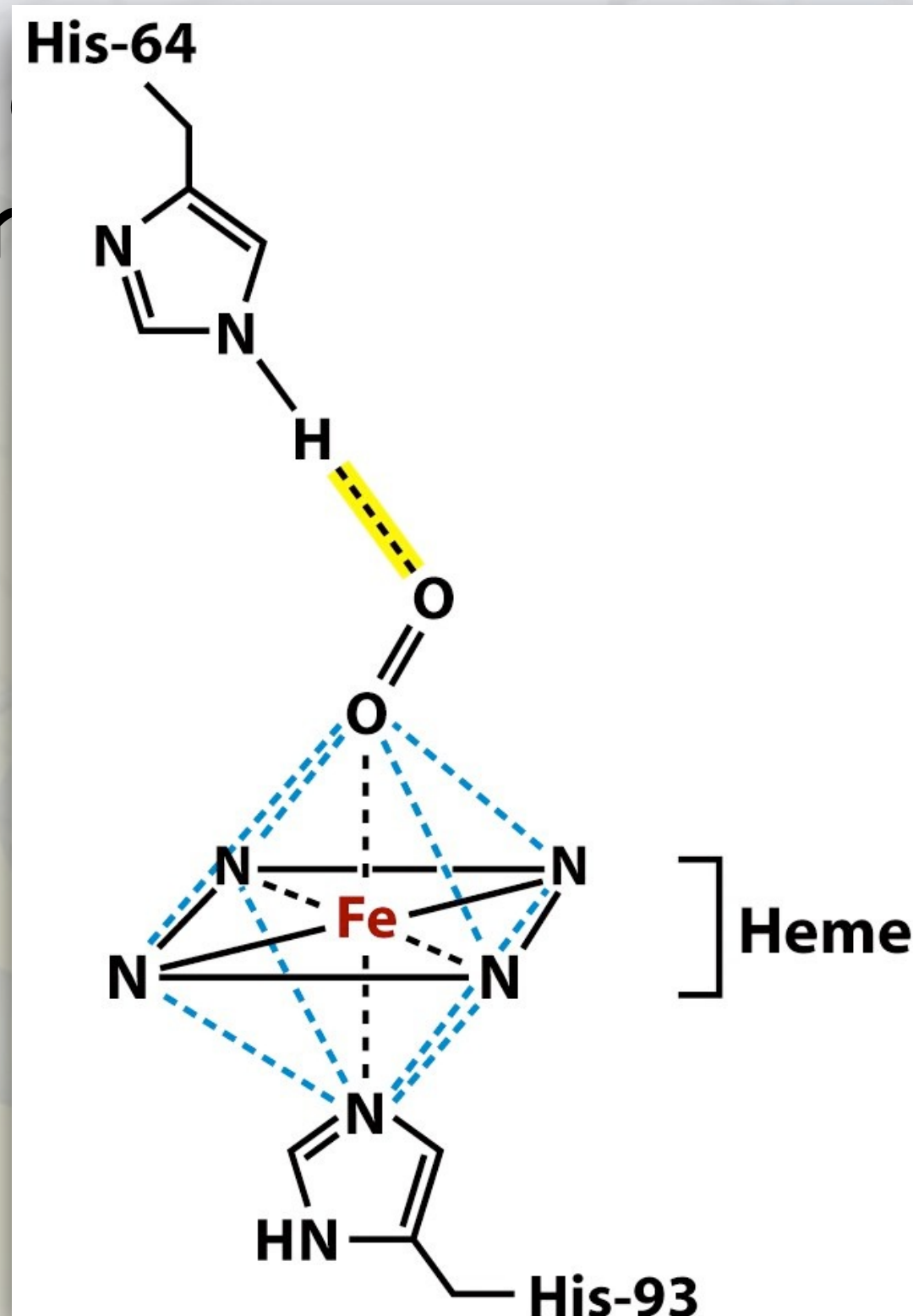
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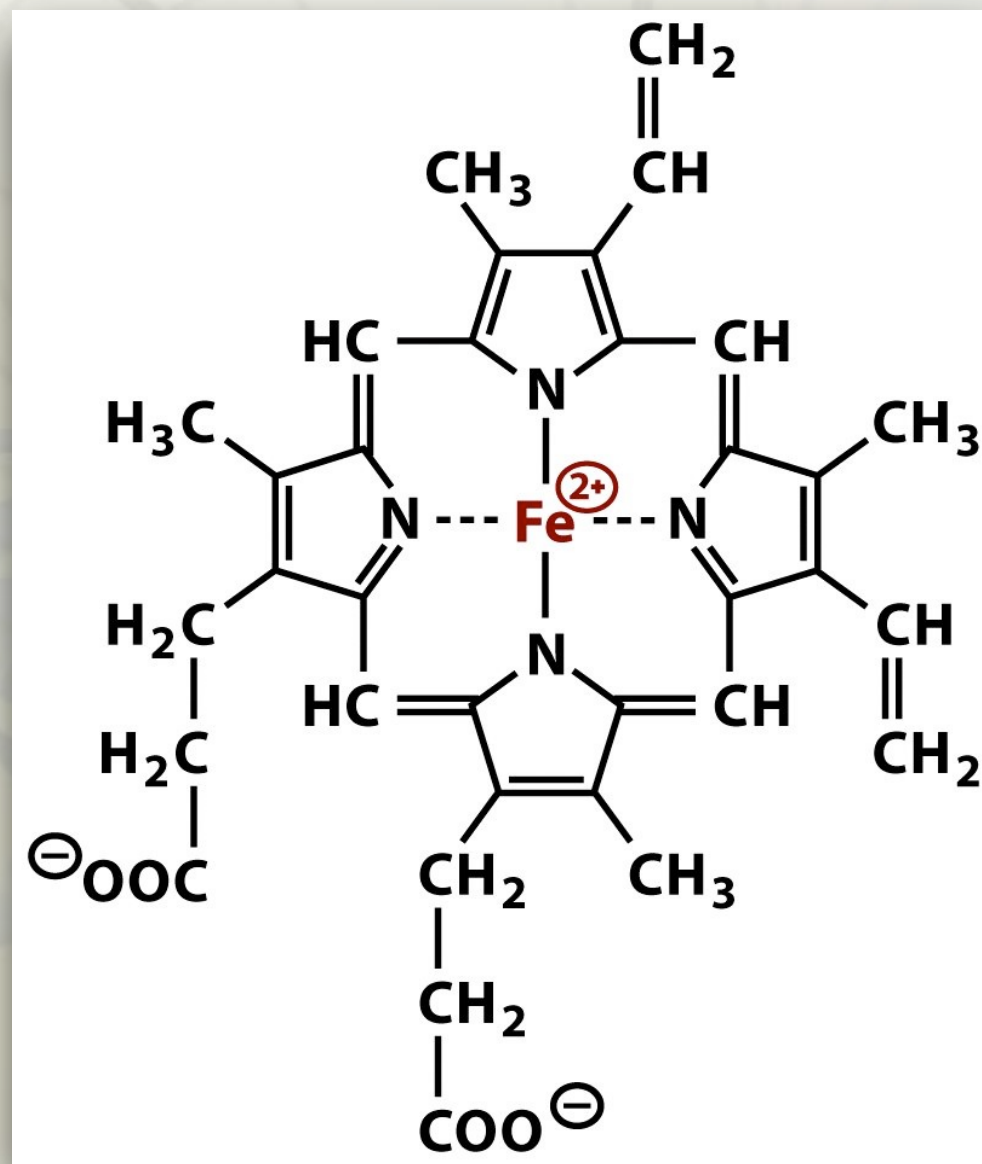
# Myoglobin and Hemoglobin

For both, a heme prosthetic group is used (proteins using a heme prosthetic group are called heme proteins).



# Myoglobin and Hemoglobin

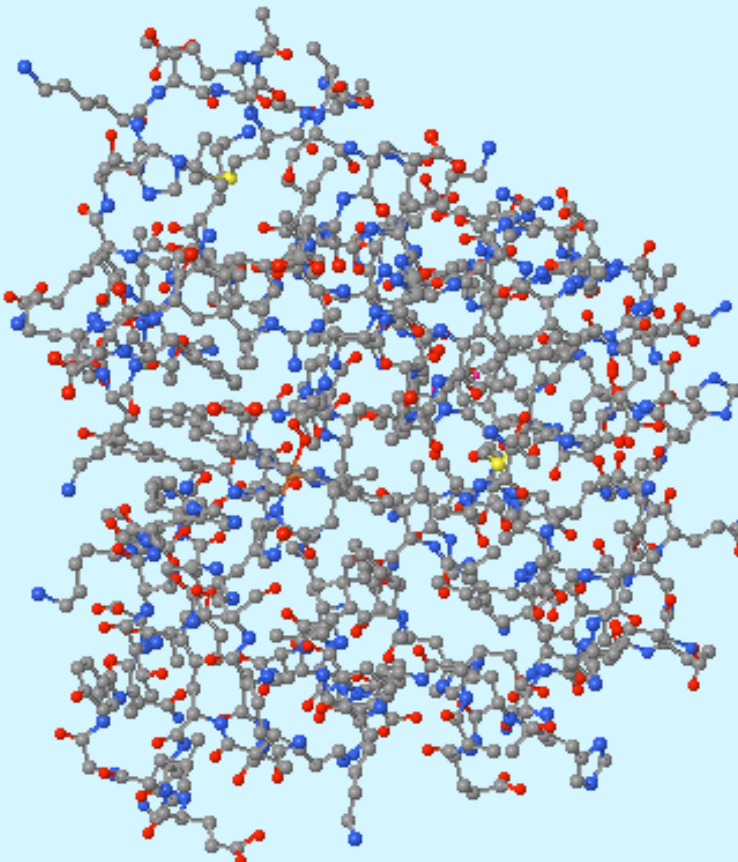
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# Myoglobin and Hemoglobin

Protein Structure - Oxy-myoglobin

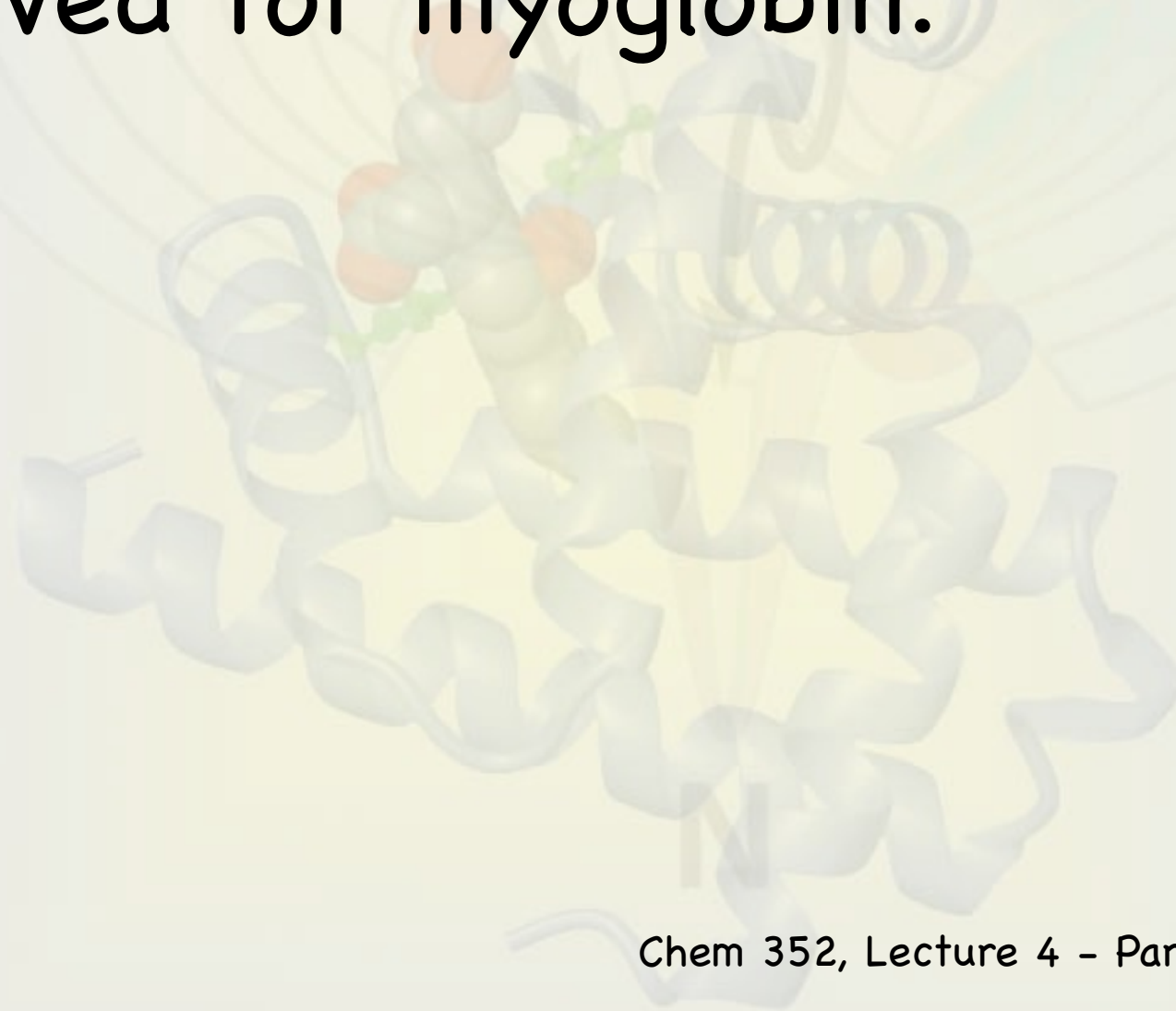


Push buttons in order

- ☒ Ball & stick model of myoglobin
- ☐ Spacefilling model of the heme group
- ☐ Zoom in on heme group
- ☐ Add spacefilling model for the bound dioxygen molecule
- ☐ Show ball & stick model of the proximal histidine
- ☐ Change proximal histidine to spacefilling model
- ☐ Show ball & stick model of the distal histidine
- ☐ Change distal histidine to spacefilling model
- ☐ Return to home

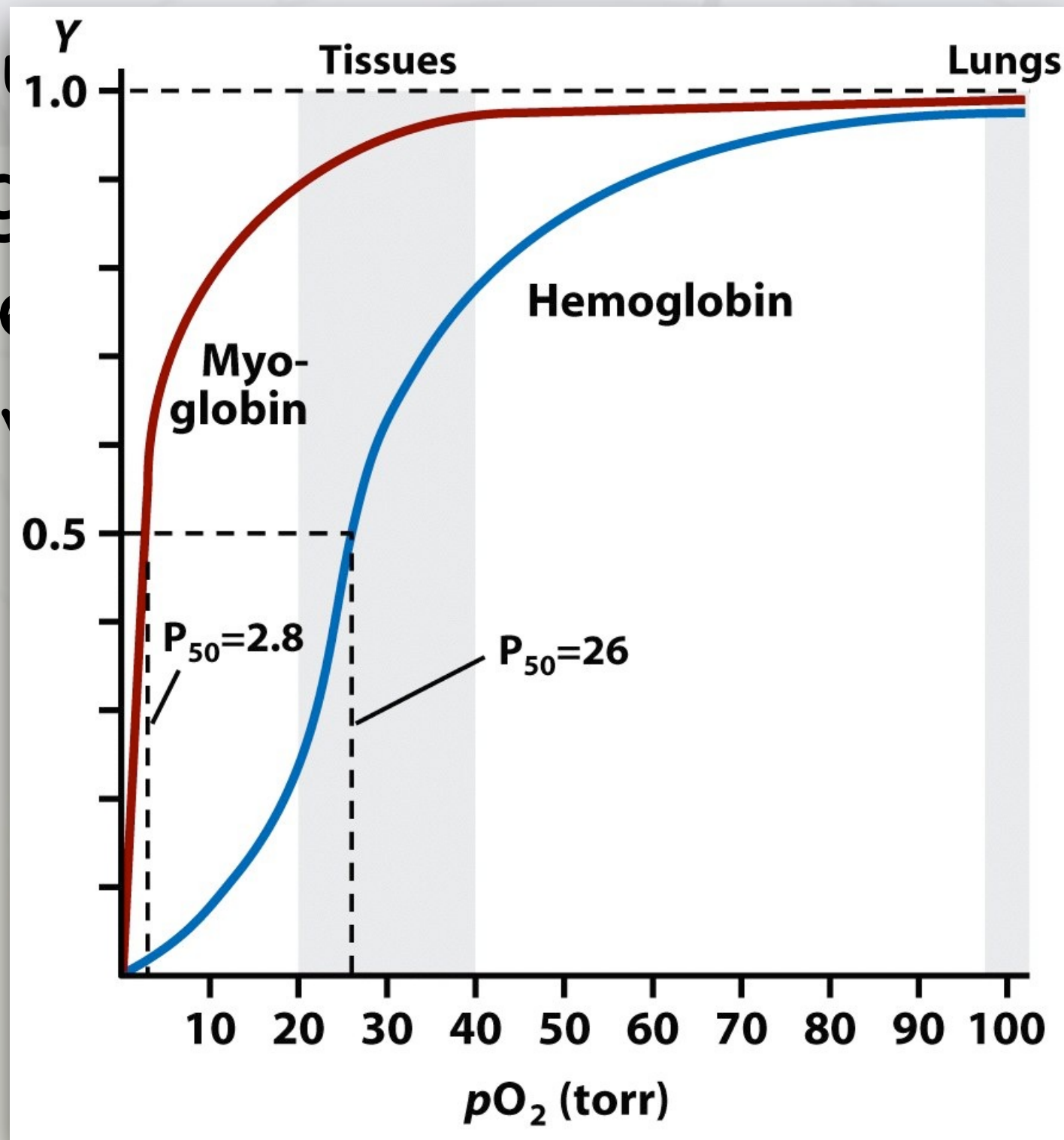
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The quaternary structure for hemoglobin produces a distinctly different oxygen binding behavior than observed for myoglobin.



# Myoglobin and Hemoglobin

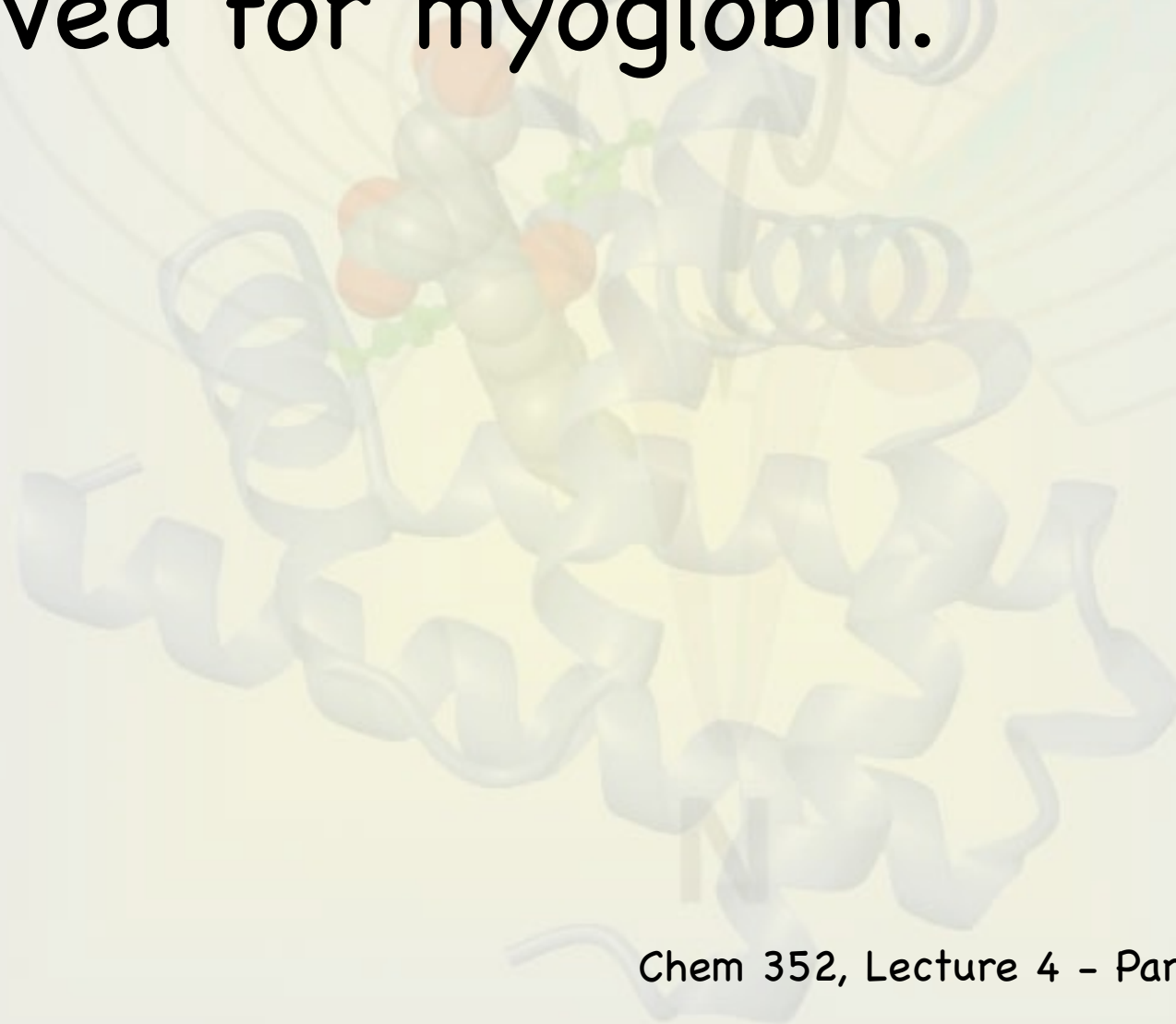
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# Myoglobin and Hemoglobin

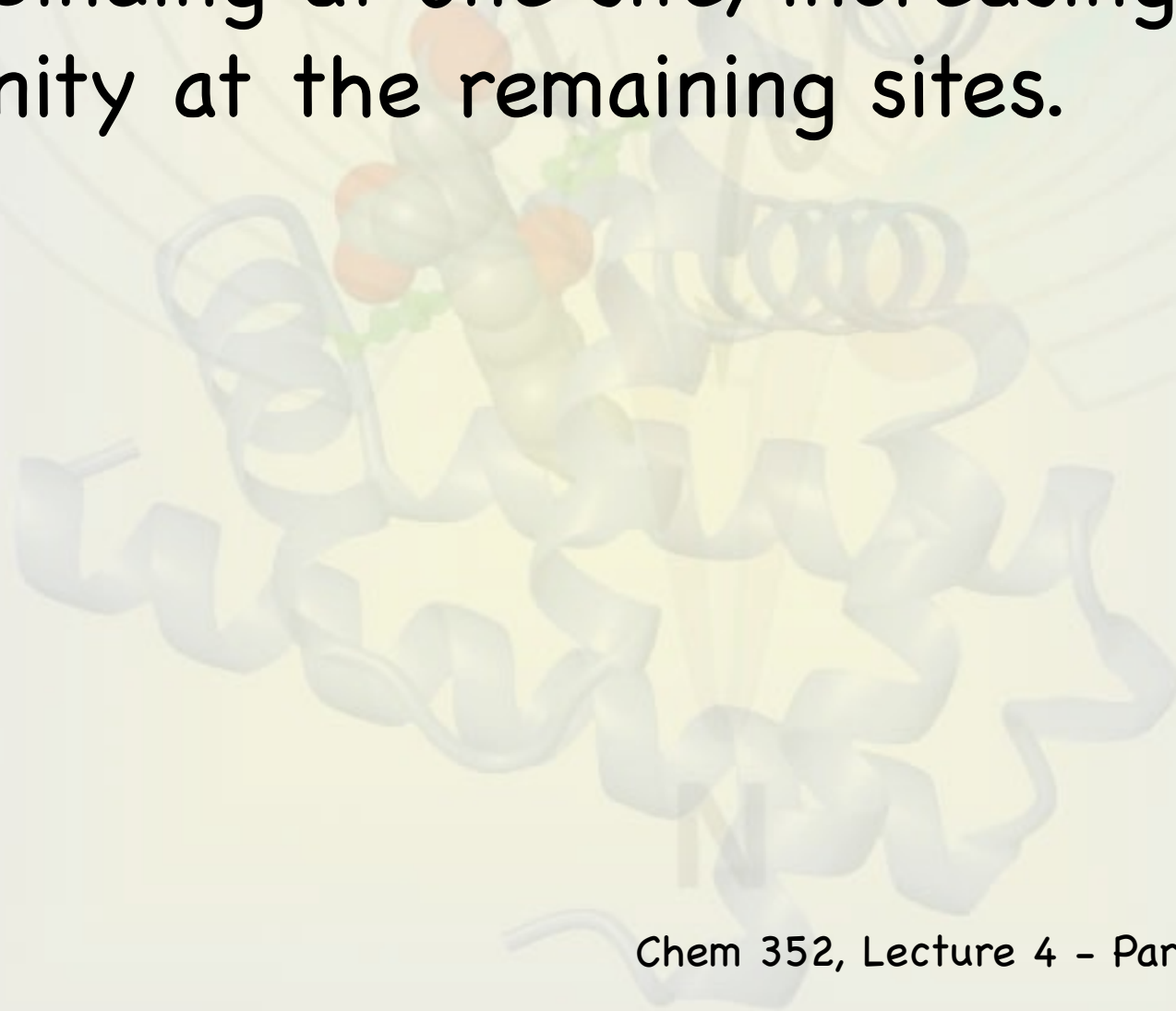
The quaternary structure for hemoglobin produces a distinctly different oxygen binding behavior than observed for myoglobin.



# Myoglobin and Hemoglobin

The four oxygen binding sites in hemoglobin communicate with one another.

- ✦  $O_2$  binding at one site, increasing the binding affinity at the remaining sites.





# Myoglobin and Hemoglobin

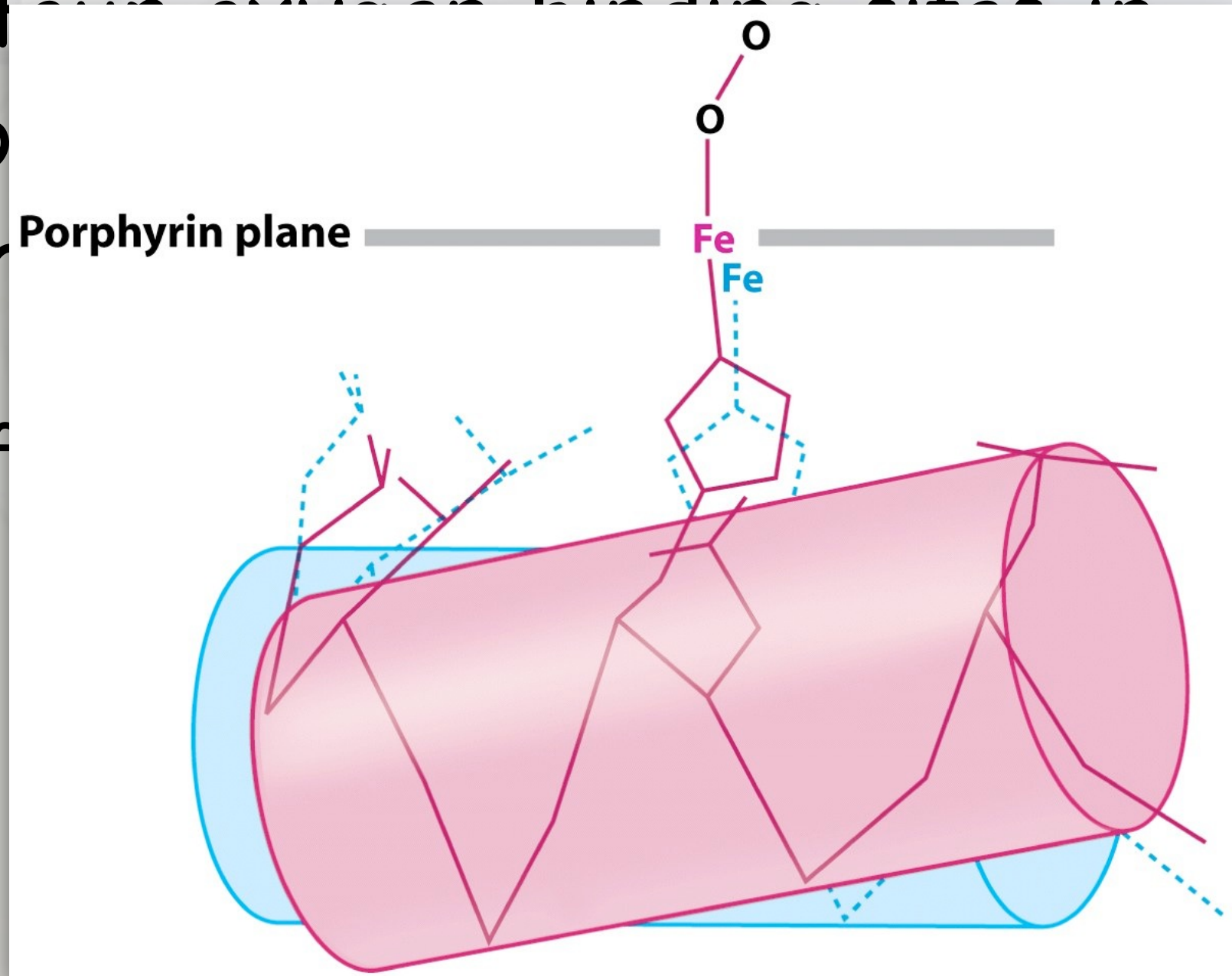
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hemo

another

✦  $O_2$   
aff

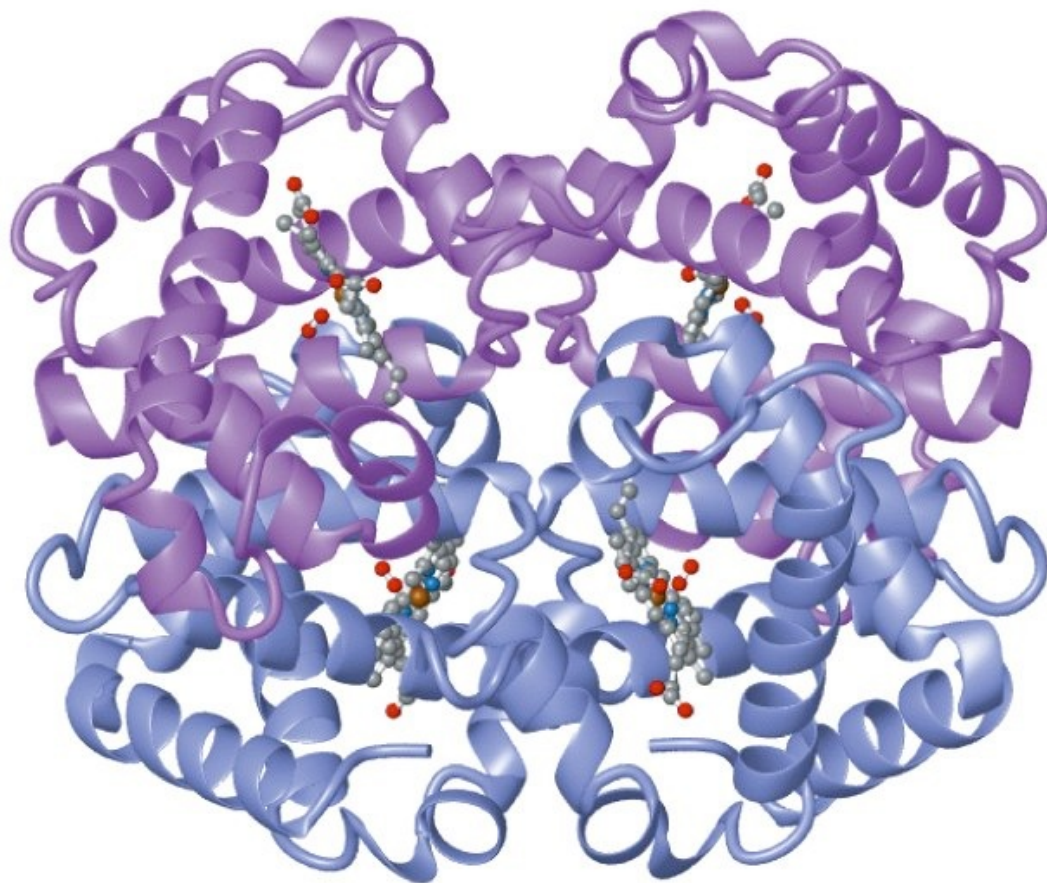
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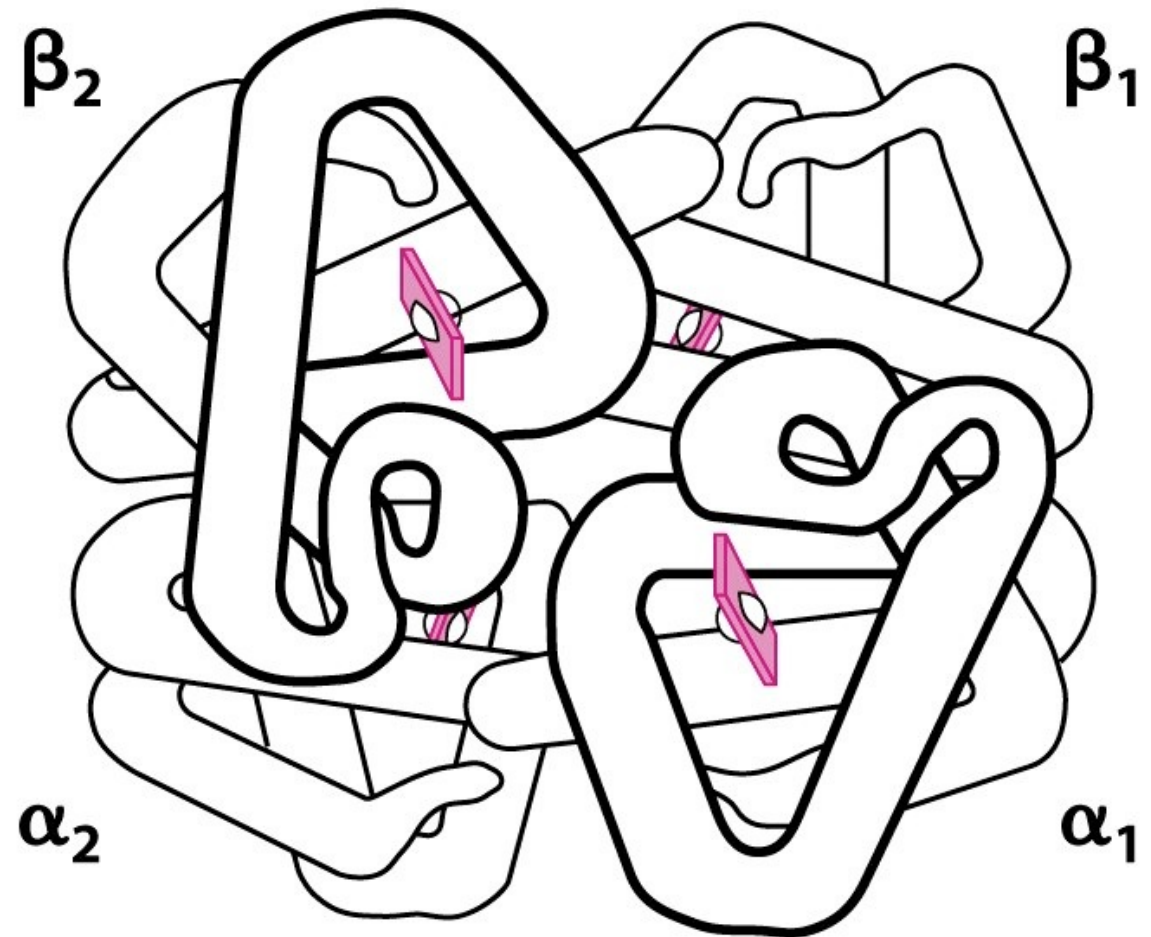
# Myoglobin and Hemoglobin

The four oxygen binding sites in

(a)



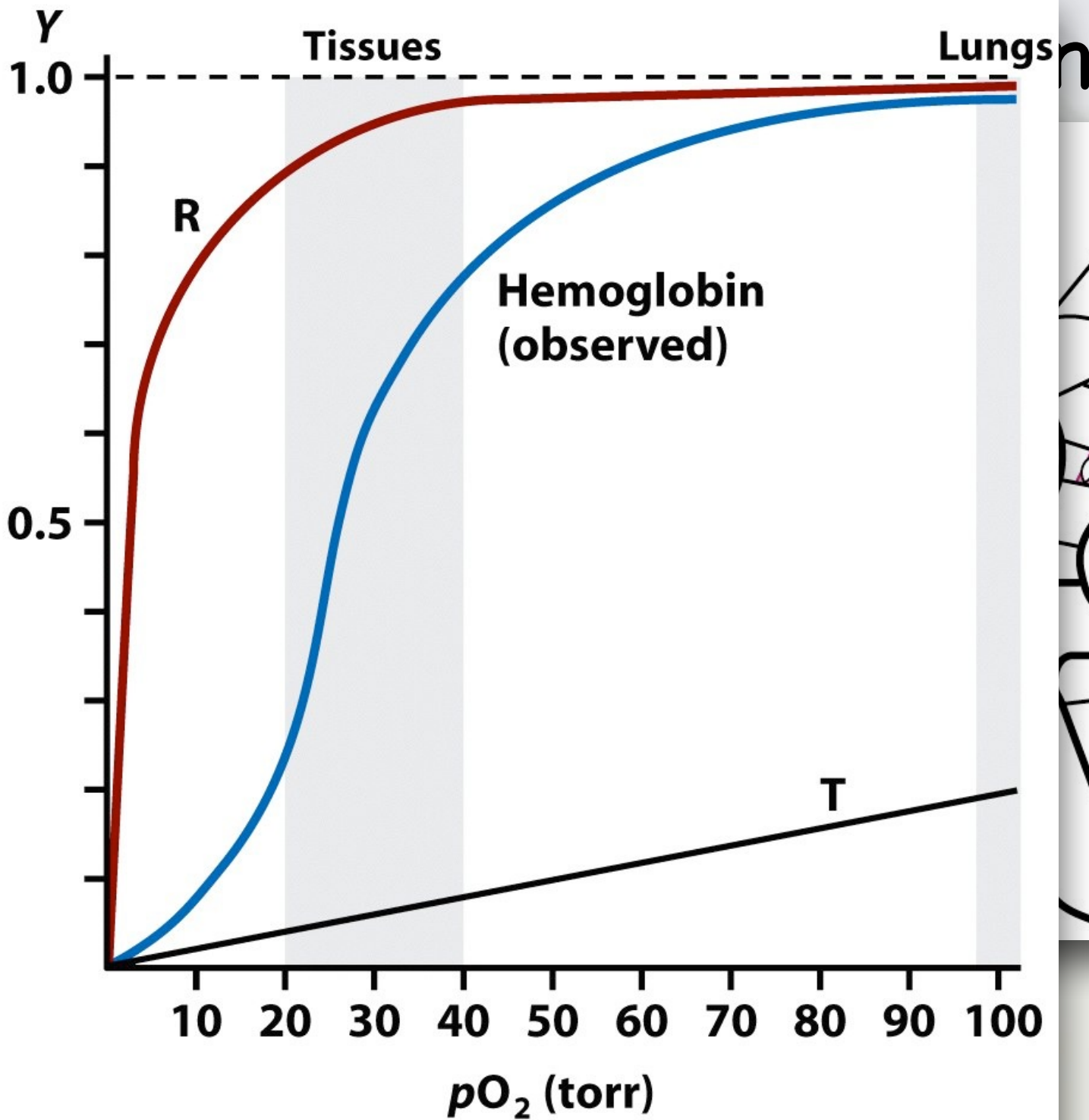
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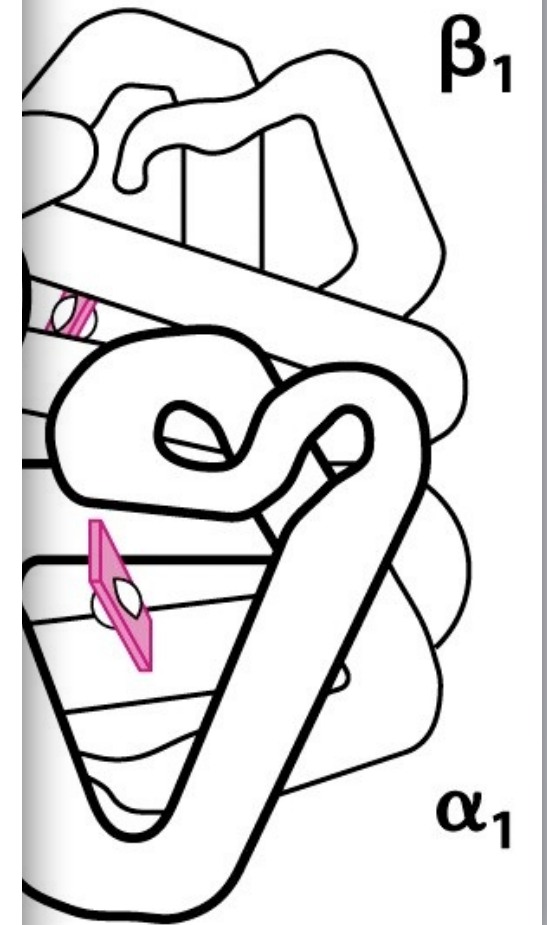


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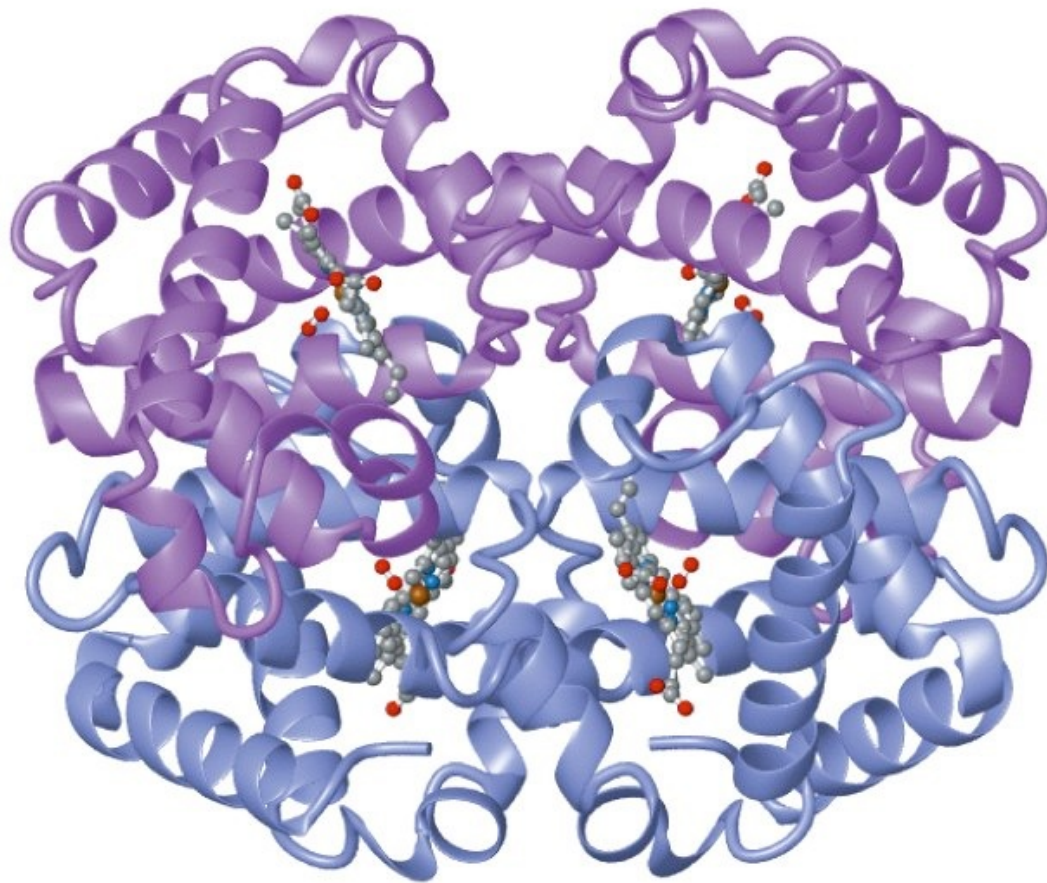
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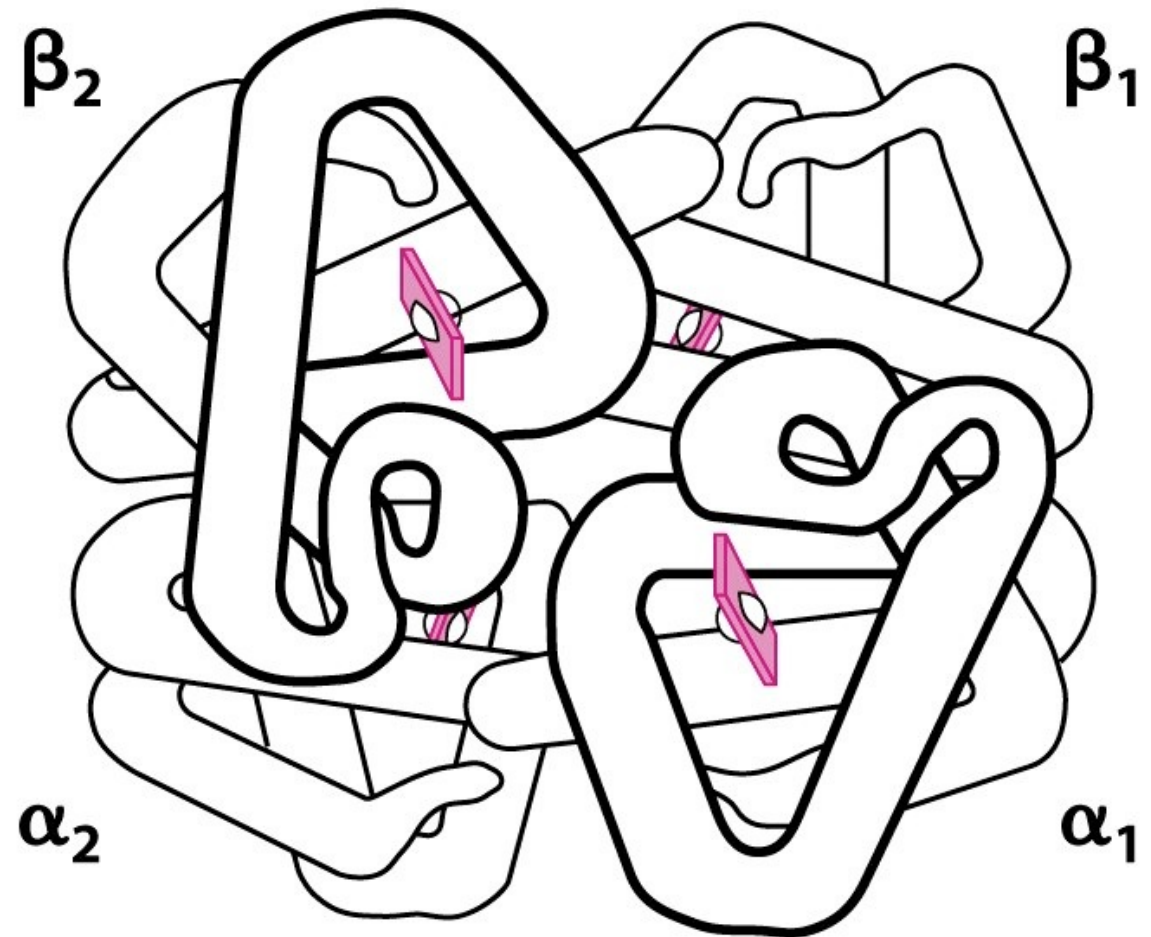
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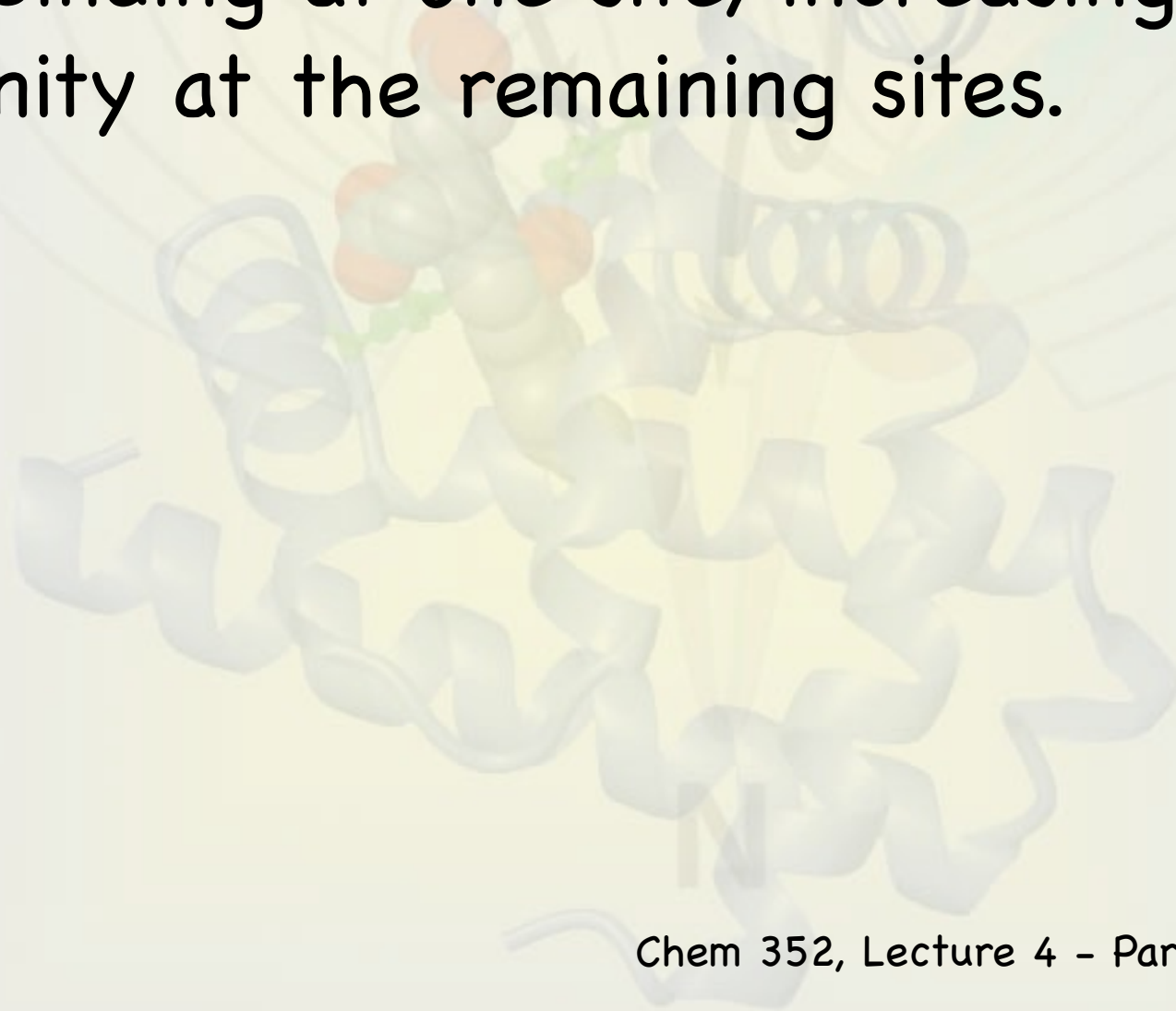




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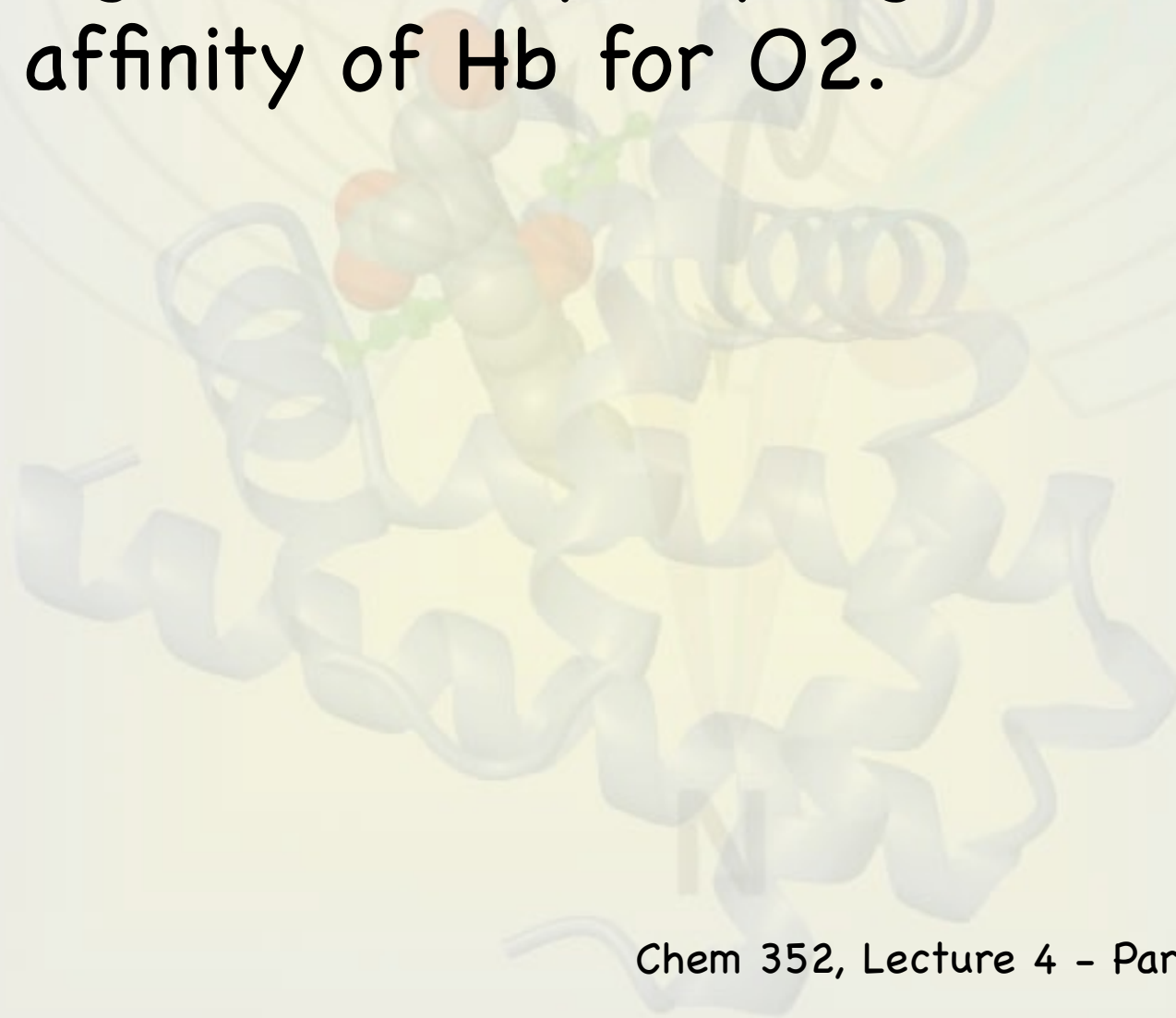
- ✦  $O_2$  binding at one site, increasing the binding affinity at the remaining sites.



# Myoglobin and Hemoglobin

Hemoglobin also provides an example of allosteric regulation.

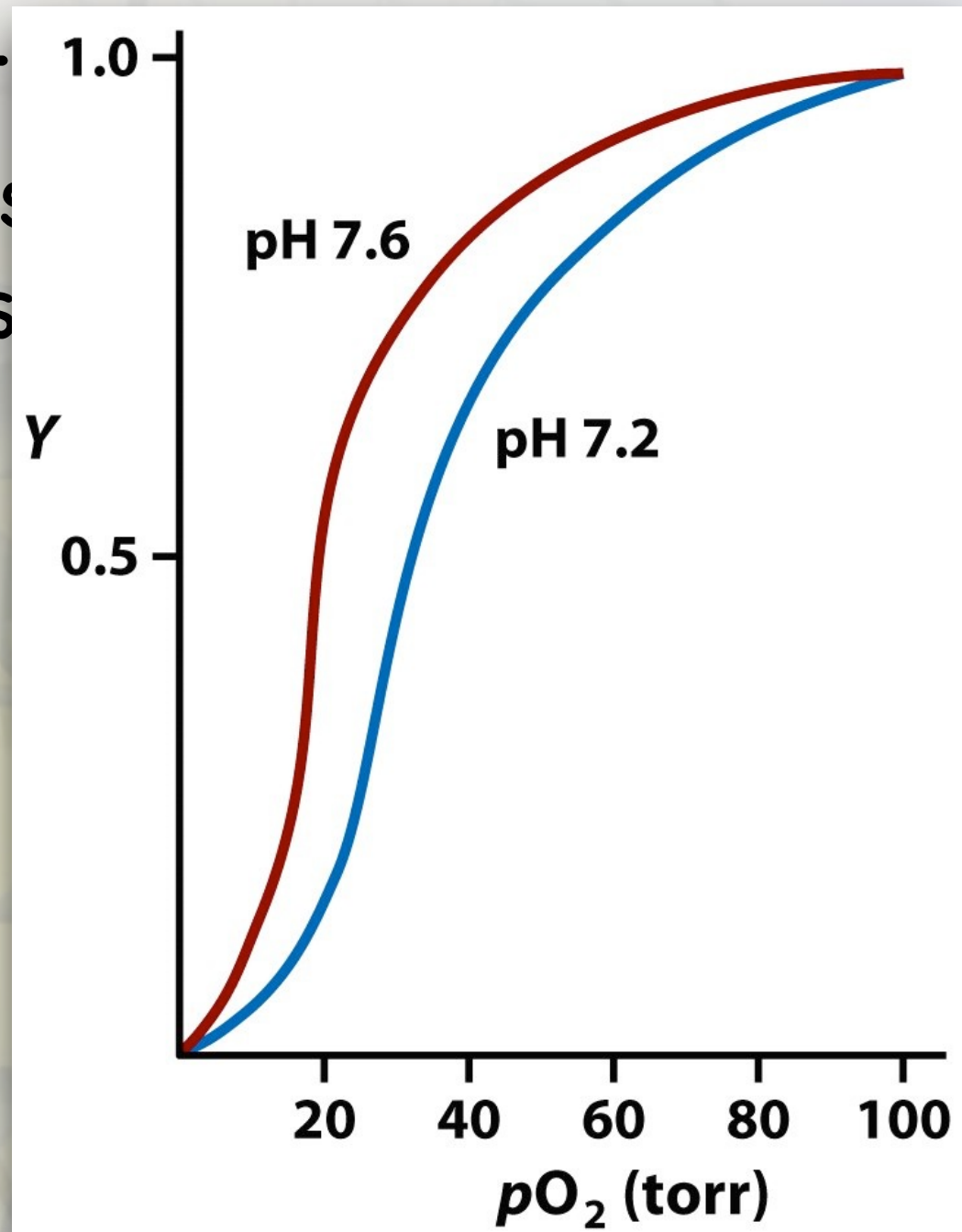
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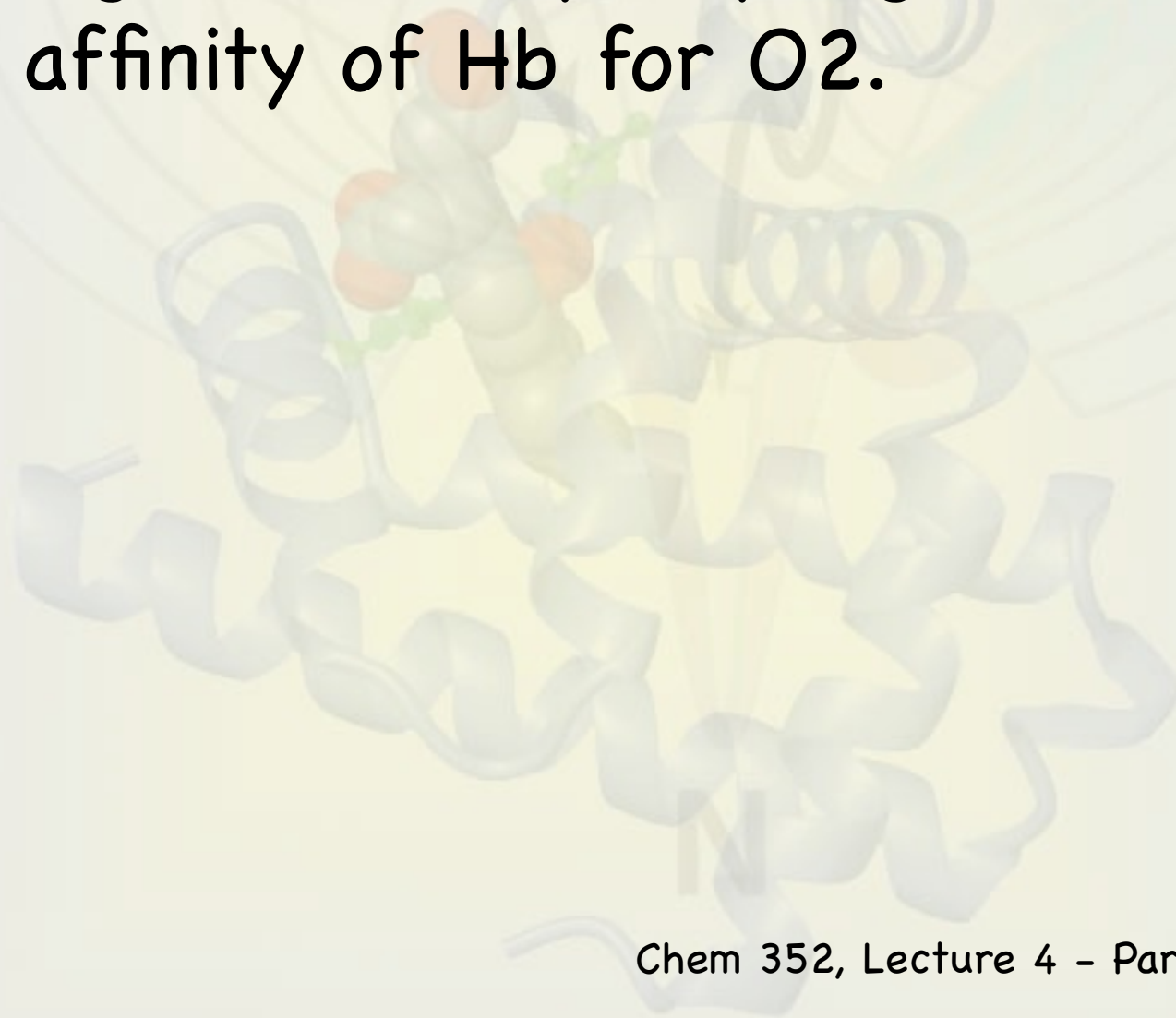
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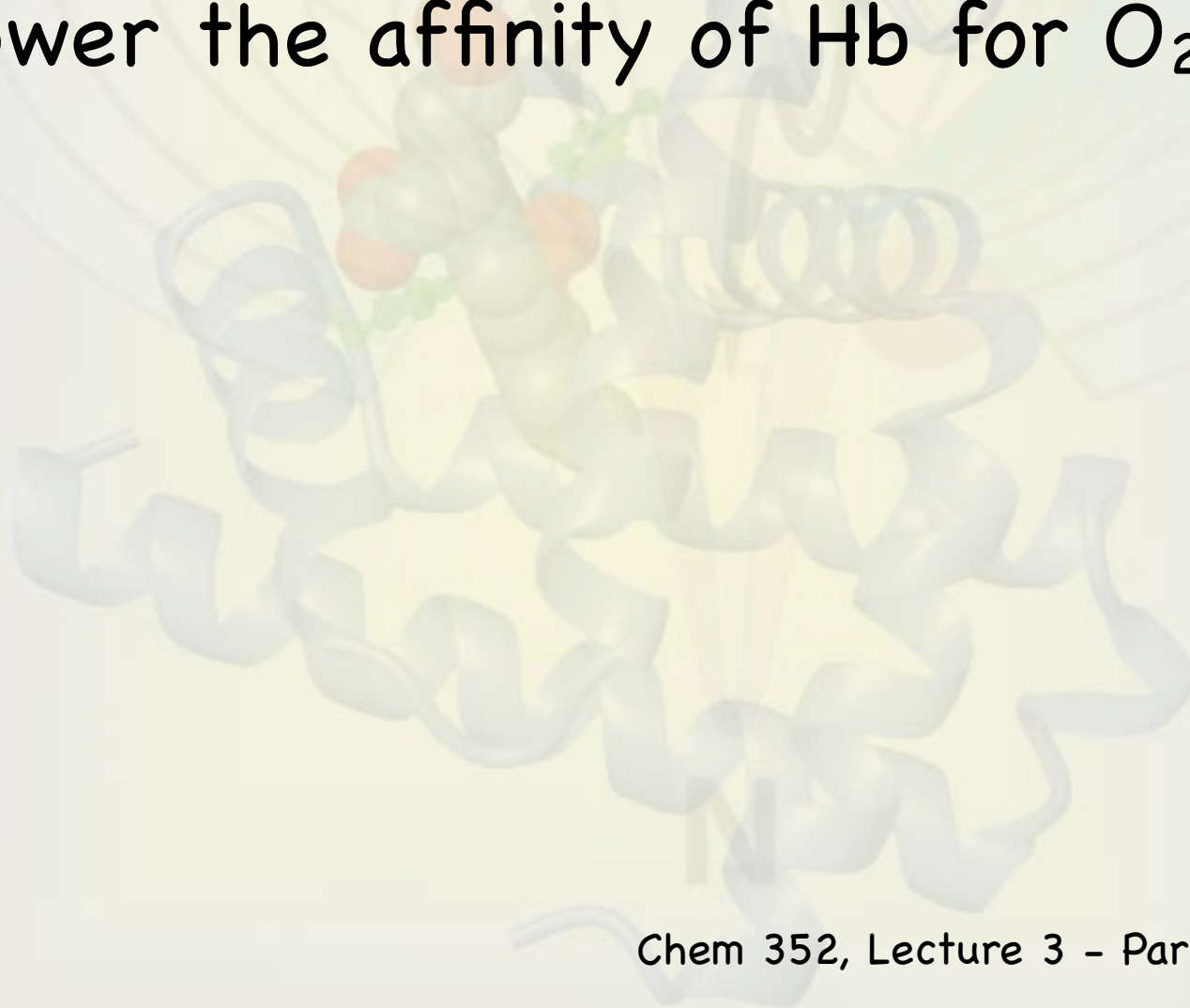
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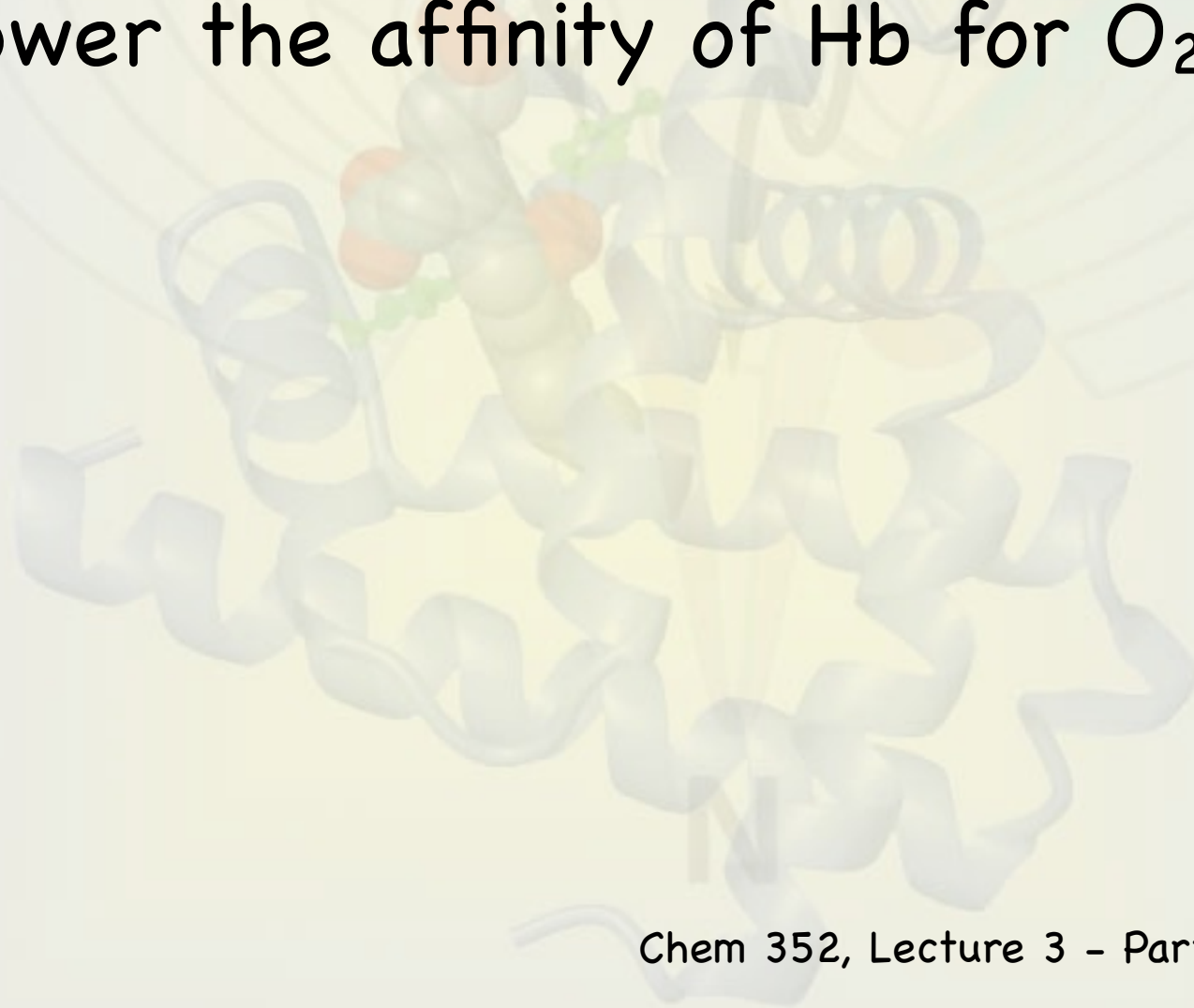
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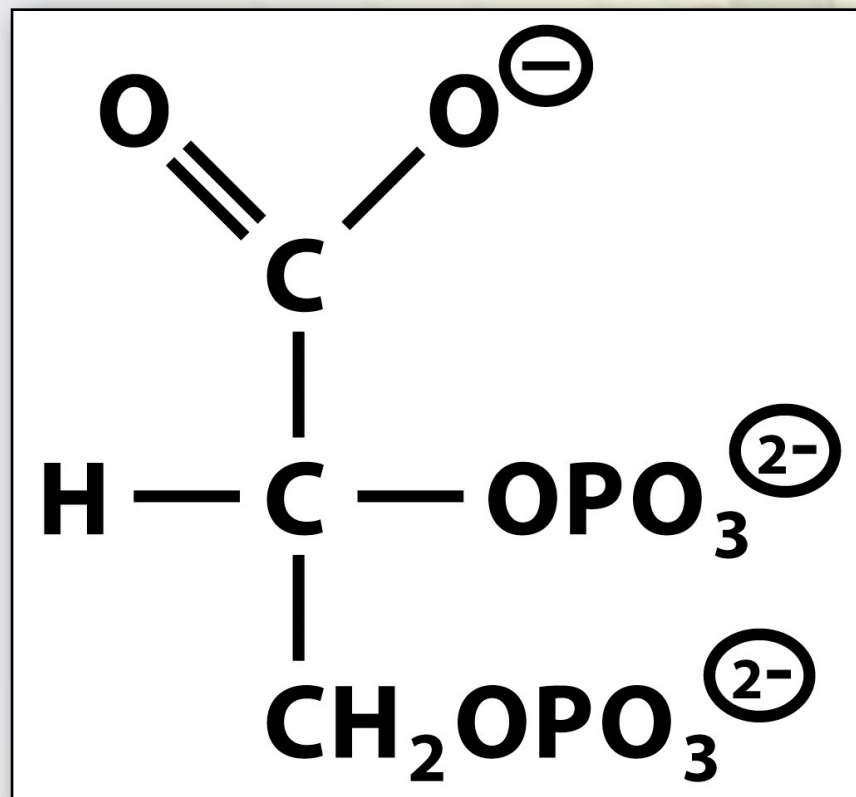
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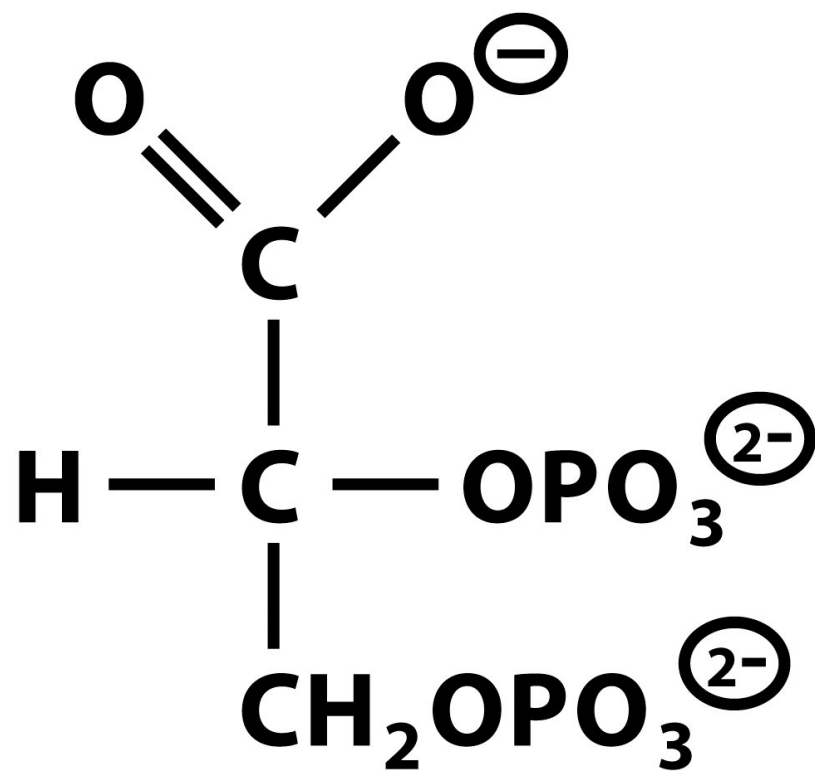
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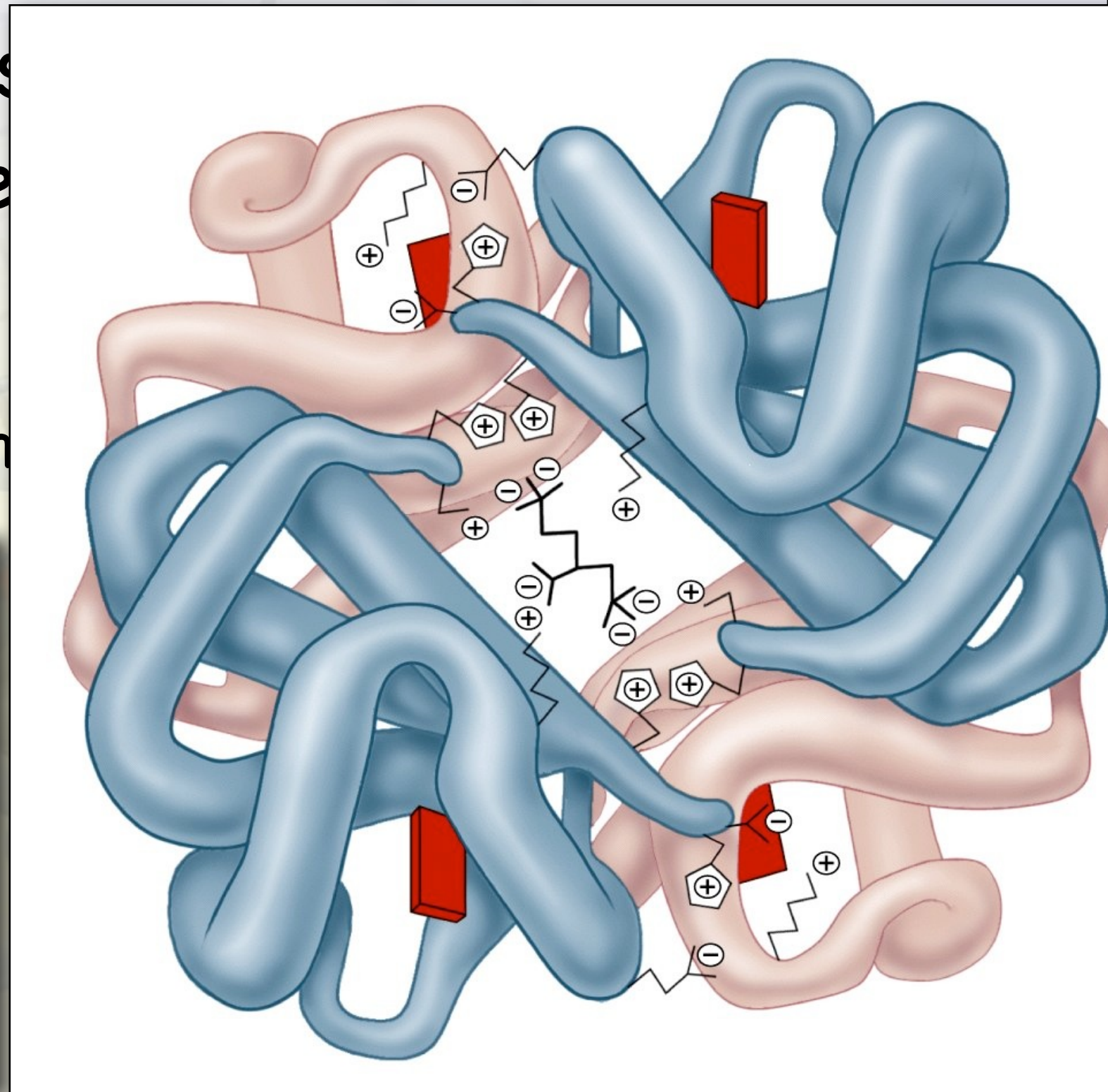
2,3-Bisphosphoglycerate

# Myoglobin and Hemoglobin

- Hemoglobin also exhibits allosteric regulation
  - The binding of 2,3-bisphosphoglycerate (BPG) to the binding site of deoxyhemoglobin lowers the affinity for oxygen.



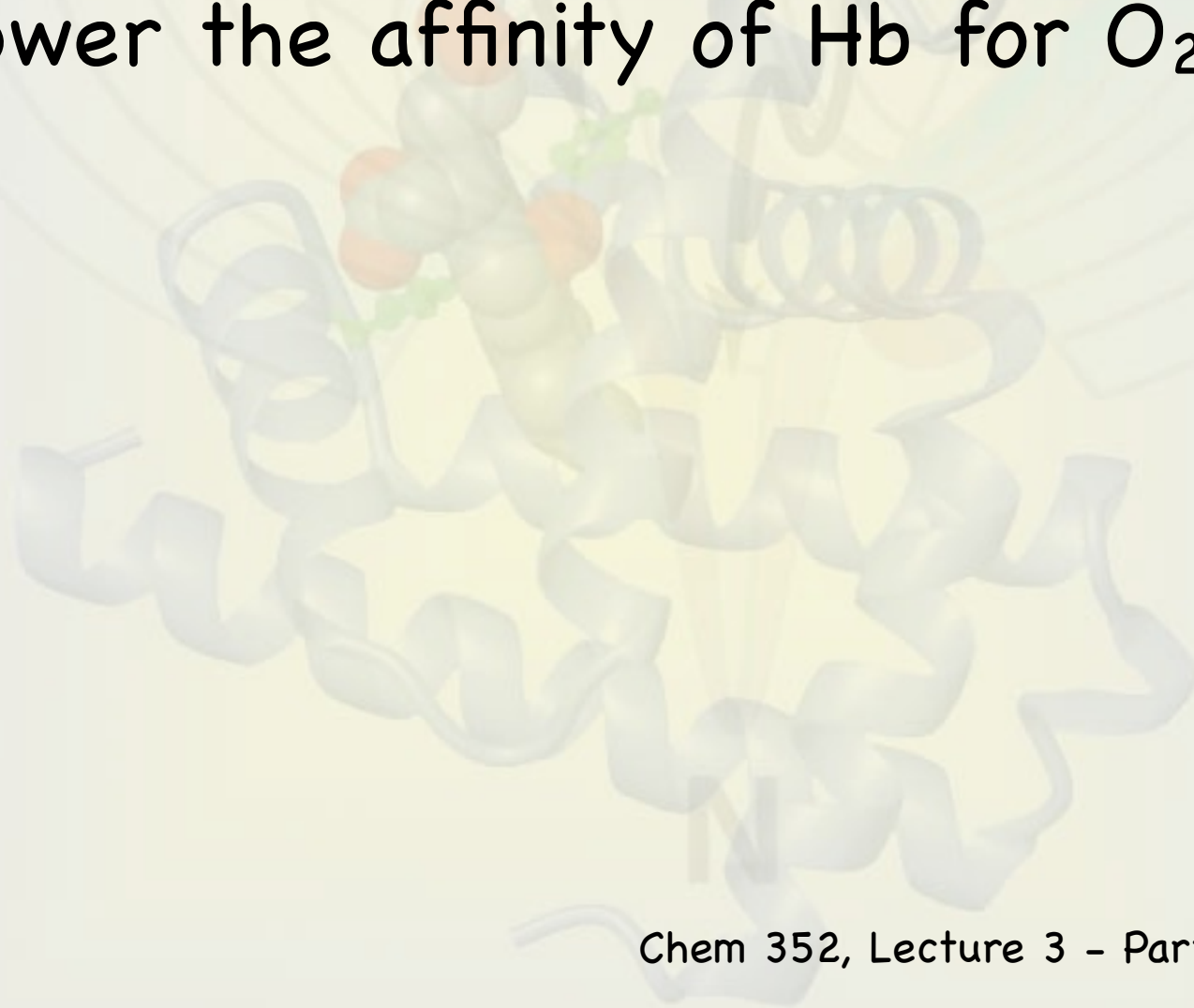
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# Enzyme Nomenclature

nomenclature |'nōmən,klā ch ər|

noun

the devising or choosing of names for things, esp. in a science or other discipline.

- the body or system of such names in a particular field : *the nomenclature of chemical compounds.*
- formal the term or terms applied to someone or something : “*customers*” *was preferred to the original nomenclature “passengers.”*

DERIVATIVES

**nomenclatural** |,nōmən'klā ch ərəl| |"noumən"kleitʃ(ə)rəl| |-

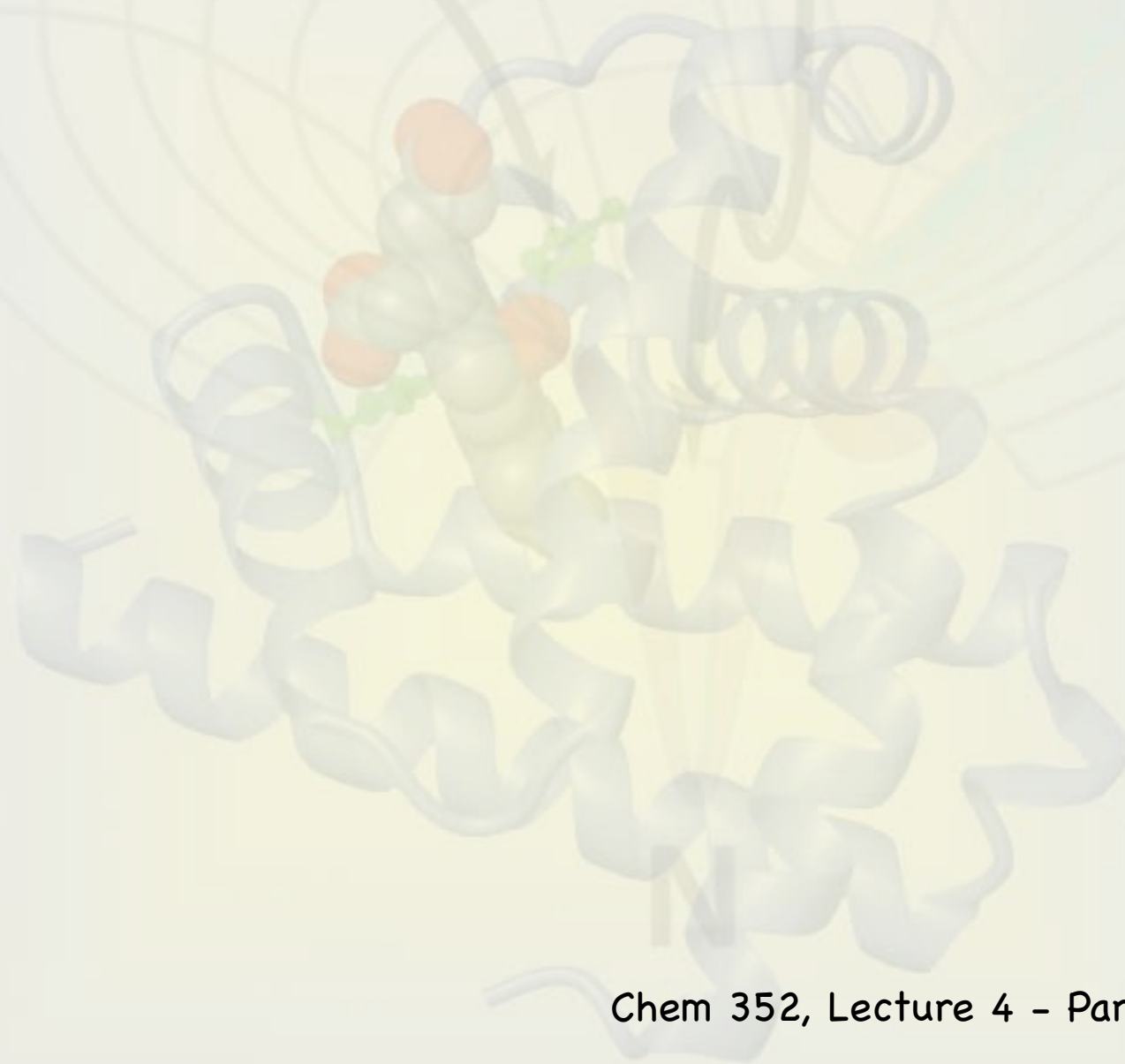
'klatʃ(ə)r(ə)l| |-klə'tʃʊər(ə)l| adjective

ORIGIN early 17th cent.: from French, from Latin *nomenclatura*, from *nomen* ‘name’ + *clatura* ‘calling, summoning’ (from *calare* ‘to call’).



# Enzyme Nomenclature

The Systematic names of enzymes use numbers



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- ✦ The numbers describes
  - the class of reaction
  - the substrates used in the reaction
  - the products produced in the reaction
- ✦ The scheme for deriving these number is defined by the International Union of Biochemistry and Molecular Biology (IUBMB)

# Enzyme Nomenclature

- Systematic names use numbers
  - ✦ pyruvate kinase – EC 2.7.1.40
  - ✦ alcohol dehydrogenase – EC 1.1.1.1

# Enzyme Classes

## •Oxidoreductases (1.)

- ✦ Catalyze oxidation–reduction reactions
- ✦ For example
  - lactate dehydrogenase
    - ✦ lactate:NAD oxidoreductase (EC 1.1.1.27)

## •Distinguishing features:

- ✦ Many (dehydrogenases) involve addition or removal of  $H_2$  as  $H:- + H^+$

# Enzyme Classes

## •Transferases (2.)

- ✦ Catalyze the transfer of a group from one molecule to another
- ✦ For example
  - L-alanine amino transferase
    - ✦ L-alanine:2-oxyglutarate aminotransferase (EC 2.6.1.2)

## •Distinguishing features:

- ✦ Look for double-replacement reactions



# Enzyme Classes

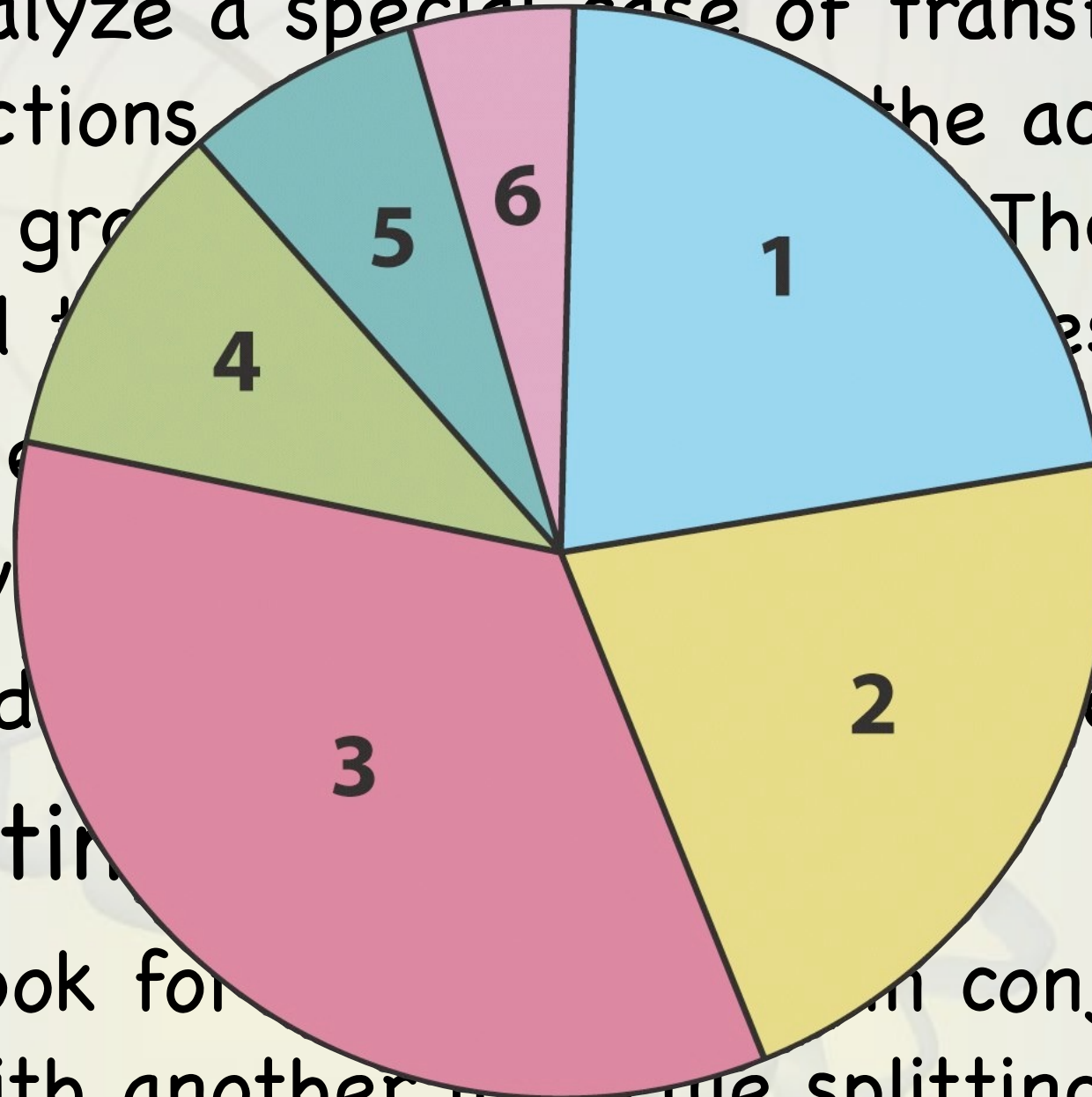
## •Hydrolases (3.)

- ✦ Catalyze a special case of transfer reactions, where water is the acceptor of the group being transferred. The reactions lead to the splitting of molecules in two.
- ✦ For example
  - pyrophosphatase
    - ✦ diphosphate phosphohydrolase (EC 3.6.1.1)
- ✦ Distinguishing features:
  - Look for water splitting in conjunction with another molecule splitting

# Enzyme Classes

## •Hydrolases (3.)

- ✦ Catalyze a special case of transfer reactions where the acceptor of the group is water. The reactions lead to the cleavage of the molecule in two.
- ✦ For example:
  - pyruvate decarboxylase (EC 3.6.1.1)
- ✦ Distinction between hydrolases and lysozymes
  - Look for the presence of another molecule splitting



# Enzyme Classes

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- ✦ For example
  - pyrophosphatase
    - ✦ diphosphate phosphohydrolase (EC 3.6.1.1)
- ✦ Distinguishing features:
  - Look for water splitting in conjunction with another molecule splitting

# Enzyme Classes

## •Lyases (4.)

- ✦ Catalyze a lysis of a substrate, which is nonoxidative, nonhydrolytic and generates a double bond.
- ✦ For example
  - pyruvate decarboxylase
    - ✦ pyruvate decarboxylase, 2-oxo-acid carboxy-lyase (EC 4.1.1.1)
- ✦ Distinguishing features:
  - Look for addition and elimination reactions involving the loss or formation of a double



# Enzyme Classes

## • Isomerase (5.)

- ✦ Catalyze a conversion between two isomers.
  - Sometimes referred to as an rearrangement reaction.
- ✦ For example
  - alanine racemase
    - ✦ alanine racemase (EC 5.1.1.1)
- ✦ Distinguishing features:
  - Look for reactions that have only a single substrate and a single product.

# Enzyme Classes

## •Ligase (6.)

- ✦ Catalyze the ligation or joining of two molecules.
  - This reaction usually requires a source of chemical energy, which is often provided by the hydrolysis of ATP to ADP and  $P_i$
- ✦ For example
  - glutamine synthetase
    - ✦ L-glutamate:ammonia ligase (EC 6.3.1.2)
- ✦ Distinguishing features:
  - Look for a combination of two reactions

# Enzyme Kinetics

- ✦ The **kinetics** of a reaction can tell you details about the mechanism of the reaction
- ✦ Kinetics of non-catalyzed reactions
  - The **rate**, or **velocity**, of a reaction is monitored as a function of substrate (reactant) conc.



$$\begin{aligned} \text{Rate} &= \frac{\text{change in concentration}}{\text{change in time}} \\ &= \frac{dP}{dt} = -\frac{dS}{dt} \end{aligned}$$

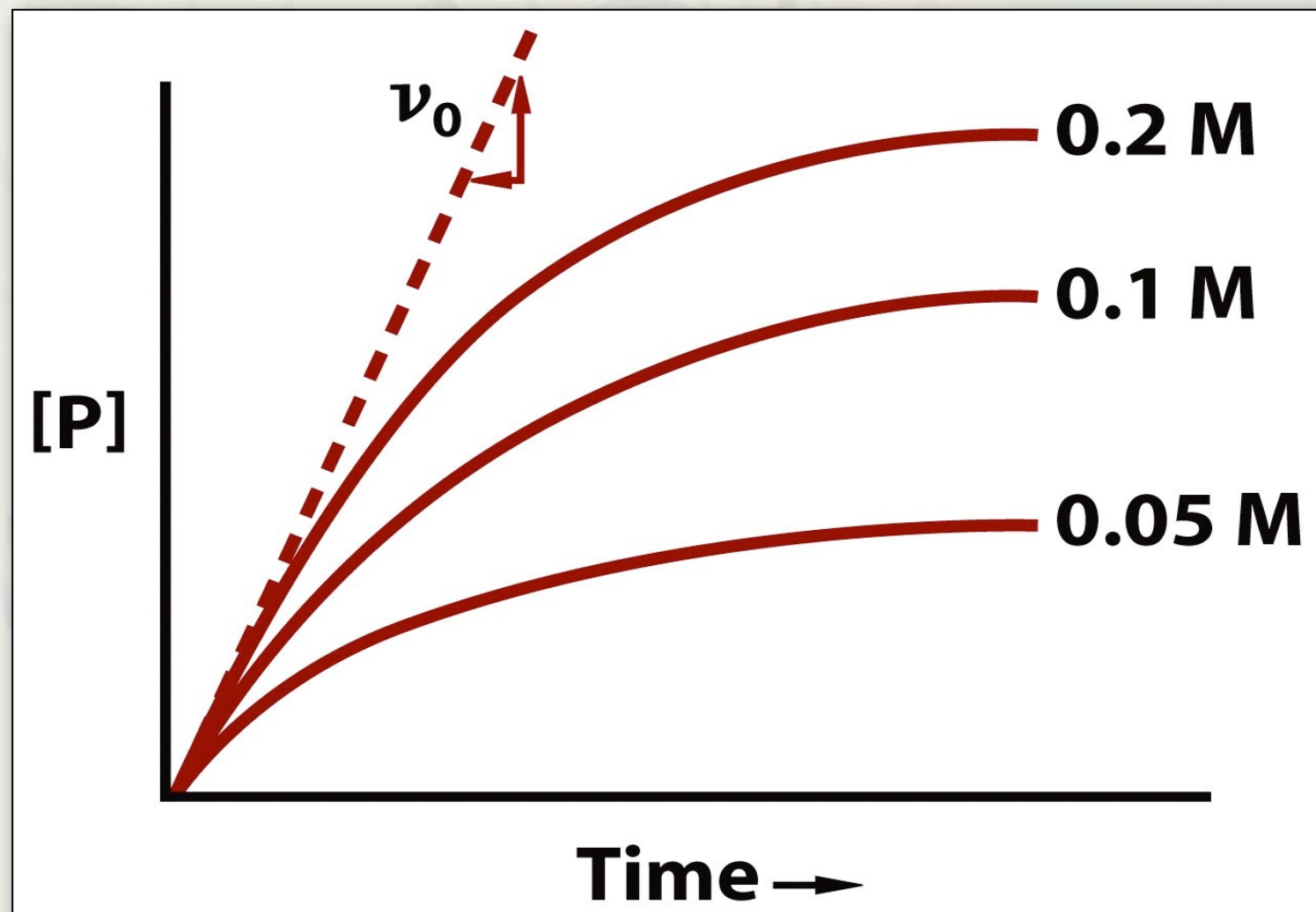
# Enzyme Kinetics

- ✦ The rate equation for this relationship can take on different forms with respect to the substrate or product concentration:
  - ✦ first order
  - ✦ second order
  - ✦ zero order



# Enzyme Kinetics

- Kinetics of non-catalyzed reactions
  - ✦ Typically it is the substrate dependence of the initial rate,  $v_0$ , that is determined.

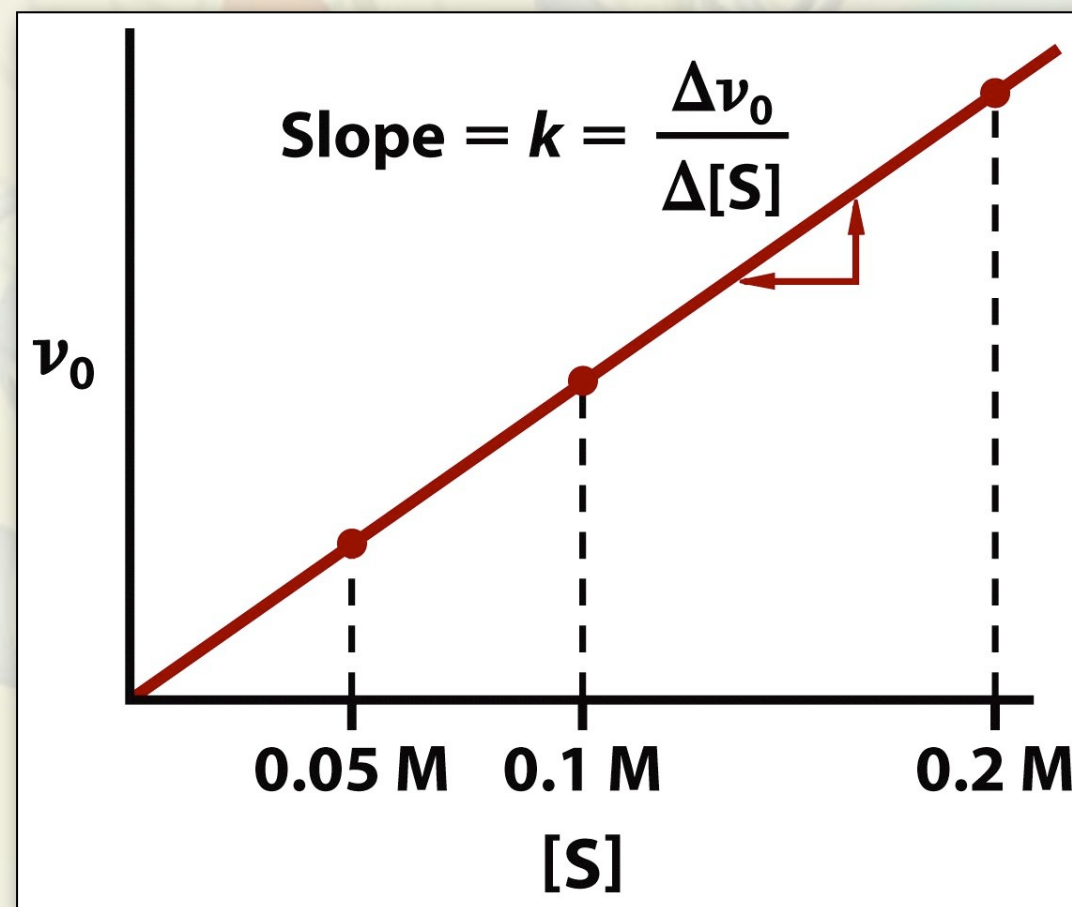


# Enzyme Kinetics

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# Enzyme Kinetics

- Kinetics of non-catalyzed reactions
  - ✦ For a first-order reaction,  $v_0$  has a straight-line dependence on  $[S]$ .
  - ✦  $v_0 = k_1[S]$  ( $k_1$  is first order rate constant)



# Enzyme Kinetics

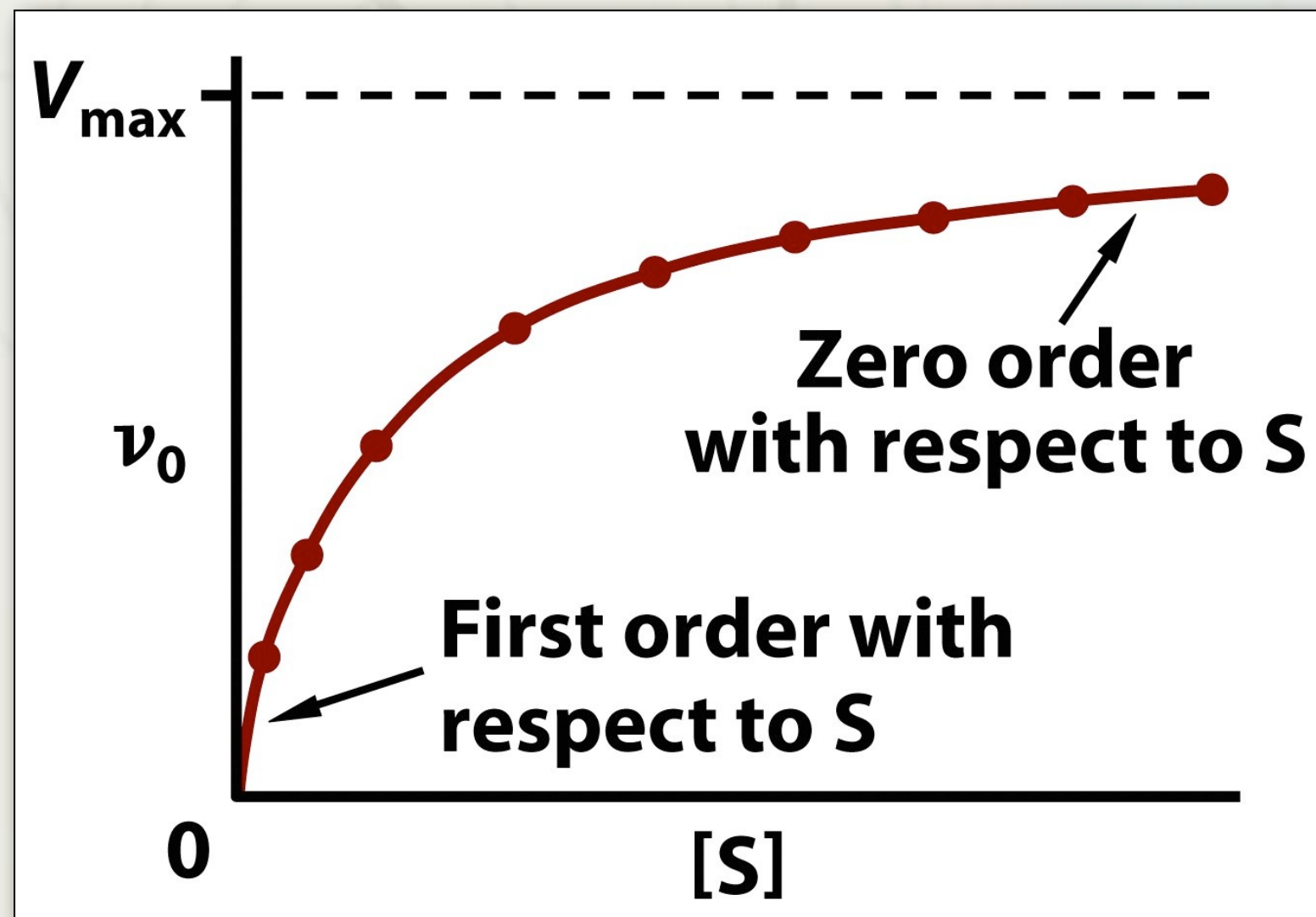
- Kinetics of non-catalyzed reactions

- ✦ For a second order reaction,  $v_o$  has a quadratic dependence on  $[S]$ .
- ✦  $v_o = k_2[S]^2$  ( $k_2$  is second order rate constant)
- ✦ For a zero order reaction,  $v_o$  is independent of  $[S]$
- ✦  $v_o = k_0$  ( $k_0$  is the zero order rate constant)



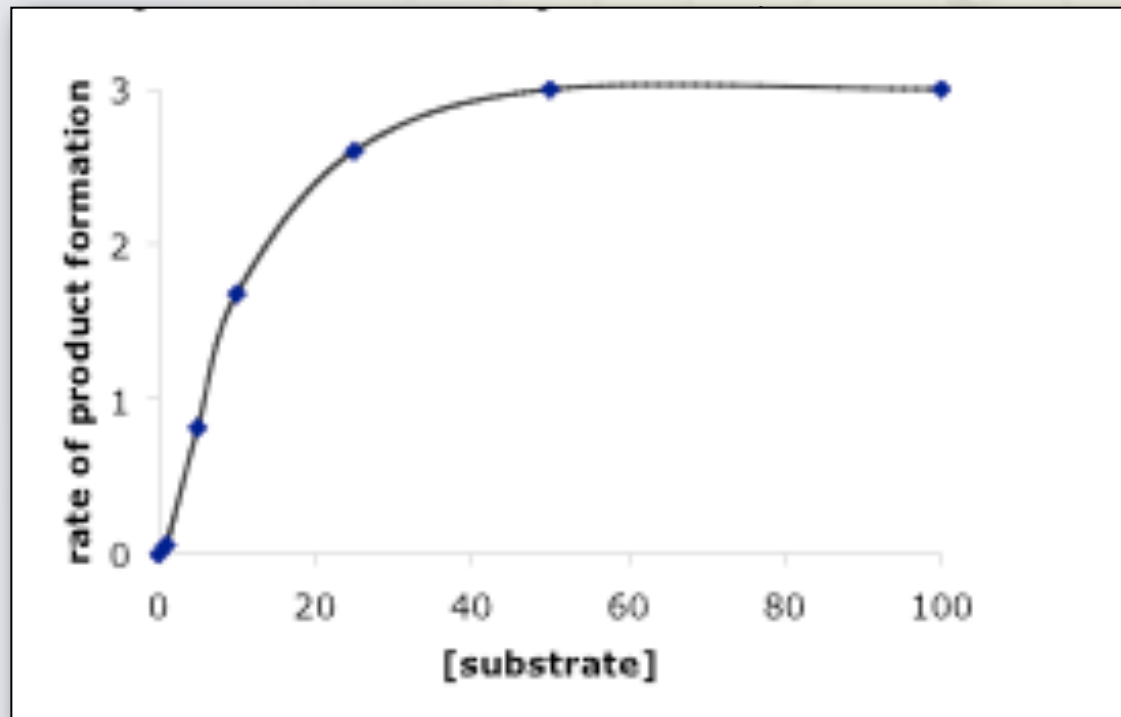
# Enzyme Kinetics

- ✦ The kinetics of an **enzyme catalyzed reaction** looks different.



# Enzyme Kinetics

- Kinetics of enzyme-catalyzed reactions
  - ✦ Michaelis-Menten model for enzyme



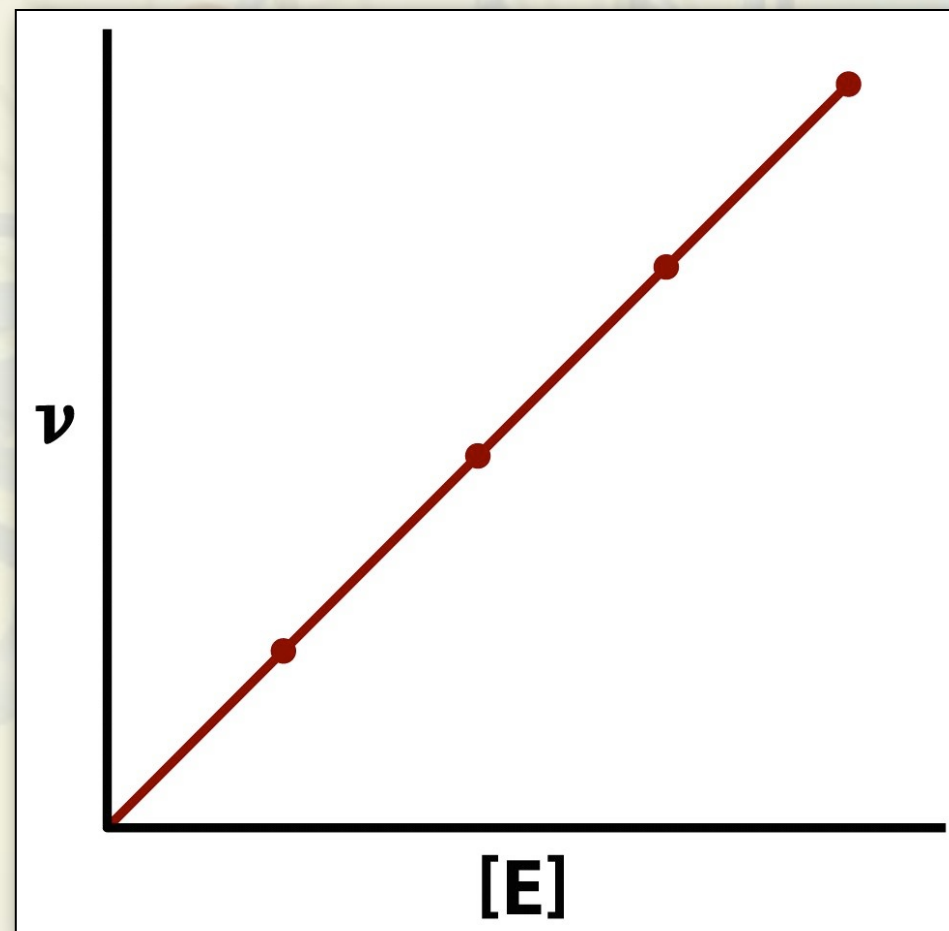
Maud Menten  
(1879-1960)



Leonor Michaelis  
(1875-1949)

# Enzyme Kinetics

- For enzyme-catalyzed reactions
  - ✦ See first-order enzyme concentration,  $[E]$ , dependence at high substrate concentrations  $[S]$ , where kinetics is zero order.



# Enzyme Kinetics

•Proposed the following mechanism for an enzyme catalyzed reaction:



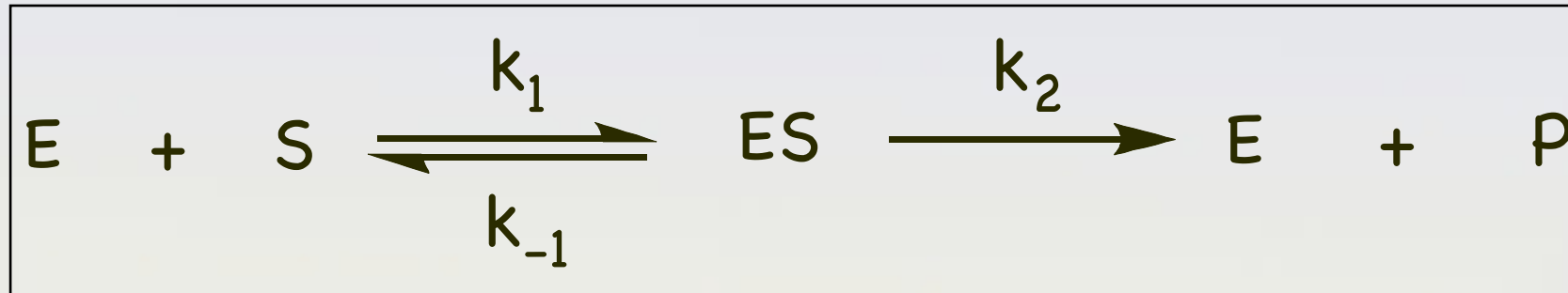
- ✦ The overall rate of the reaction is therefore determined by the conversion of enzyme-substrate complex, ES, to product:

$$v_o = k_2[\text{ES}]$$

- Came up with an expression for [ES] as a function of [S]
  - ✦ Substitution in the the above expression for  $v_o$  will then give  $v_o$  as a function of [S].



# Enzyme Kinetics



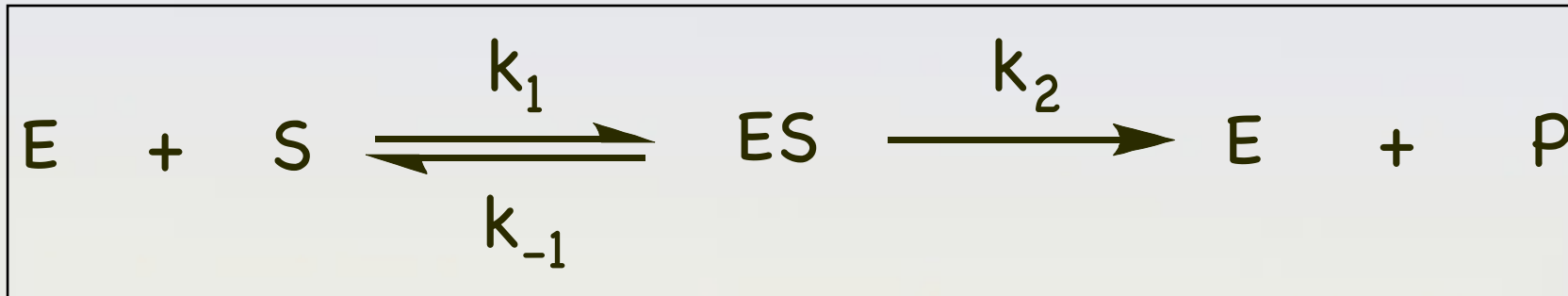
• Proposed that the concentration of ES quickly reaches a steady state, in which the rate at which ES is formed, ( $=k_1[\text{E}][\text{S}]$ ), is equal to the rate at which ES is consumed ( $=k_{-1}[\text{ES}] + k_2[\text{ES}]$ ):

$$k_{-1}[\text{ES}] + k_2[\text{ES}] = k_1[\text{E}][\text{S}]$$

✦ Solving for [ES] gives:

$$[\text{ES}] = \frac{k_1[\text{E}][\text{S}]}{k_{-1} + k_2}$$

# Enzyme Kinetics



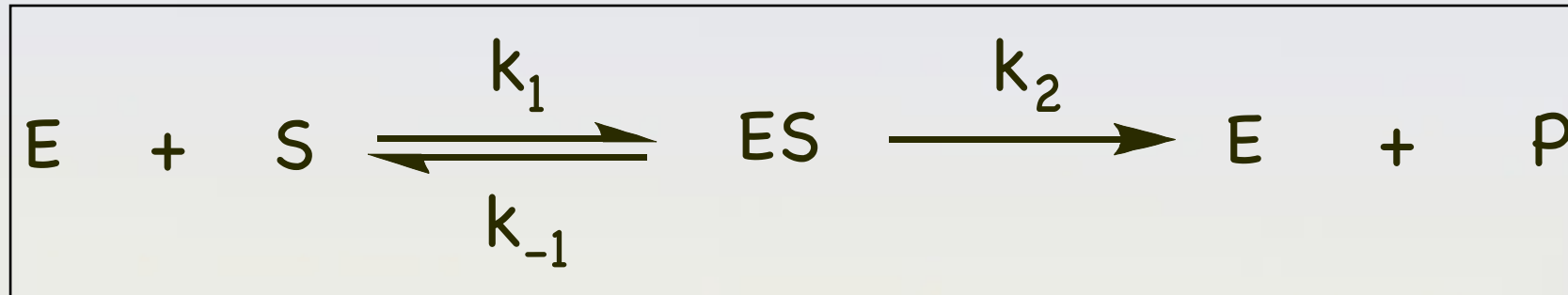
- ✦ The rate constants are combined to produce a single constant,  $K_M$ , called the Michaelis-Menten constant.

$$K_M = \frac{k_{-1} + k_2}{k_1}$$

- ✦ Therefore the expression for  $[\text{ES}]$  becomes

$$[\text{ES}] = \frac{[\text{E}][\text{S}]}{K_M}$$

# Enzyme Kinetics



• Before this expression for [ES] can be substituted into the expression for  $v_o$ , the variable [E] needs to be eliminated.

- ✦ [E] is the free enzyme concentration, which is equal to the total enzyme concentration,  $[E]_T$ , minus the enzyme-substrate concentration, [ES].

$$[E] = [E]_T - [ES]$$

# Enzyme Kinetics

- ✦ Substitution of this expression for [E] into the one derived before for [ES] gives an expression for  $v_o$  as a function of [S]:

$$\begin{aligned}[ES] &= \frac{([E]_T - [ES])[S]}{K_M} \\ &= \frac{[E]_T[S] - [ES][S]}{K_M} \\ &= \frac{[E]_T[S]}{K_M} - \frac{[ES][S]}{K_M} \\ [ES] + \frac{[ES][S]}{K_M} &= \frac{[E]_T[S]}{K_M}\end{aligned}$$

$$\begin{aligned}[ES] \left( 1 + \frac{[S]}{K_M} \right) &= \frac{[E]_T[S]}{K_M} \\ [ES] \left( \frac{K_M + [S]}{K_M} \right) &= \frac{[E]_T[S]}{K_M} \\ [ES] &= \left( \frac{K_M}{K_M + [S]} \right) \frac{[E]_T[S]}{K_M} \\ [ES] &= \frac{[E]_T[S]}{K_M + [S]}\end{aligned}$$



# Enzyme Kinetics

- ✦ Substitution of this expression for [ES] into the one for  $v_o$  gives us the Michaelis-Menton equation:

$$v_o = k_2[ES]$$
$$v_o = \frac{k_2[E]_T[S]}{K_M + [S]}$$

- At very high substrate concentration ( $[S] \gg K_M$ ),

$$v_o = k_2[E]_T \quad (\text{as } [S] \text{ becomes large})$$

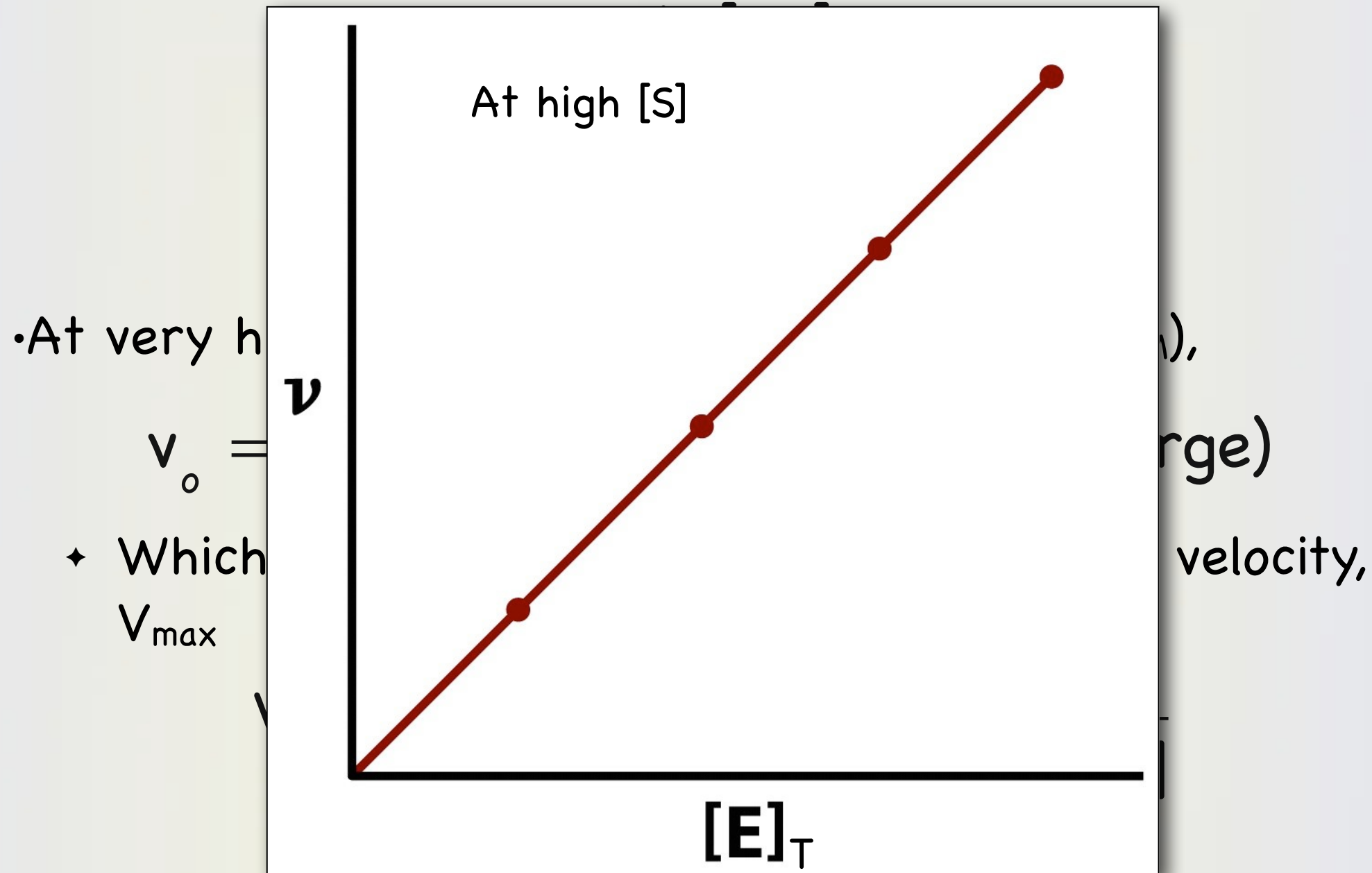
- ✦ Which is a constant equal to the maximum velocity,

$V_{\max}$

$$V_{\max} = k_2[E]_T, \quad v_o = \frac{V_{\max}[S]}{K_M + [S]}$$

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# Enzyme Kinetics

$k_{cat}$

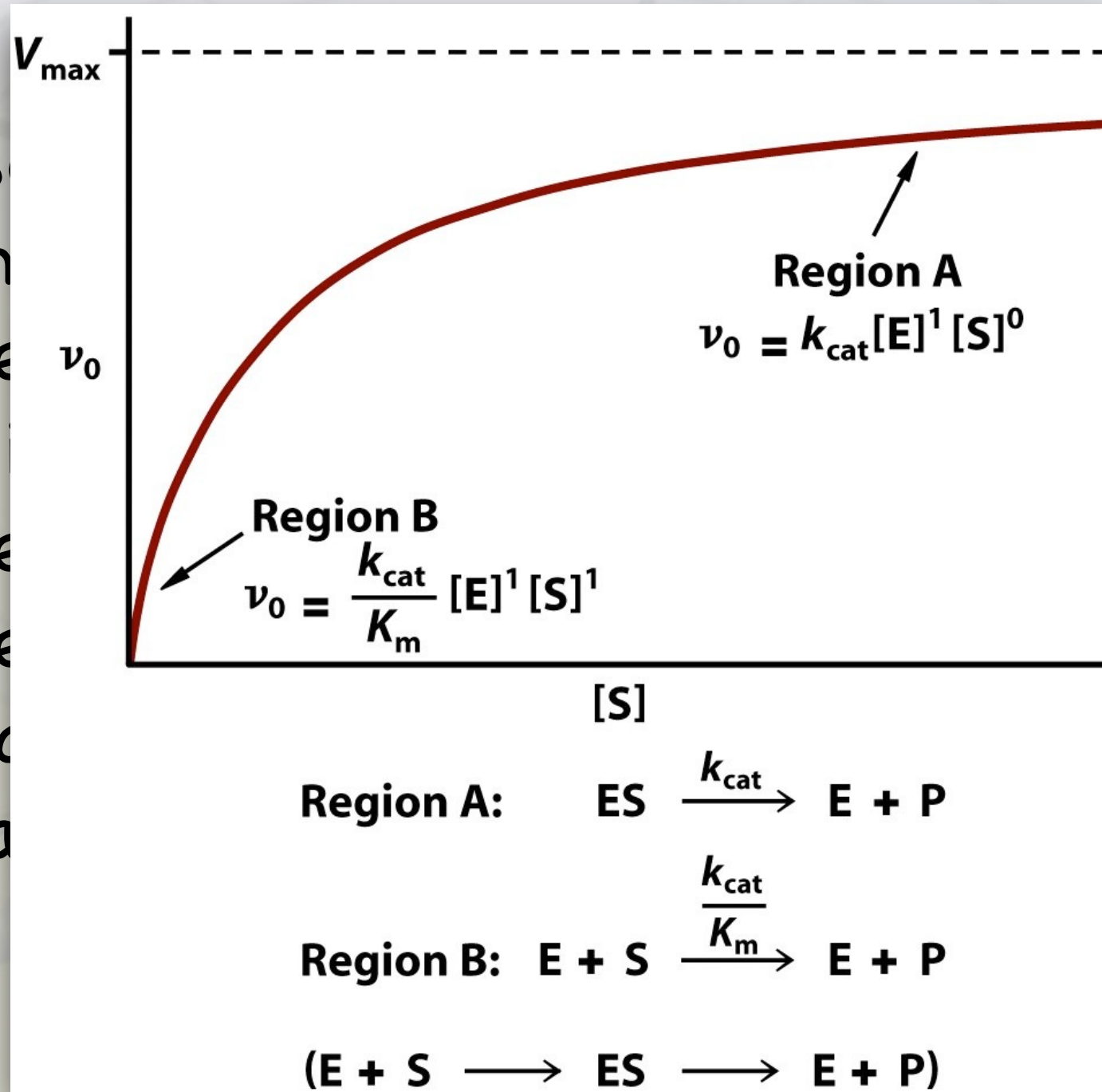
- ✦ Represented by the zero-order rate constant at high  $[S]$  ( $k_{cat} = k_2$ )
- ✦ It is determined from  $V_{max}$  ( $k_{cat} = V_{max}/[E]_T$ )
- ✦ Has units of frequency (1/sec, 1/min) and represents the number of catalytic cycles an enzyme can carry out per unit time when fully saturated with substrate.
- ✦ Also called the turnover number



# Enzyme Kinetics

$k_{cat}$

- ✦ Represents the rate of the reaction at high substrate concentrations
- ✦ It is determined by the catalytic rate constant ( $k_{cat}$ ) and the total enzyme concentration ( $[E]_T$ )
- ✦ Has units of  $\text{mol L}^{-1} \text{s}^{-1}$  and represents the maximum rate of the enzyme-catalyzed reaction when the enzyme is fully saturated with substrate
- ✦ Also called the turnover number



# Enzyme Kinetics

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**TABLE 5.1** Examples of catalytic constants

Enzyme	$k_{cat} (s^{-1})^*$
Papain	10
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Carboxypeptidase	$10^2$
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Dehydrogenases	$10^3$
Transaminases	$10^3$
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\*The catalytic constants are given only as orders of magnitude.

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# Enzyme Kinetics

$K_M$

- ✦ When  $k_2 \ll k_{-1}$ ,  $K_M$  is equal to the dissociation constant for the enzyme-substrate complex



- Small  $K_M$  indicates strong binding of the substrate to enzyme
- Large  $K_M$  indicate weak binding of substrate to enzyme.



# Enzyme Kinetics

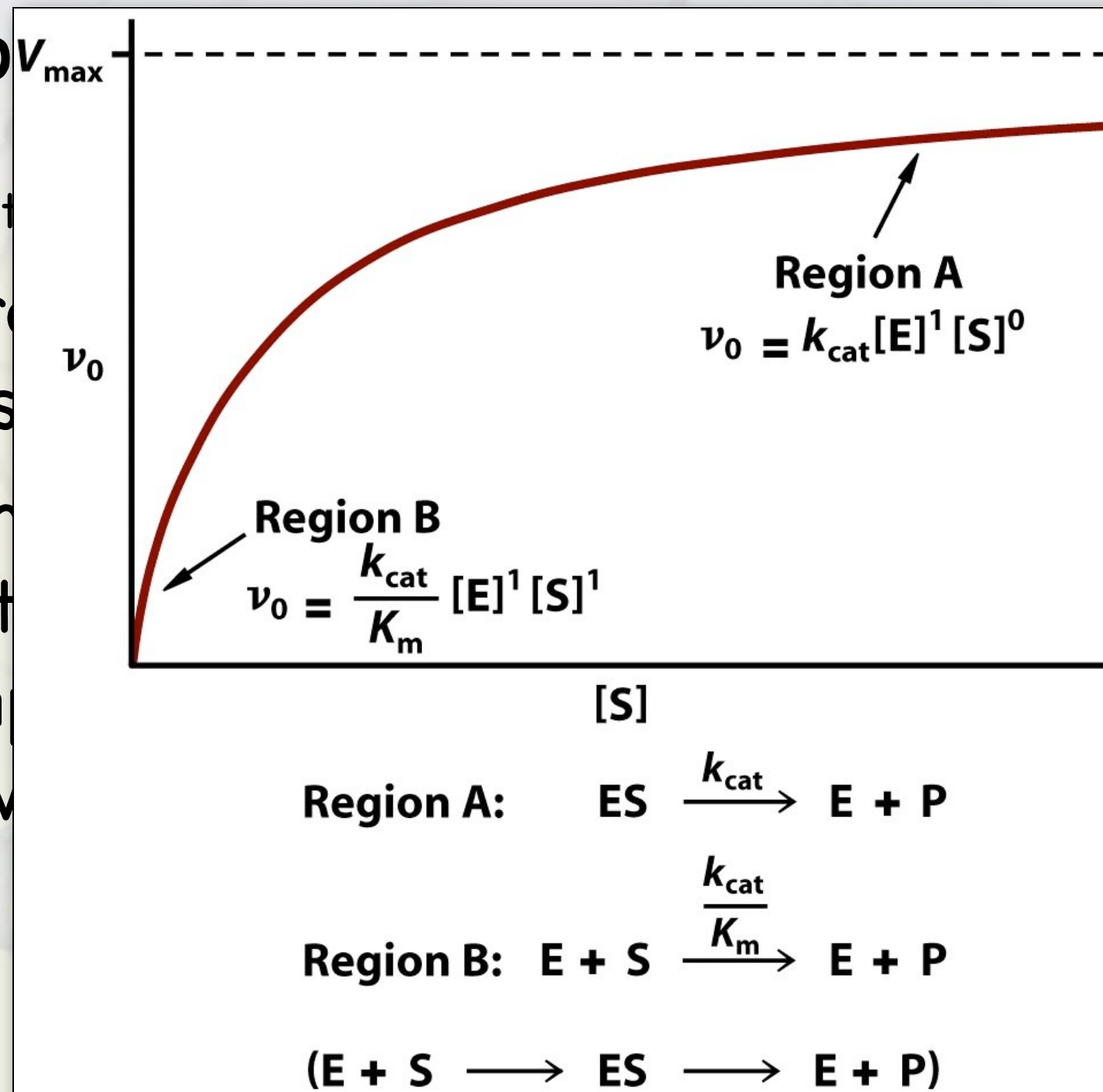
- Combining  $k_{\text{cat}}$  and  $K_M$

- ✦  $k_{\text{cat}}/K_M$  is called the **catalytic efficiency**.
- ✦ It represents the second order rate constant at low  $[S]$
- ✦ Higher values of  $k_{\text{cat}}/K_M$  indicate an enzyme that is both good at forming the ES complex, and then once formed, good at converting the bound substrate to product.

# Enzyme Kinetics

## • Combined

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# Enzyme Kinetics

$k_{\text{cat}}/K_M$  – catalytic efficiency

- ✦ It is used to assess **catalytic perfection**
  - When  $k_{\text{cat}}/K_M > 10^8 \text{ s}^{-1}\text{M}^{-1}$  it says that the reaction is diffusion-rate limited
  - This means that there are no changes that can be made to the enzyme to make the reaction go any faster.

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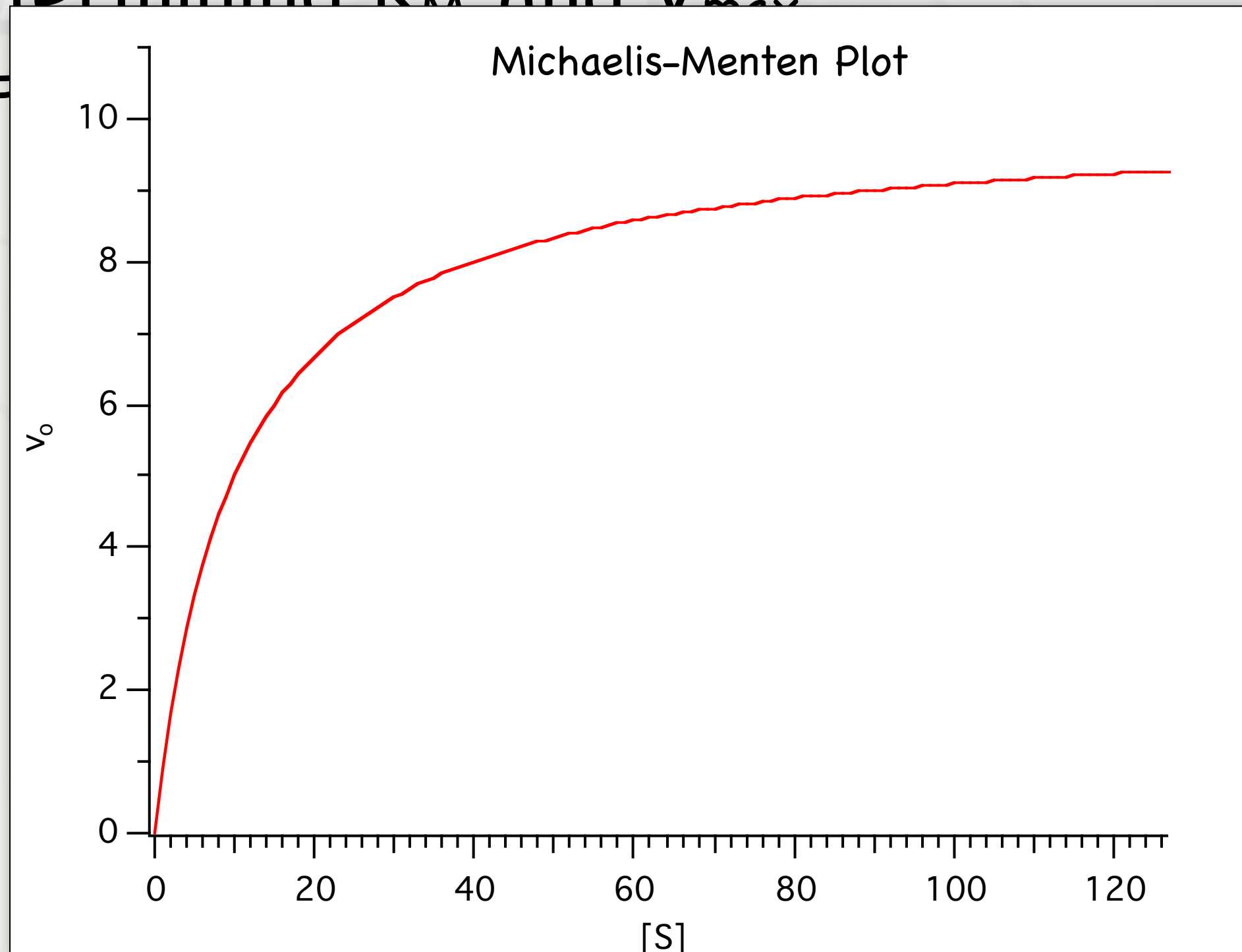
# Enzyme Kinetics

- Determining  $K_M$  and  $V_{max}$ .
  - ✦ From the  $v_o$  versus  $[S]$  plot
    - $V_{max}$  is the maximum  $v_o$  at high  $[S]$
    - $K_M$  is the  $[S]$  value when  $v_o$  is at the half maximum,  $v_o = V_{max}/2$

# Enzyme Kinetics

- Determining  $K_M$  and  $V_{max}$

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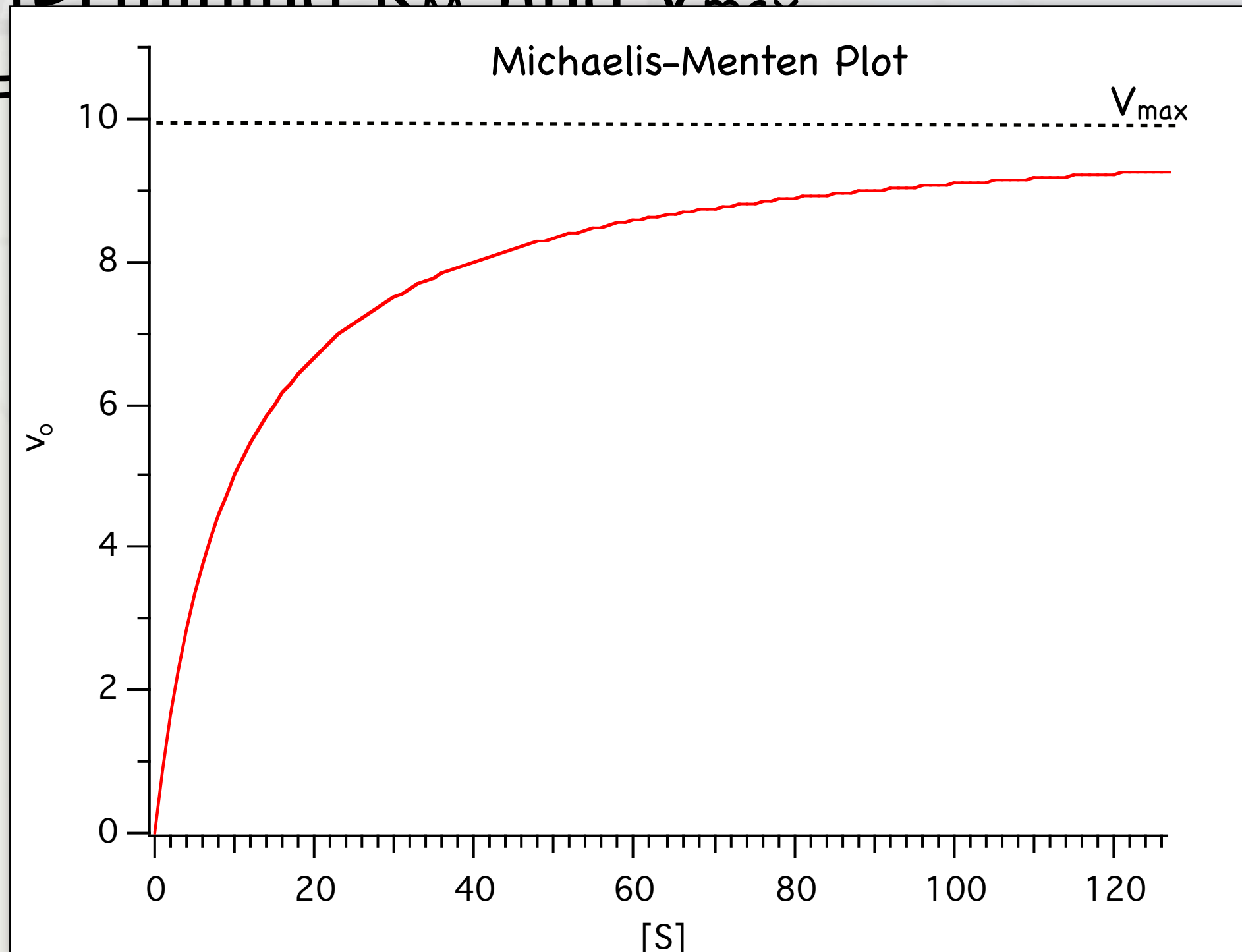




# Enzyme Kinetics

- Determining  $K_M$  and  $V_{max}$

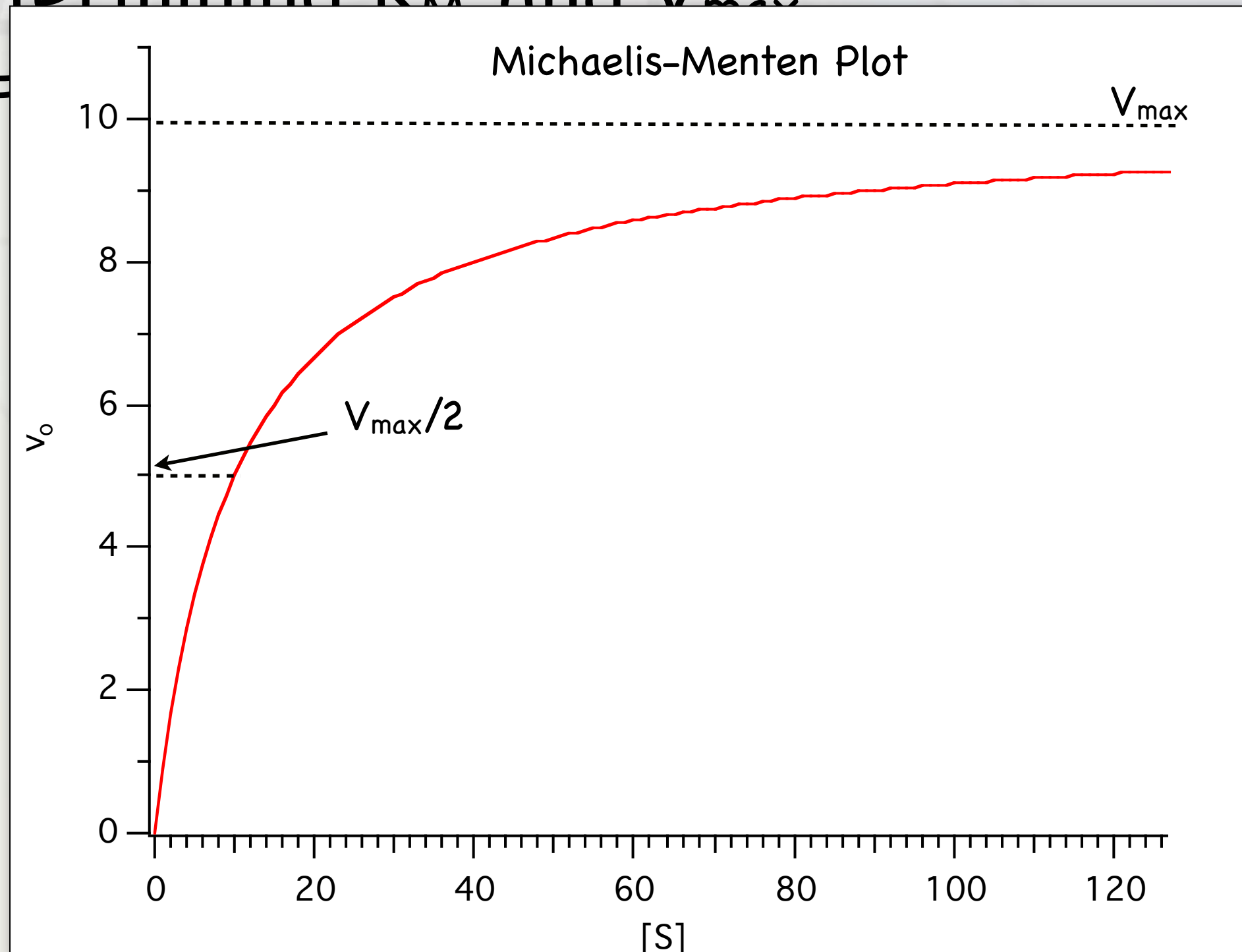
♦  $F$



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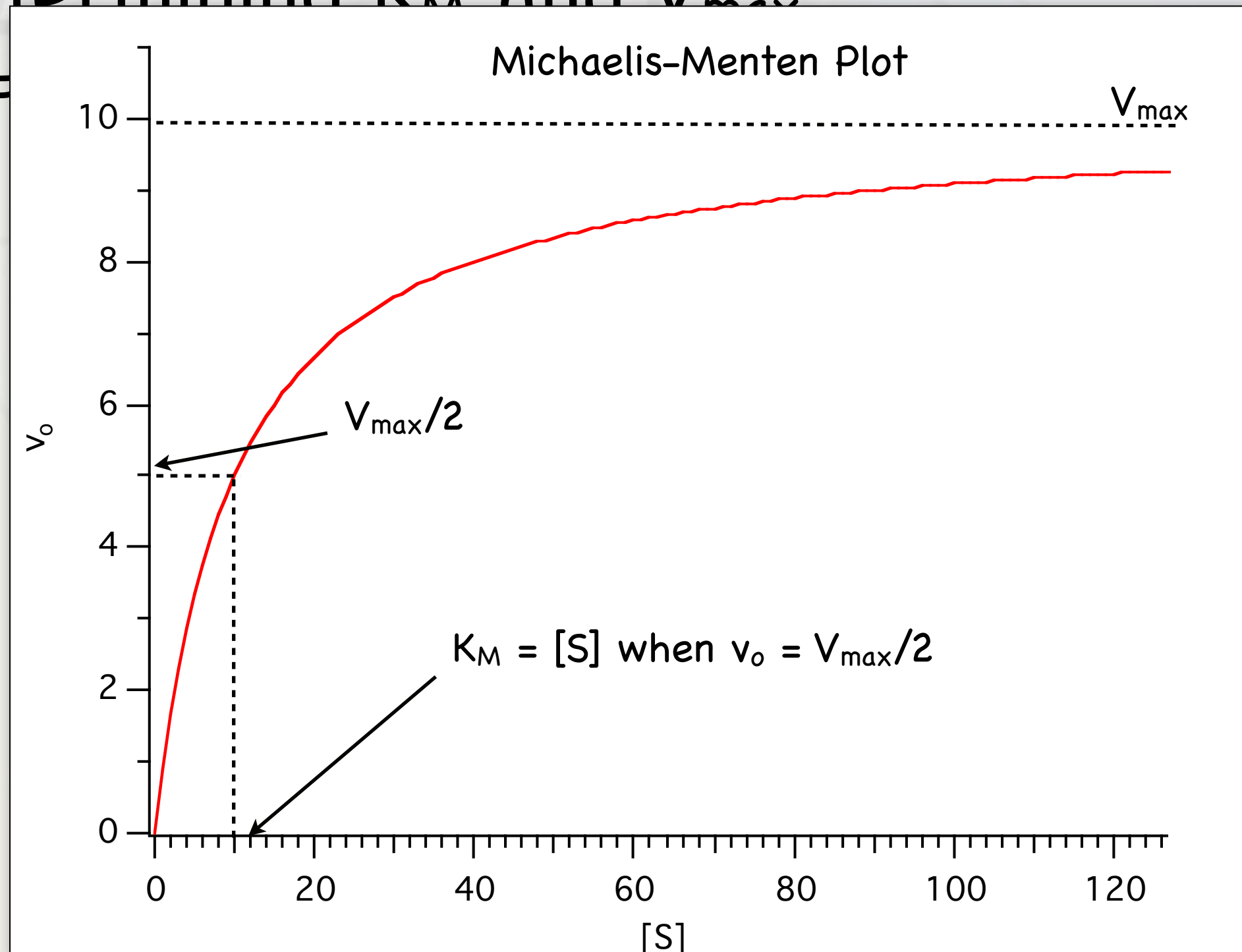
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# Enzyme Kinetics

- Determining  $K_M$  and  $V_{max}$

♦  $F$



# Enzyme Kinetics

## Problem:

Initial velocities have been measured for the reaction of  $\alpha$ -chymotrypsin with tyrosine benzyl ester [S] at six different substrate concentration. Use the data below to make a reasonable estimate of the  $V_{\max}$  and  $K_M$  for this substrate.

[S] {mM}	$v_o$ {mM/min}
0.008	40
0.01	45
0.04	75
0.1	87
2	90
10	95

# Enzyme Kinetics

## •Determining $K_M$ and $V_{max}$ .

- ✦ From the double-reciprocal plot (Lineweaver-Burk plot)

$$\frac{1}{v_o} = \frac{K_M + [S]}{V_{max} [S]}$$

- ✦ Taking the reciprocal of the Michaelis-Menten equation and plotting  $1/v_o$  versus  $1/[S]$  produces a straight line

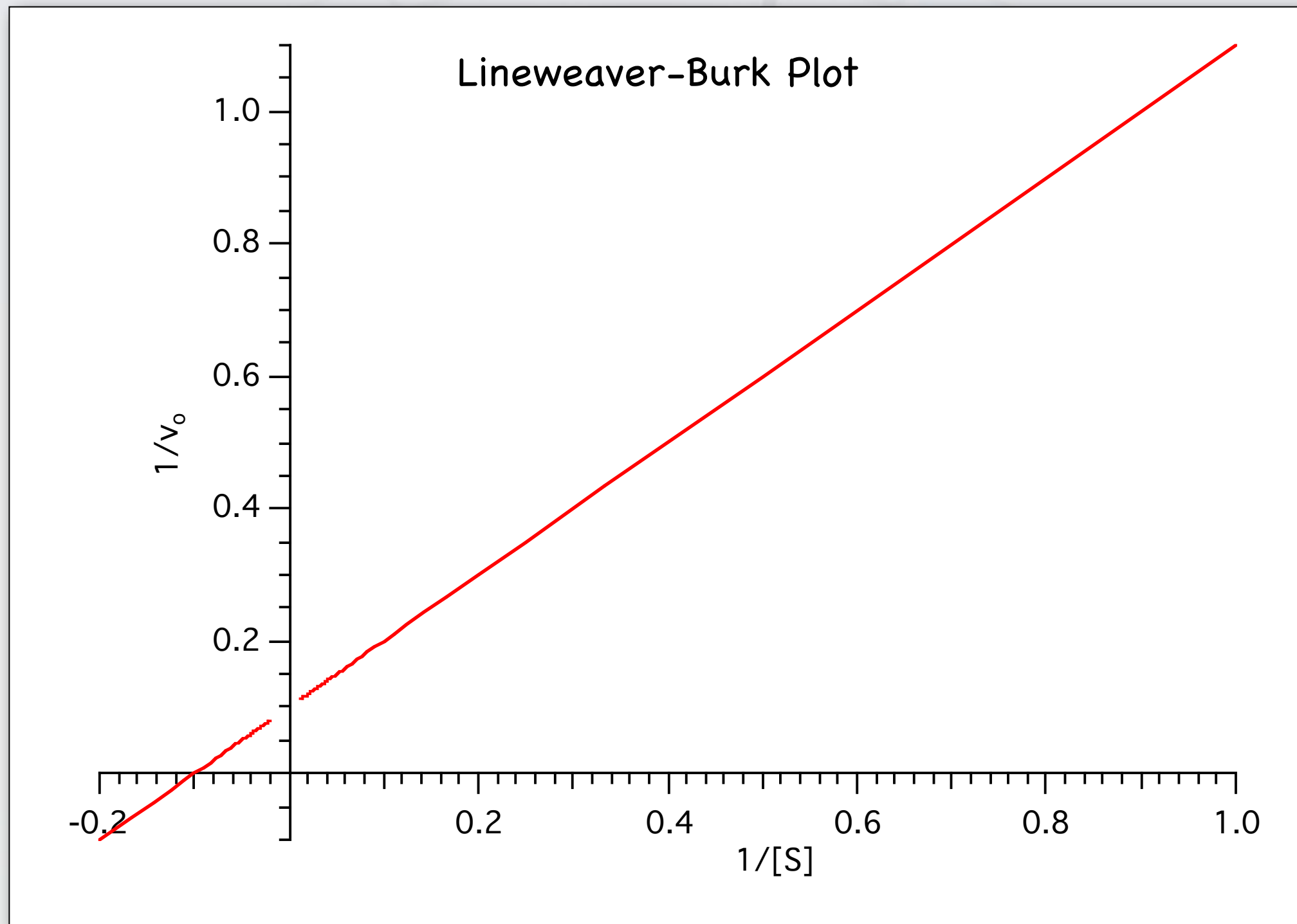
$$= \frac{K_M}{V_{max} [S]} + \frac{[S]}{V_{max} [S]}$$

$$\frac{1}{v_o} = \frac{K_M}{V_{max}} \left( \frac{1}{[S]} \right) + \frac{1}{V_{max}}$$

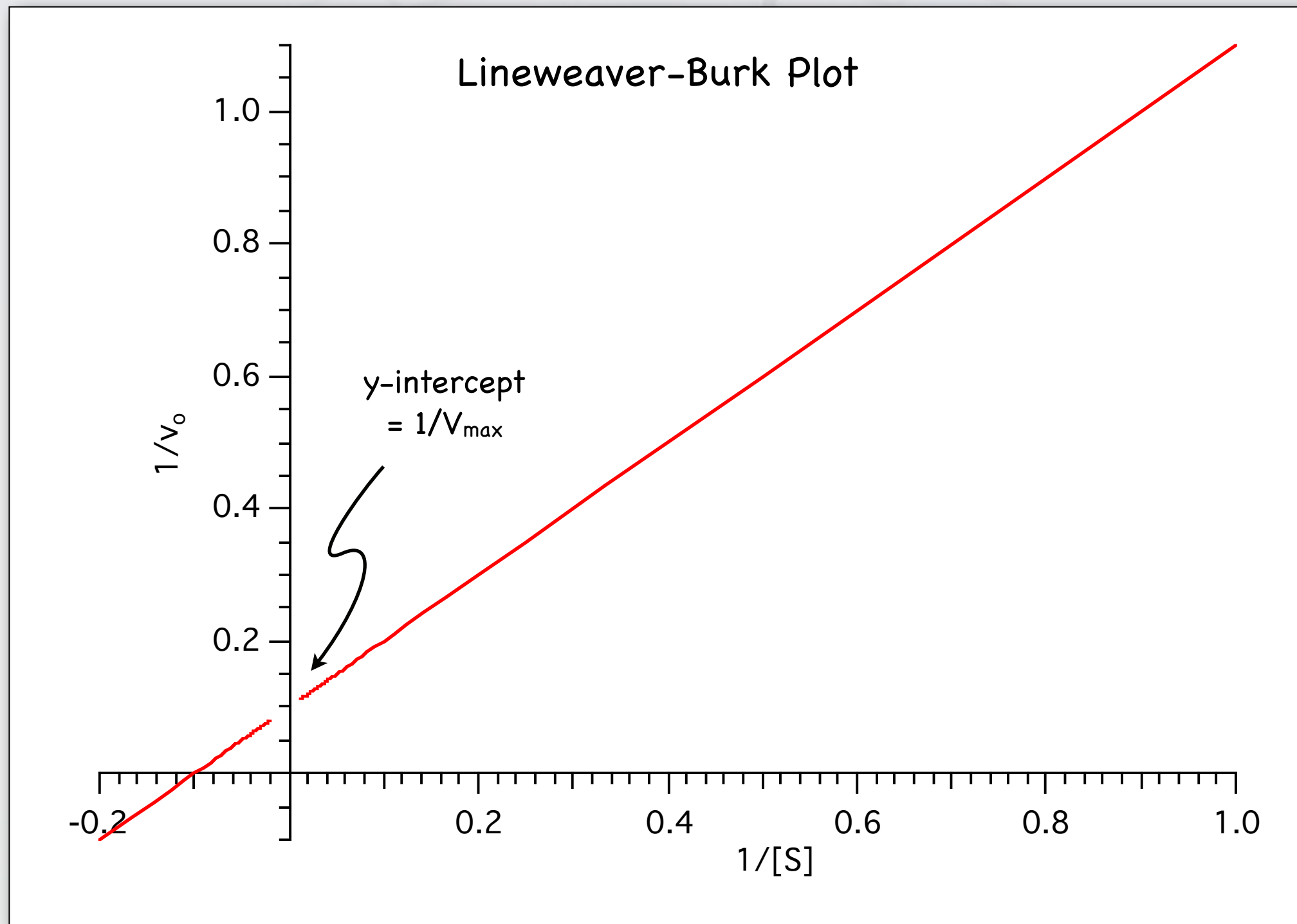
$$y = m \bullet x + b$$



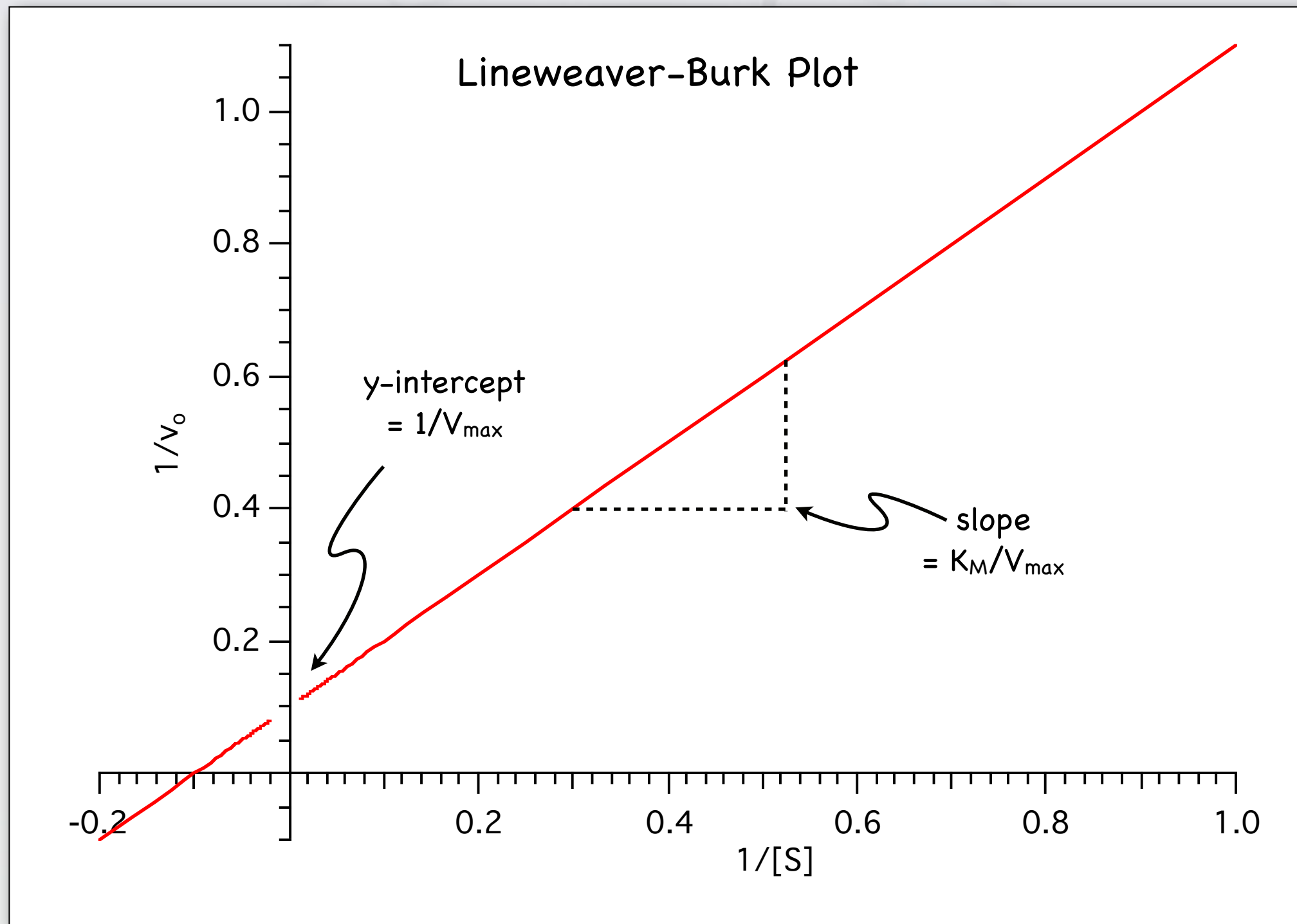
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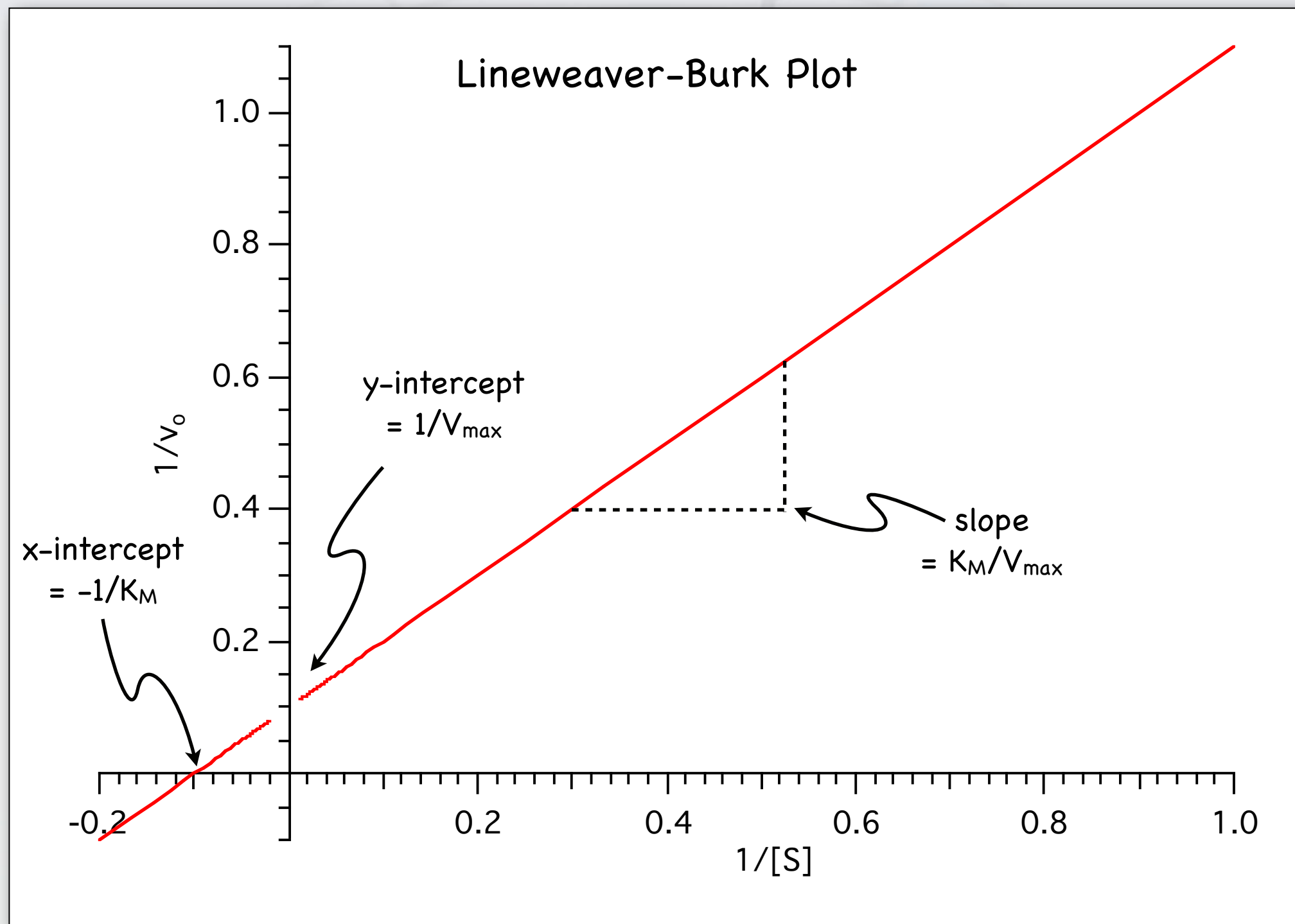
# Enzyme Kinetics



# Enzyme Kinetics



# Enzyme Kinetics



# Enzyme Kinetics

## Summary:

$$V_{\max}$$

- ✦ It is the velocity observed when an enzyme is fully saturated with substrate at high [S]
- ✦ Is the maximum velocity in the Michaelis-Menten plot.
- ✦ It can be used to determine  $k_{\text{cat}}$ .
- ✦ It can be determined from the y-intercept in a Lineweaver-Burk plot (y-intercept =  $1/V_{\max}$ ).



# Enzyme Kinetics

## Summary:

$$K_M$$

- ✦ It is a measure of how strongly an enzyme is able to bind to the substrate.
- ✦ It is equal to the substrate concentration that produces a half-maximum velocity ( $v_o = V_{\max}/2$ ) in the Michaelis-Menten plot.
- ✦ It can be determined from either the slope/y-intercept, or from the x-intercept of a Lineweaver-Burk plot (x-intercept =  $-1/K_M$ ).

# Enzyme Kinetics

## Summary:

$$k_{\text{cat}}$$

- ✦ It is the catalytic rate constant ( $k_2$ ).
- ✦ It is also called the **turnover number** and tells how often each enzyme molecule converts a substrate to product per unit of time.
- ✦ It can be determined from  $V_{\text{max}}$  and the total enzyme concentration  $[E]_{\text{T}}$ ,  
( $k_{\text{cat}} = V_{\text{max}}/[E]_{\text{T}}$ ).

# Enzyme Kinetics

## Summary:

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## Summary:

$$k_{\text{cat}}/K_M$$

- ✦ It is a measure of the catalytic efficiency for an enzyme and incorporates both how readily an enzyme binds its substrate to form the enzyme-substrate complex ( $1/K_M$ ), and once formed, how readily it converts it to product ( $k_{\text{cat}}$ ).
- ✦ It is used to assess **catalytic perfection**
  - $k_{\text{cat}}/K_M > 10^8 \text{ s}^{-1}\text{M}^{-1}$  (The theoretical, diffusion rate limit.)



# Enzyme Kinetics

## Summary:

- ♦ It is a measure of an enzyme's catalytic efficiency for a particular substrate, readily compared to the rate of the uncatalyzed reaction.
- ♦ It is calculated as the ratio of the catalytic rate constant ( $k_{cat}$ ) to the Michaelis constant ( $K_m$ ).

**TABLE 5.2** Catalytic efficiencies of some enzymes

	<b>Enzymatic rate constant (<math>k_{cat}/K_m</math> in <math>M^{-1}s^{-1}</math>)</b>
Carbonic anhydrase	$7 \times 10^6$
Chymotrypsin	$9 \times 10^7$
Chorismate mutase	$2 \times 10^6$
Triose phosphate isomerase	$4 \times 10^8$
Cytidine deaminase	$3 \times 10^6$
Adenosine deaminase	$10^7$
Mandelate racemase	$10^6$
$\beta$ -Amylase	$10^7$
Fumarase	$10^9$
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Alkaline phosphatase	$3 \times 10^7$
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# Enzyme Kinetics

## Summary:

$$(k_{\text{cat}}/K_M)/k_n$$

- ✦ Is called the **catalytic proficiency** and is a measure of how much an enzyme increases the rate of a reaction over its non-catalyzed rate ( $k_n$ ).

# Enzyme Kinetics

## Summary:

**TABLE 5.2** Catalytic proficiencies of some enzymes

	<b>Nonenzymatic rate constant (<math>k_n</math> in <math>s^{-1}</math>)</b>	<b>Enzymatic rate constant (<math>k_{cat}/K_m</math> in <math>M^{-1}s^{-1}</math>)</b>	<b>Catalytic proficiency</b>
Carbonic anhydrase	$10^{-1}$	$7 \times 10^6$	$7 \times 10^7$
Chymotrypsin	$4 \times 10^{-9}$	$9 \times 10^7$	$2 \times 10^{16}$
Chorismate mutase	$10^{-5}$	$2 \times 10^6$	$2 \times 10^{11}$
Triose phosphate isomerase	$4 \times 10^{-6}$	$4 \times 10^8$	$10^{14}$
Cytidine deaminase	$10^{-10}$	$3 \times 10^6$	$3 \times 10^{16}$
Adenosine deaminase	$2 \times 10^{-10}$	$10^7$	$5 \times 10^{16}$
Mandelate racemase	$3 \times 10^{-13}$	$10^6$	$3 \times 10^{18}$
$\beta$ -Amylase	$7 \times 10^{-14}$	$10^7$	$10^{20}$
Fumarase	$10^{-13}$	$10^9$	$10^{21}$
Arginine decarboxylase	$9 \times 10^{-16}$	$10^6$	$10^{21}$
Alkaline phosphatase	$10^{-15}$	$3 \times 10^7$	$3 \times 10^{22}$
Orotidine 5'-phosphate decarboxylase	$3 \times 10^{-16}$	$6 \times 10^7$	$2 \times 10^{23}$

# Enzyme Kinetics

## Summary:

$$(k_{\text{cat}}/K_M)/k_n$$

- ✦ Is called the **catalytic proficiency** and is a measure of how much an enzyme increases the rate of a reaction over its non-catalyzed rate ( $k_n$ ).



# Enzyme Kinetics

## Problem:

Initial velocities have been measured for the reaction of  $\alpha$ -chymotrypsin with tyrosine benzyl ester [S] at six different substrate concentration. Use the data below to make a reasonable estimate of the  $V_{\max}$  and  $K_M$  for this substrate.

[S] {mM}	$v_o$ {mM/min}
0.008	40
0.01	45
0.04	75
0.1	87
2	90
10	95

# Enzyme Kinetics

## Problem:

Given the enzyme concentration used in this experiment was  $72\mu\text{M}$ ,

- A. What is the turnover number for chymotrypsin when it is fully saturated with the substrate?
- B. Is chymotrypsin, under the conditions used in this experiment, displaying catalytic perfection?

# Enzyme Kinetics

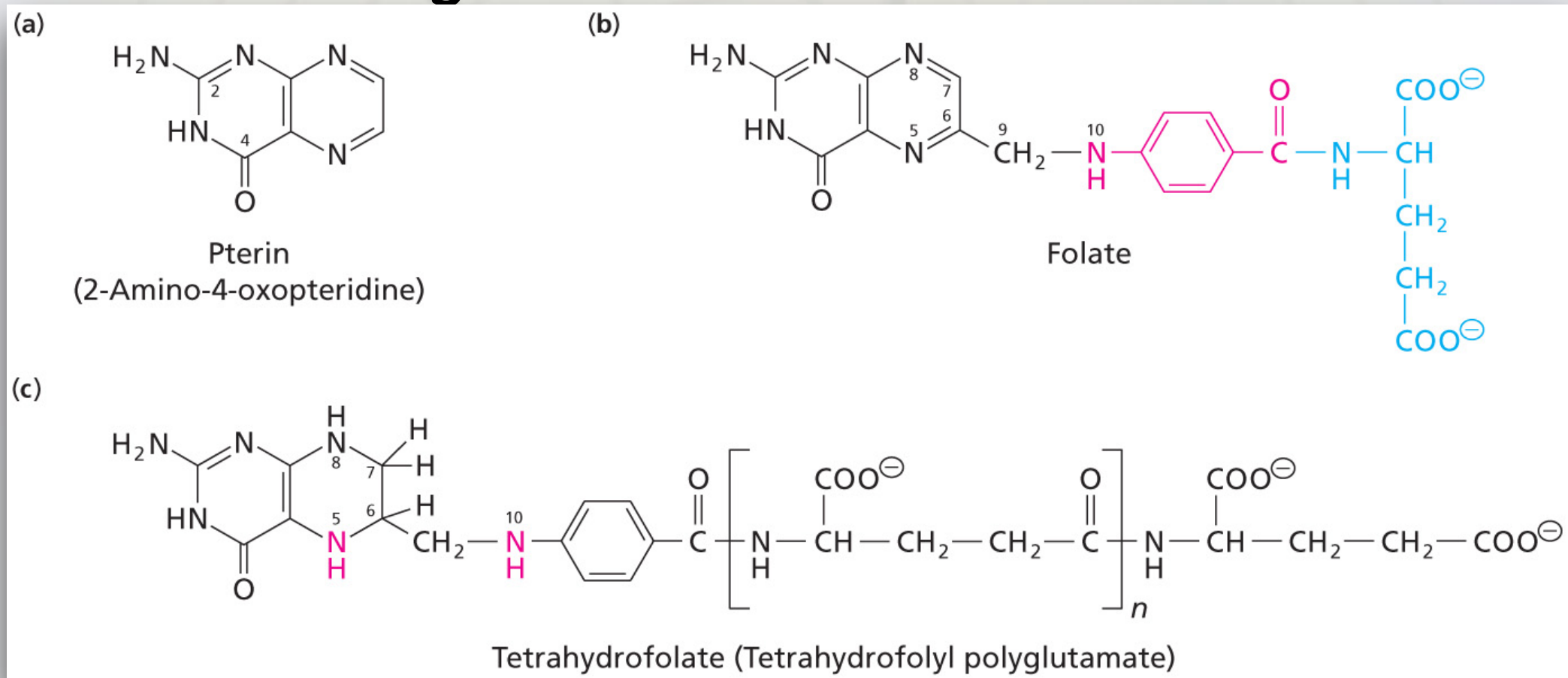
## Enzyme Inhibition

- ✦ The binding of small molecules can inhibit enzyme activity
  - Metabolites
    - ✦ Can be part of normal metabolic regulation.
    - ✦ Allosteric inhibition
  - Drugs
  - Toxins
- ✦ Covalent modification of the enzyme
  - Inhibition can reversible or irreversible

# Enzyme Kinetics

## Enzyme Inhibition

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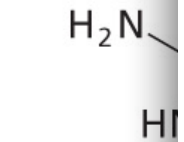
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# Enzyme Kinetics

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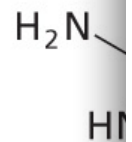
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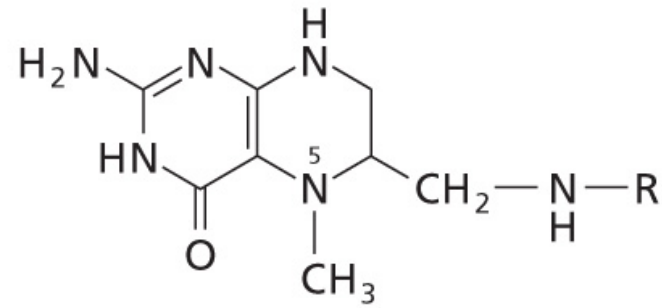
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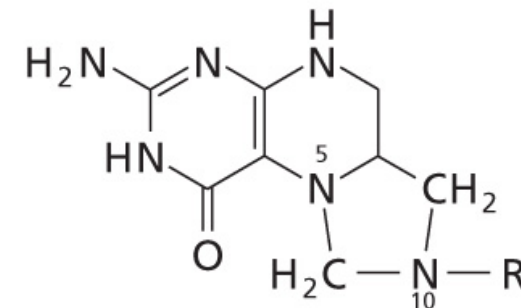


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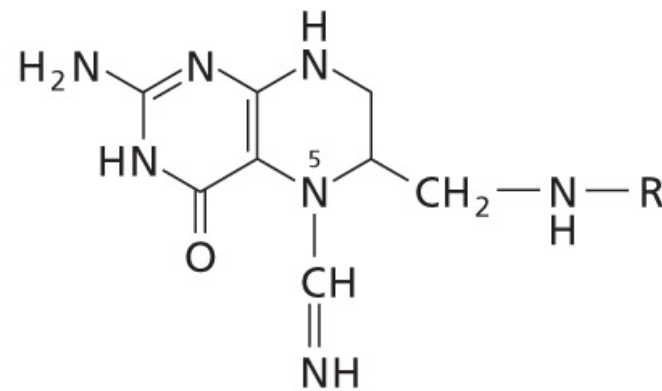
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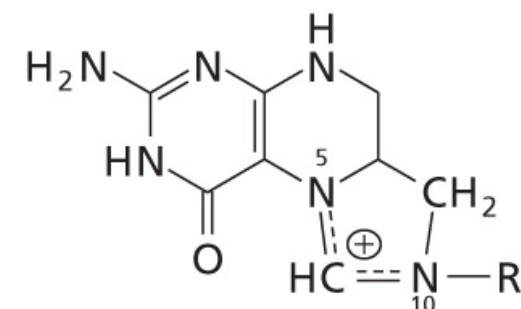
5-Methyltetrahydrofolate



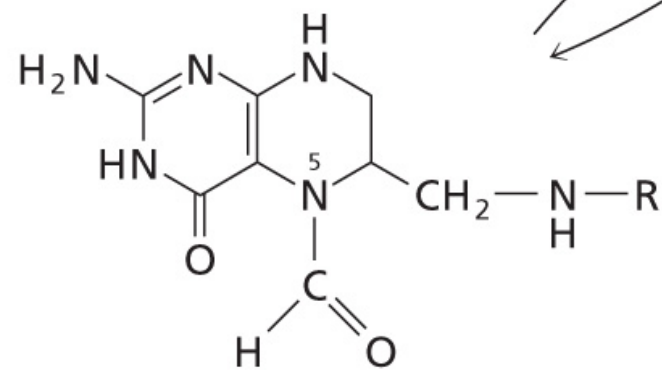
5,10-Methylenetetrahydrofolate



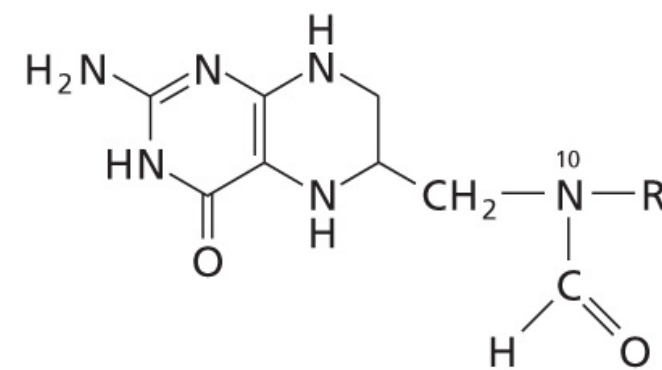
5-Formiminotetrahydrofolate



5,10-Methenyltetrahydrofolate

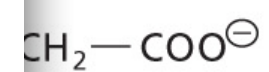


5-Formyltetrahydrofolate



10-Formyltetrahydrofolate

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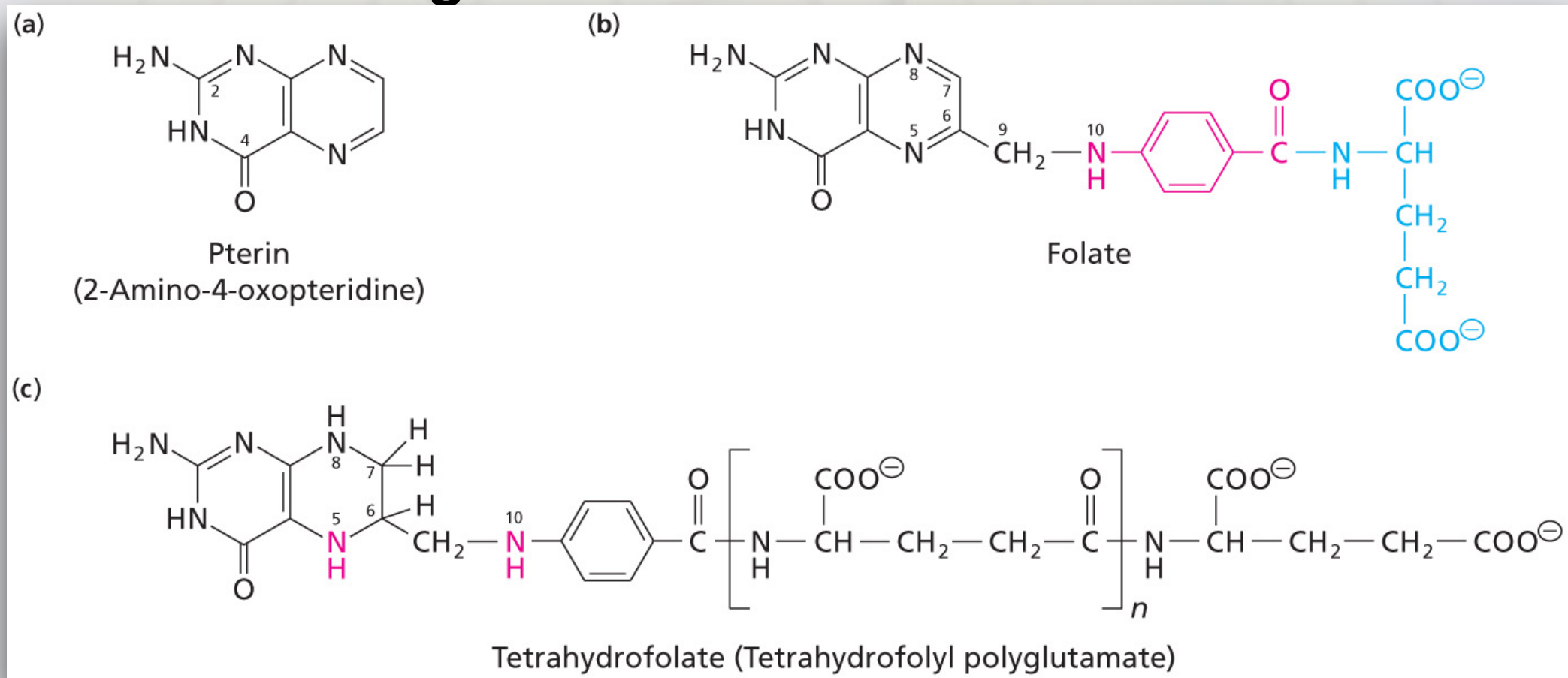
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## Enzyme Inhibition

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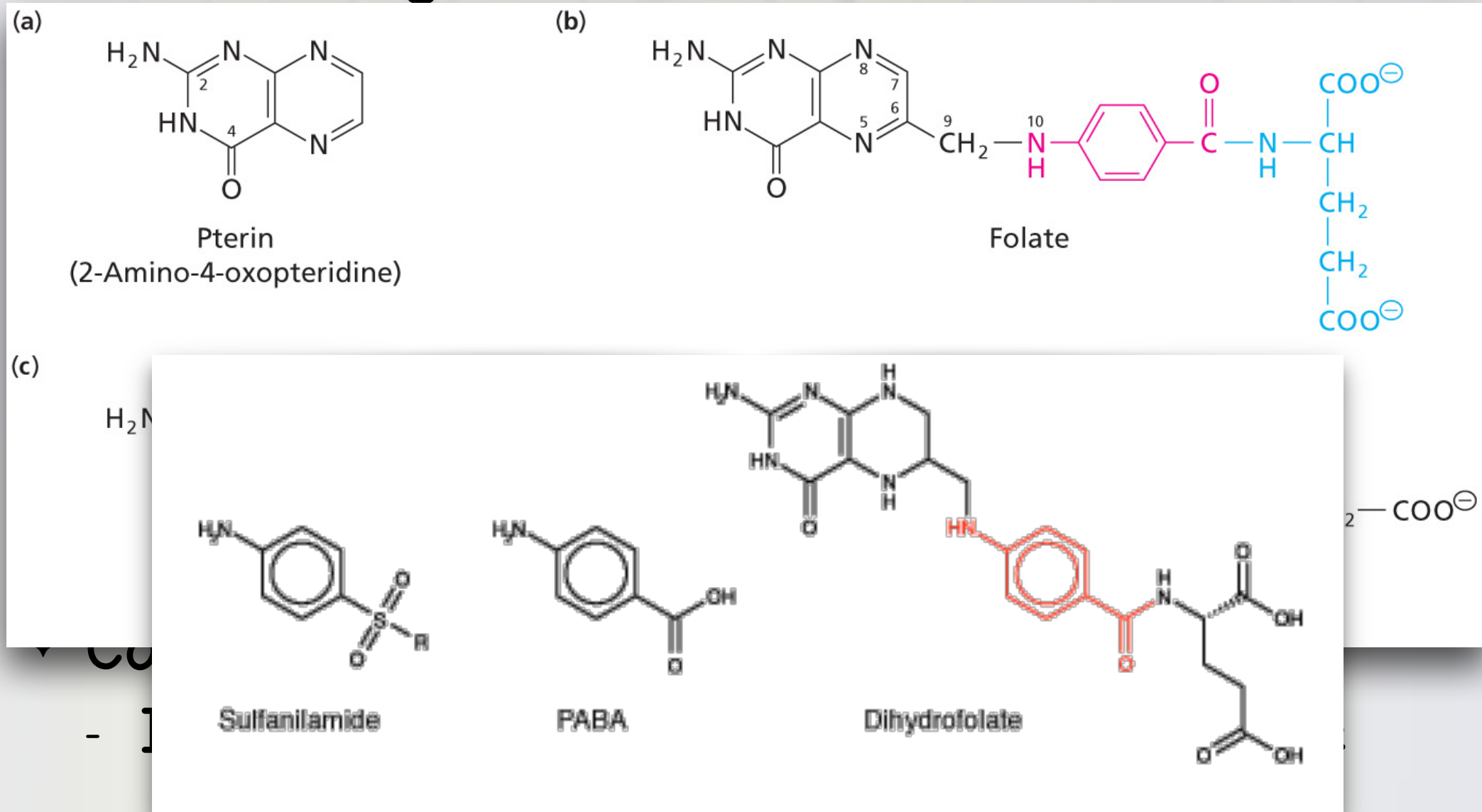


- Inhibition can reversible or irreversible

# Enzyme Kinetics

## Enzyme Inhibition

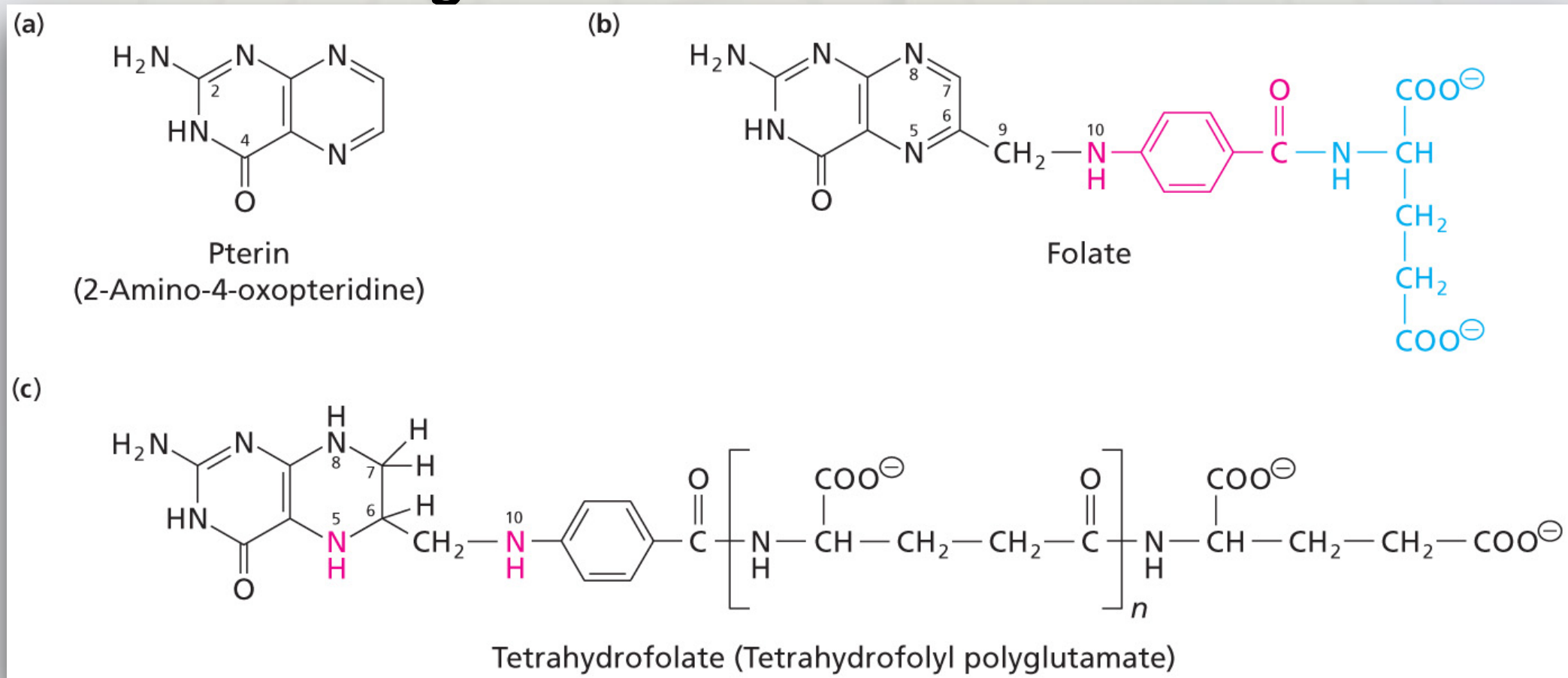
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# Enzyme Kinetics

## Enzyme Inhibition

- ♦ The binding of small molecules can inhibit



- Inhibition can reversible or irreversible

# Enzyme Kinetics

## Enzyme Inhibition

- ✦ The binding of small molecules can inhibit enzyme activity
  - Metabolites
    - ✦ Can be part of normal metabolic regulation.
    - ✦ Allosteric inhibition
  - Drugs
  - Toxins
- ✦ Covalent modification of the enzyme
  - Inhibition can reversible or irreversible

# Enzyme Kinetics

## •Reversible Enzyme Inhibition

- ✦ Competitive inhibition
- ✦ Uncompetitive inhibition
- ✦ Noncompetitive inhibition



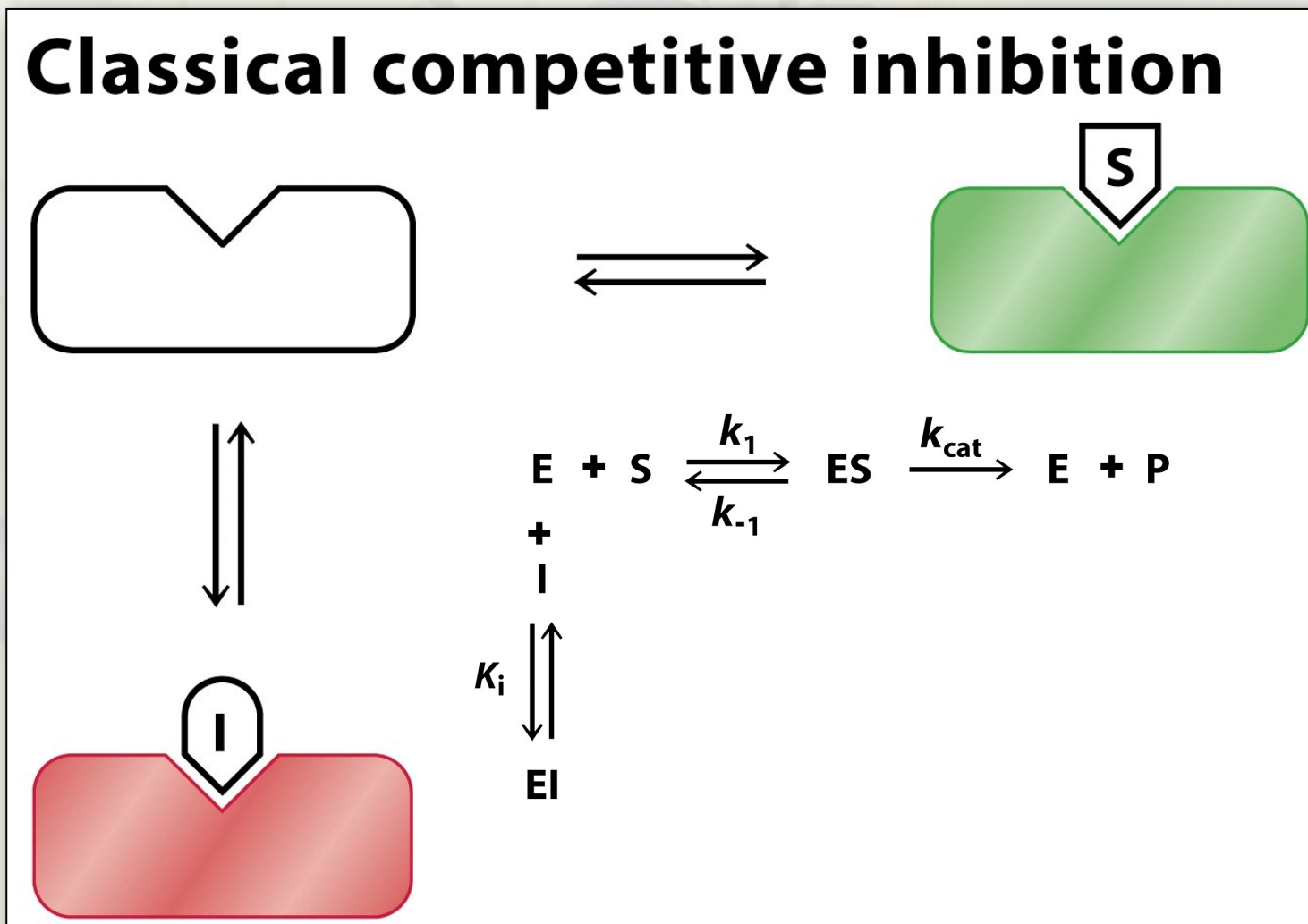
$$K_i = K_d = \frac{[E][I]}{[EI]} \quad \text{or} \quad \frac{[ES][I]}{[ESI]}$$



# Enzyme Kinetics

- Reversible Enzyme Inhibition

- ✦ Competitive inhibition
  - Mode used in drug design.

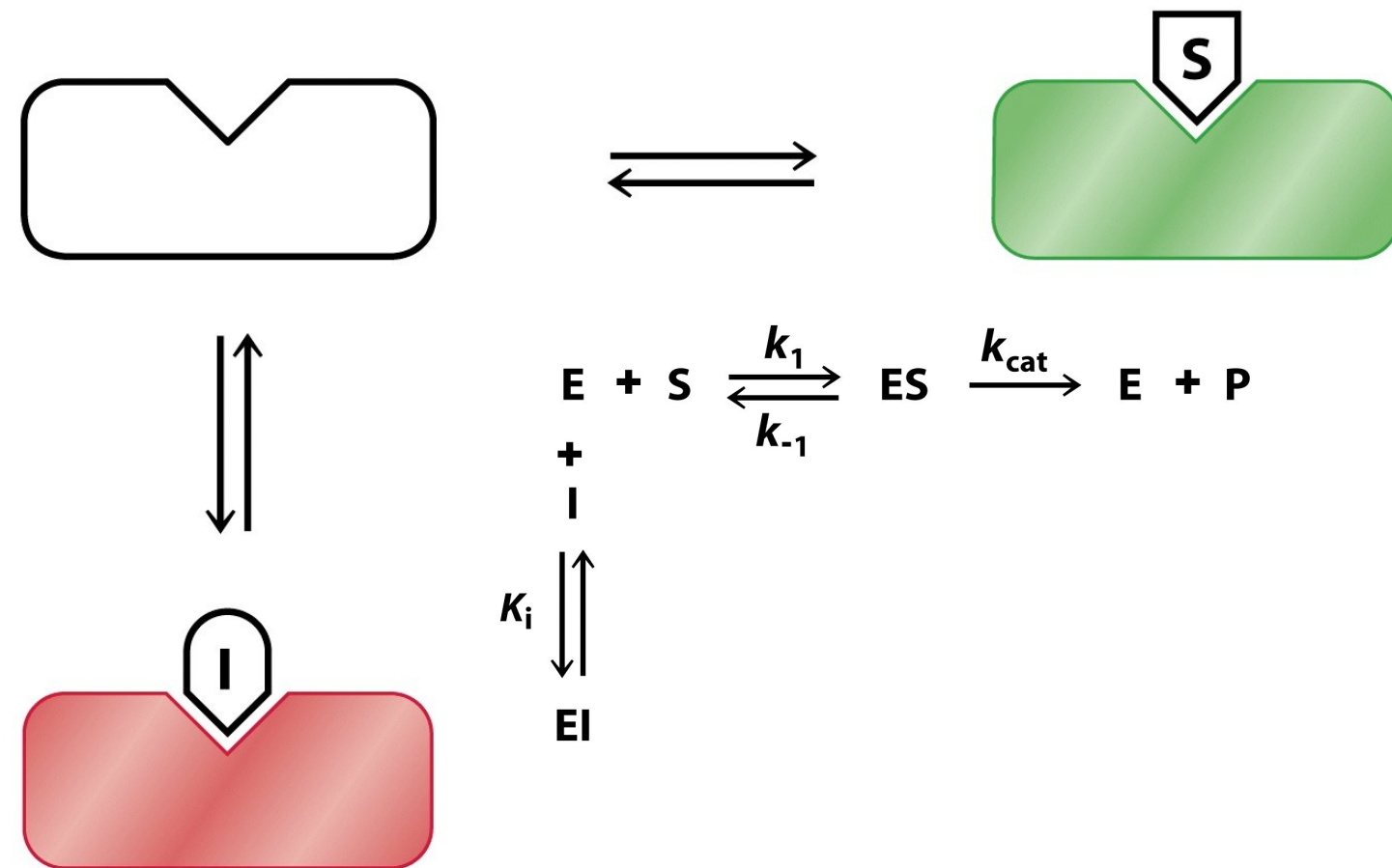


# Enzyme Kinetics

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### Classical competitive inhibition

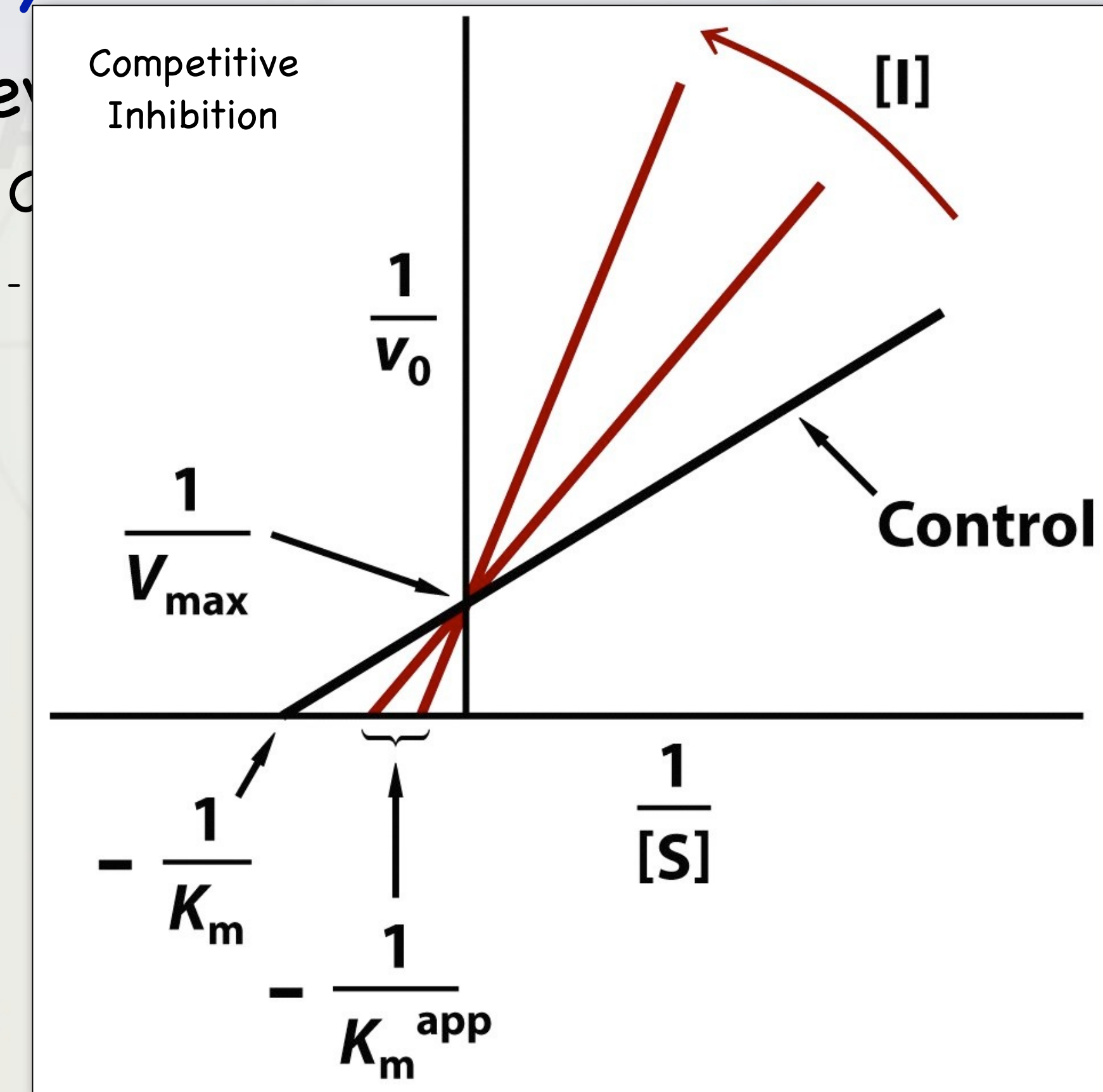


Inhibitor binds to the same site on the enzyme as the substrate

# Enzyme Kinetics

• Review

• Competitive Inhibition



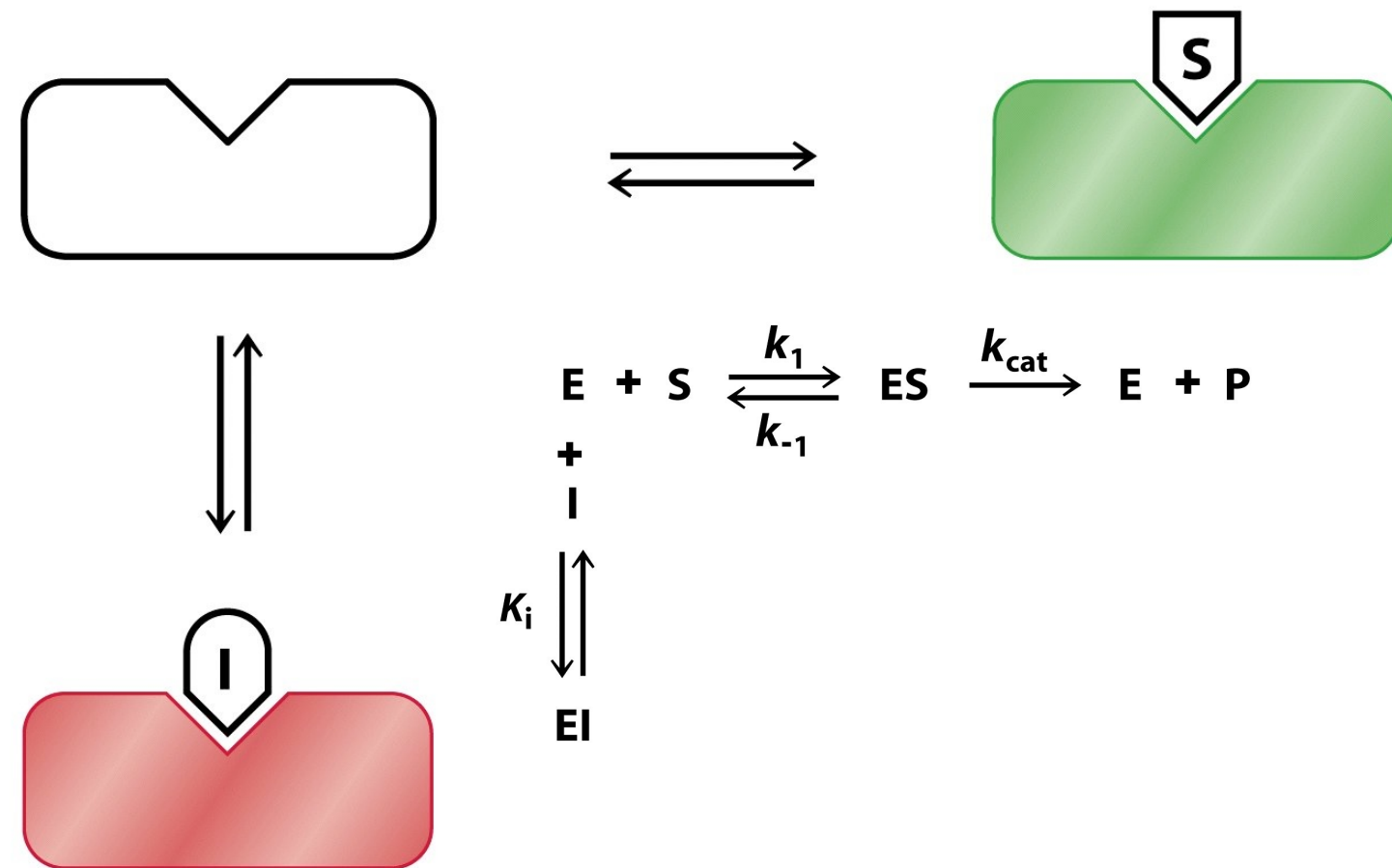
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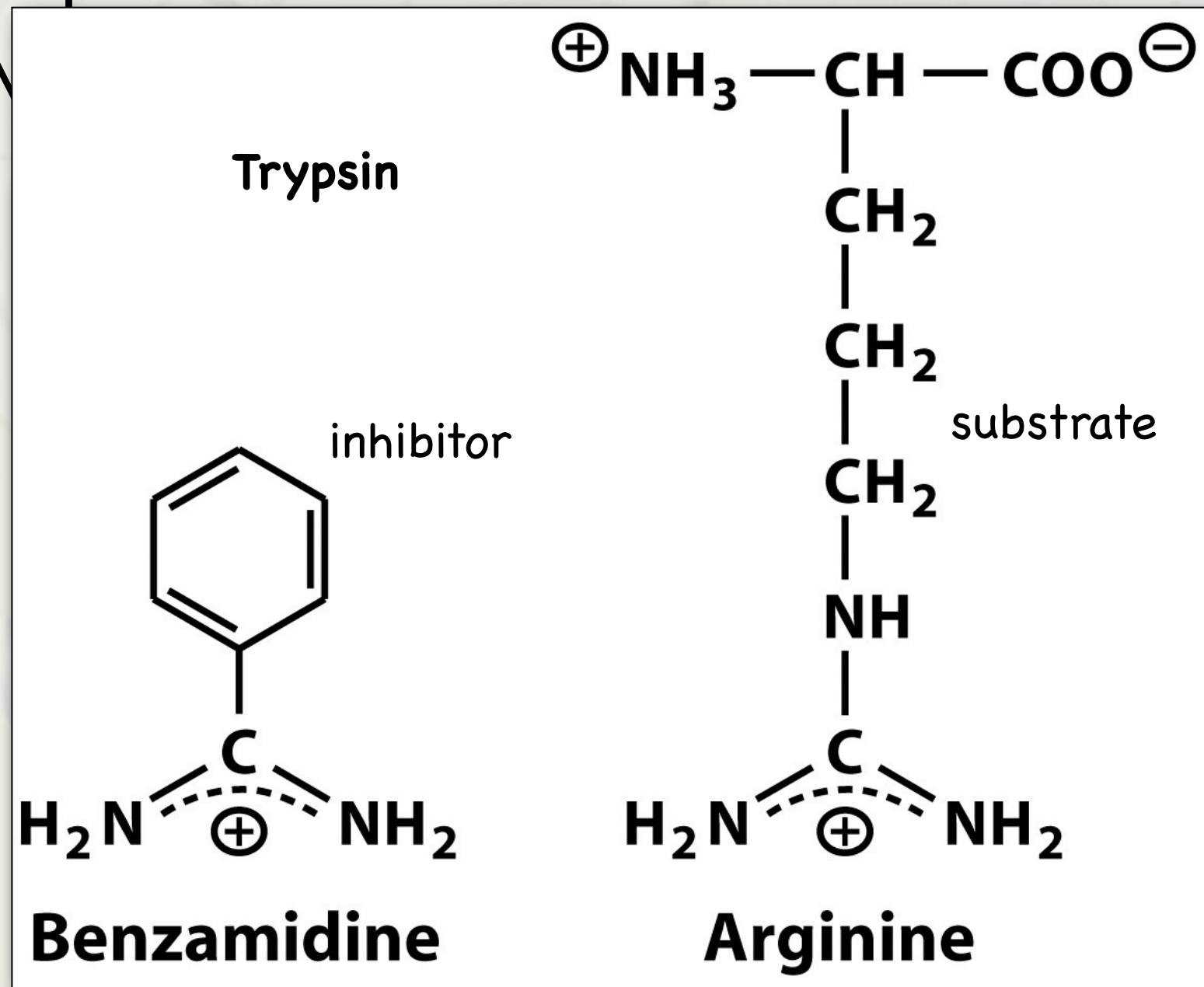


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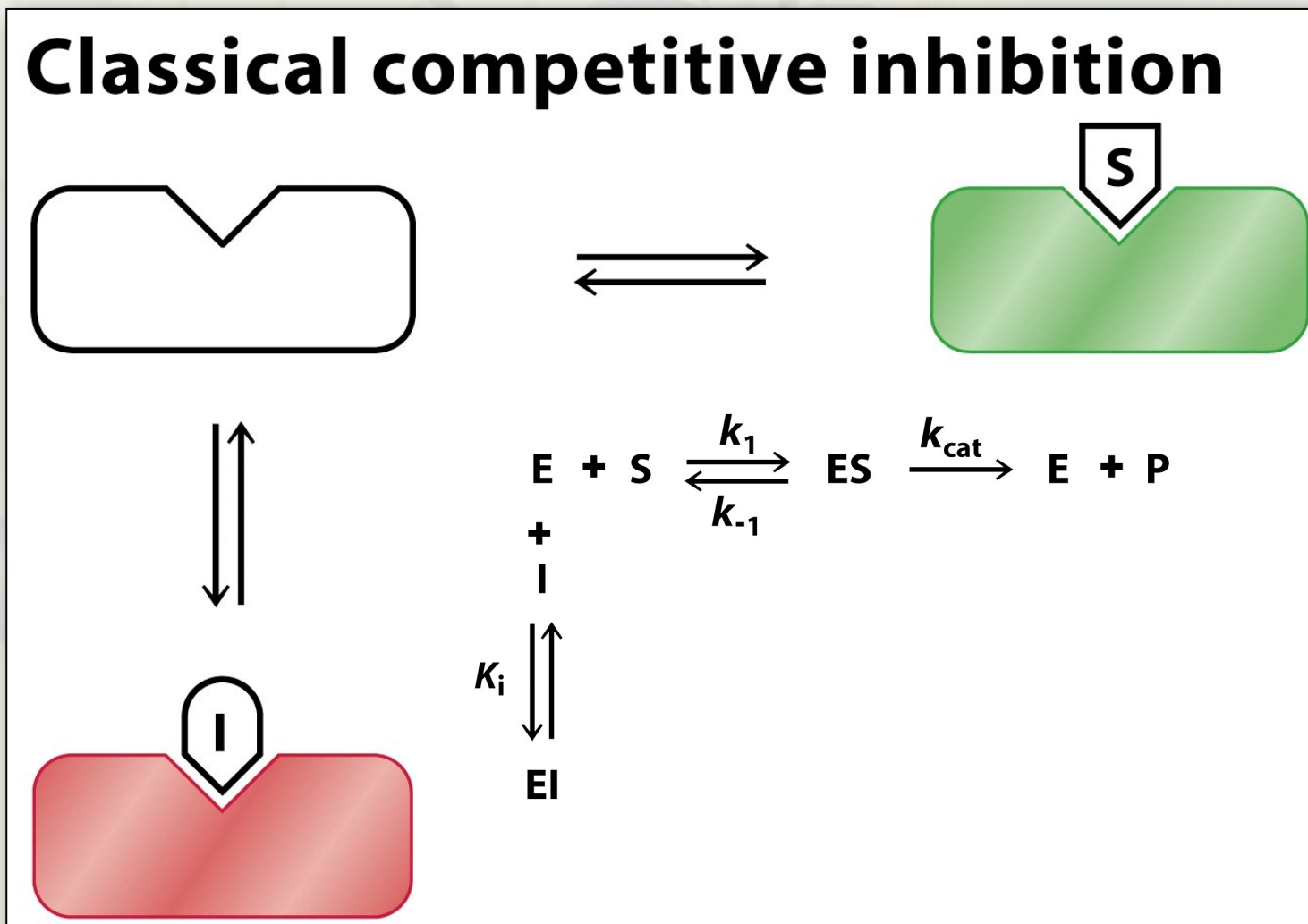
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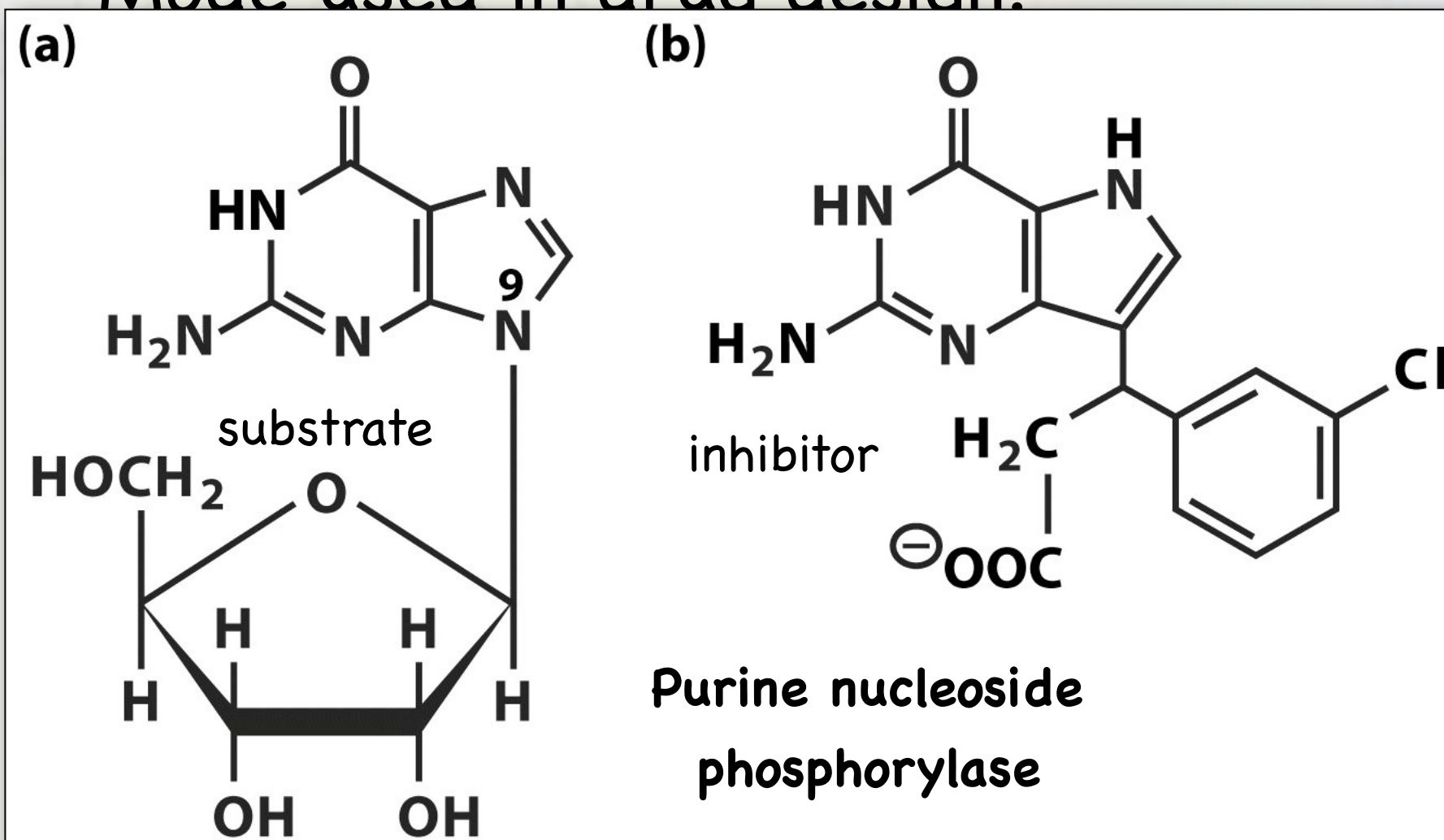
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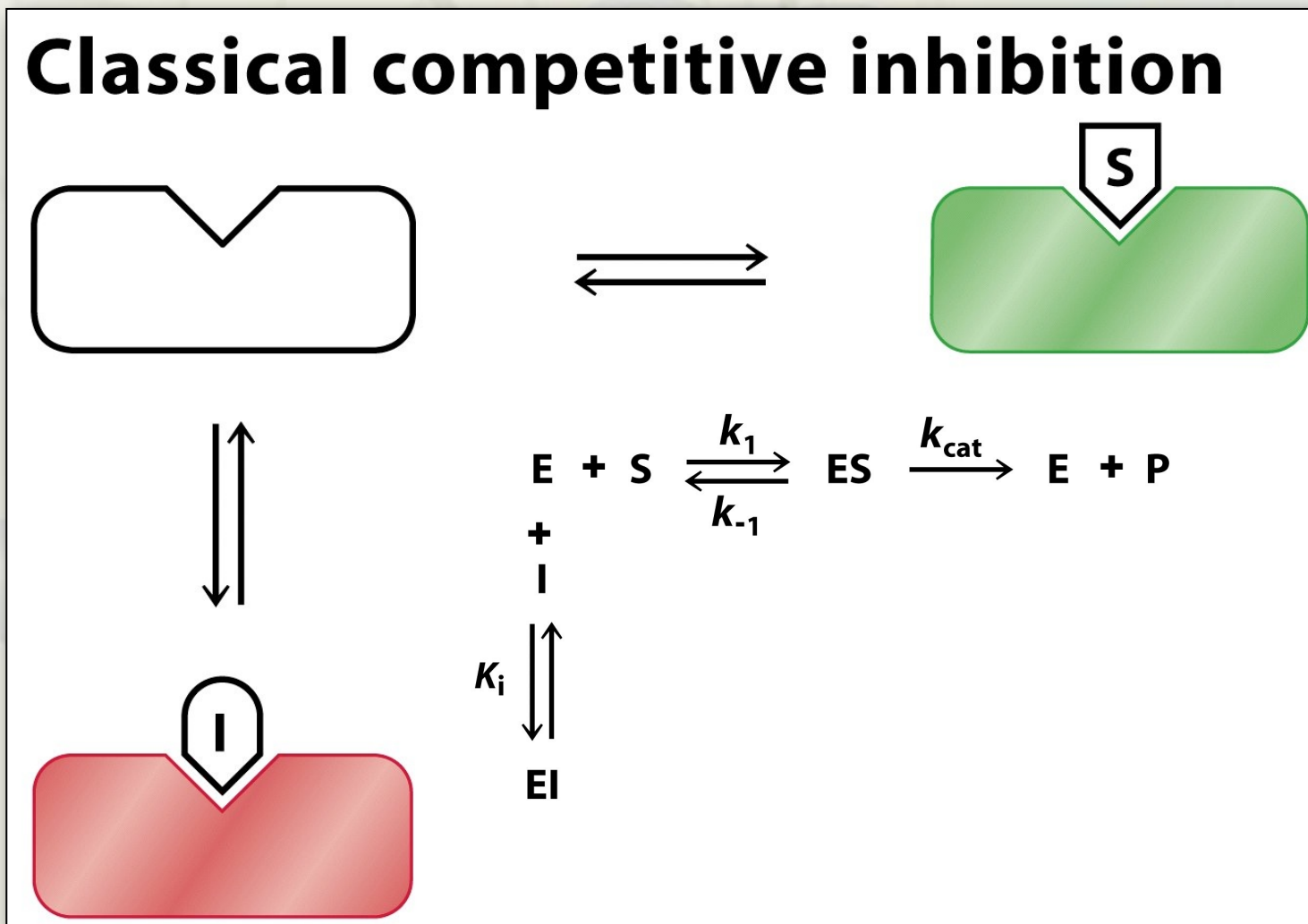


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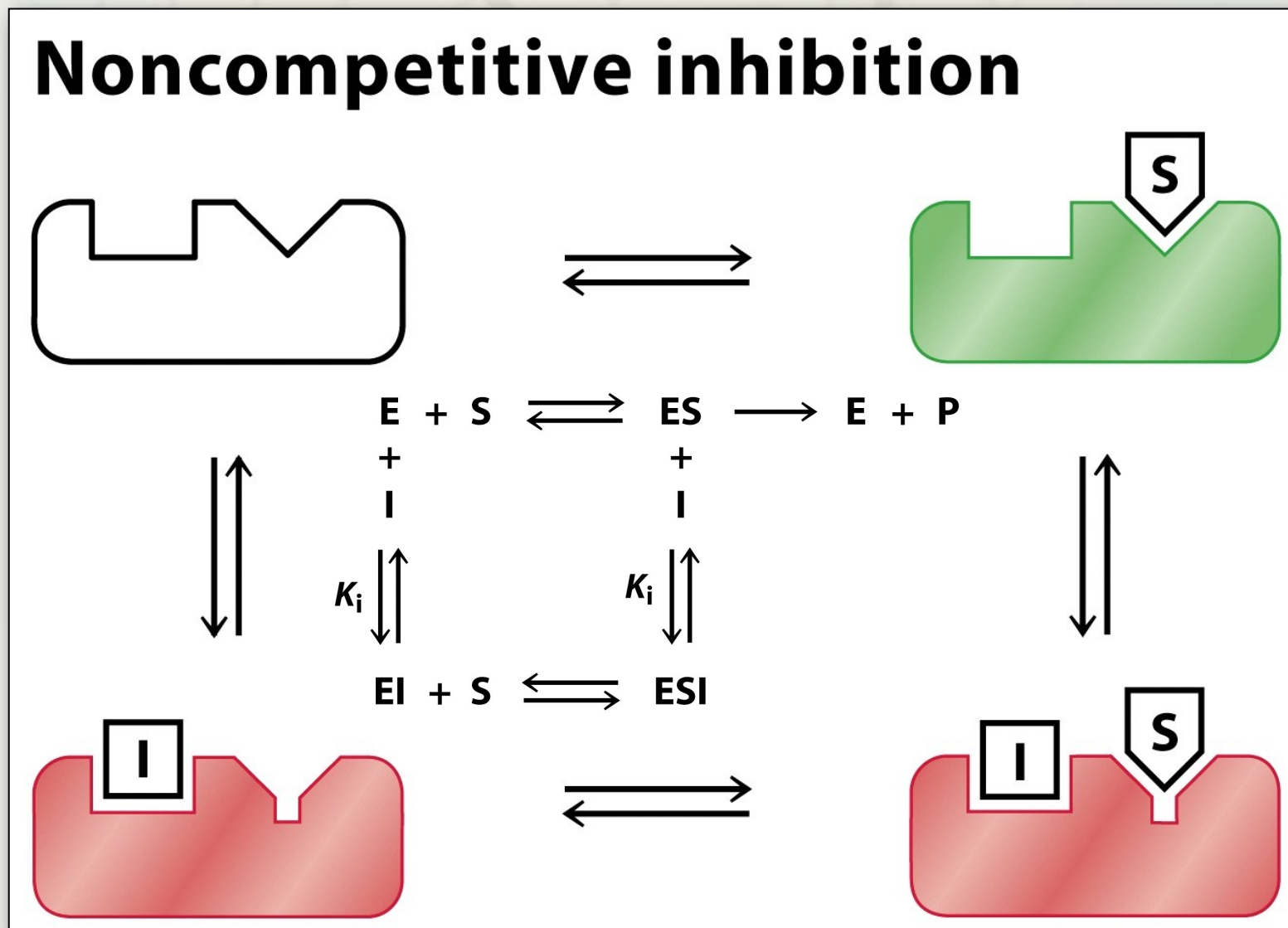


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# Enzyme Kinetics

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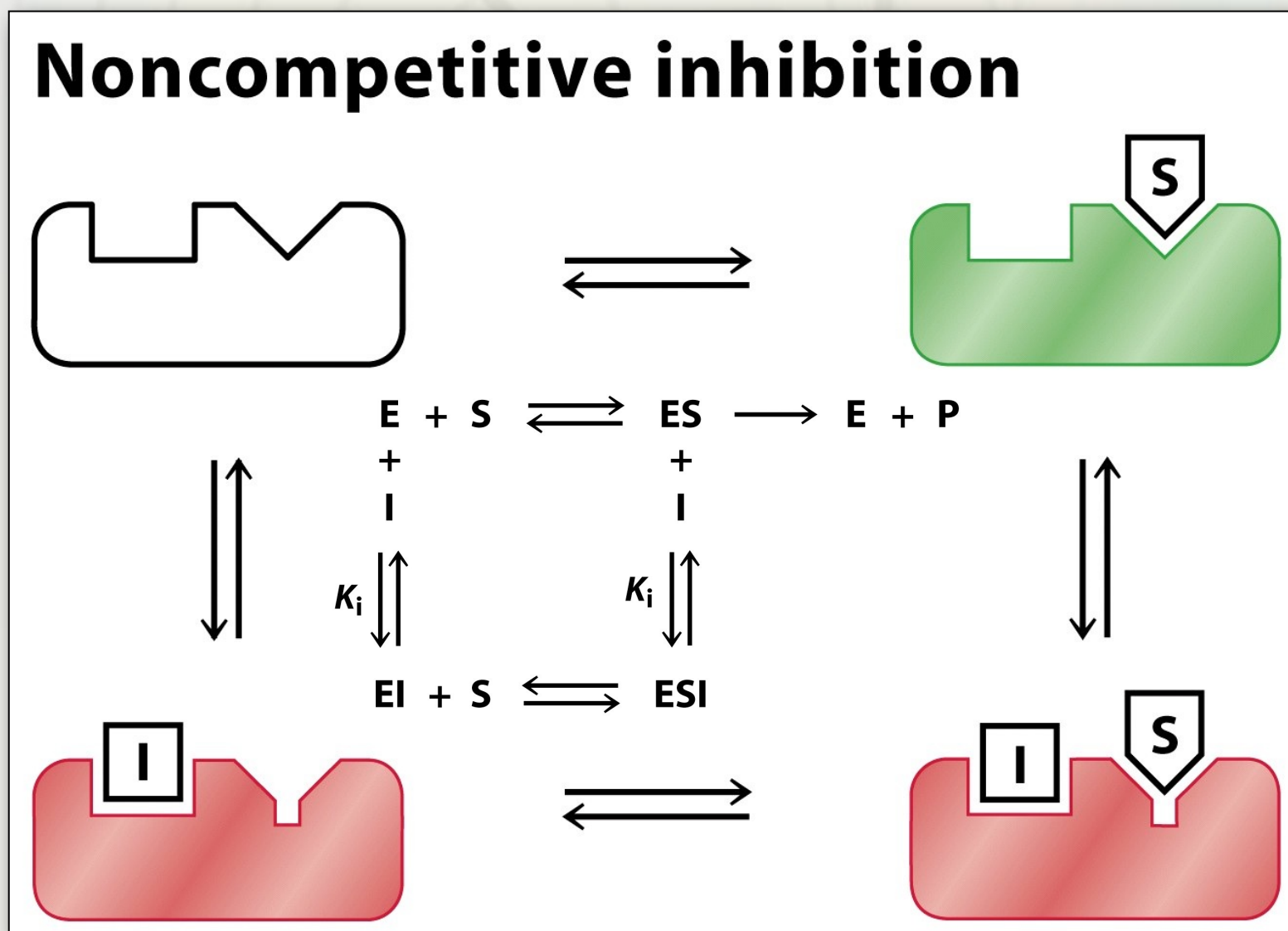
- ✦ Noncompetitive inhibition
  - Mode used in allosteric inhibition



# Enzyme Kinetics

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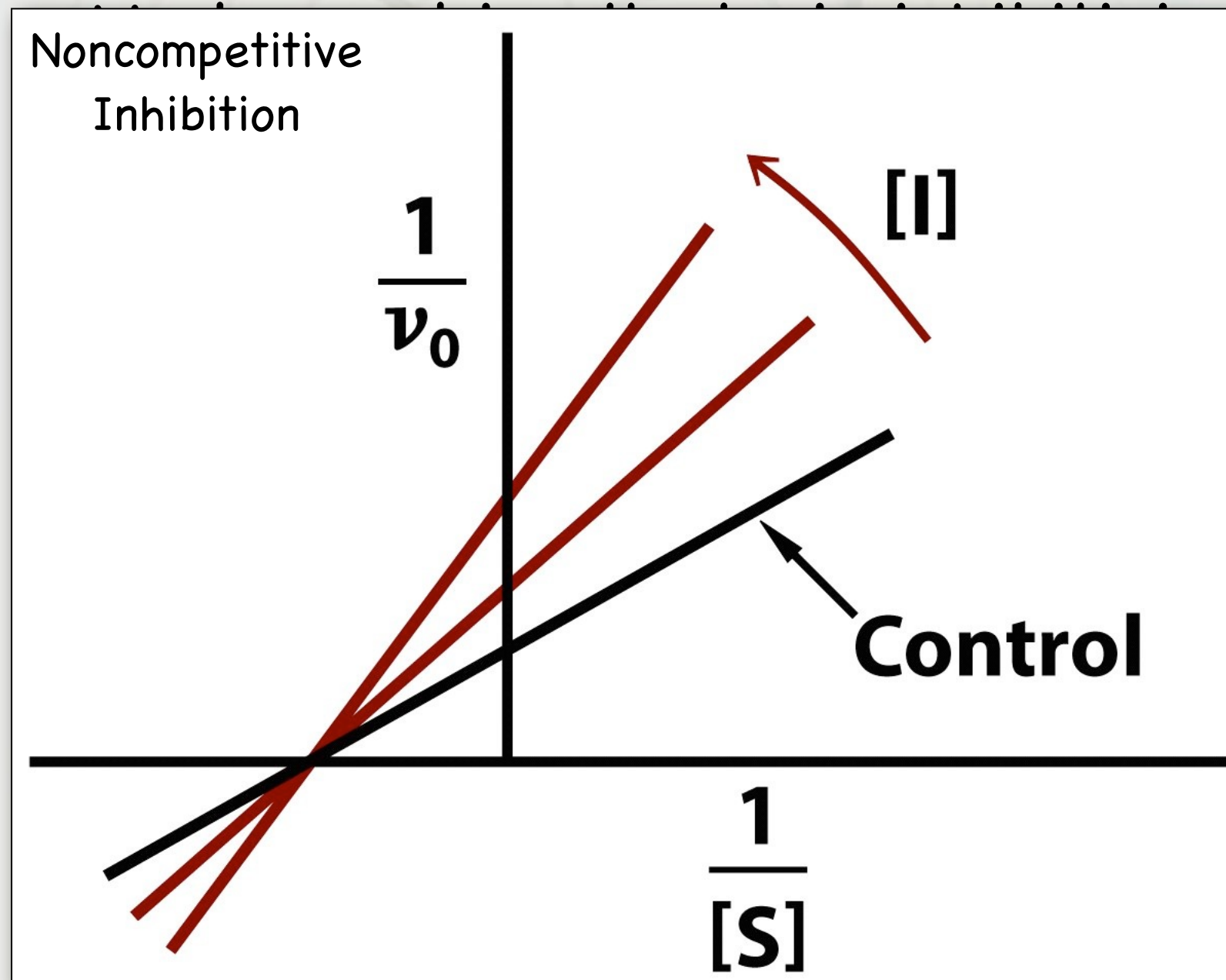


Inhibitor binds independently of the substrate



# Enzyme Kinetics

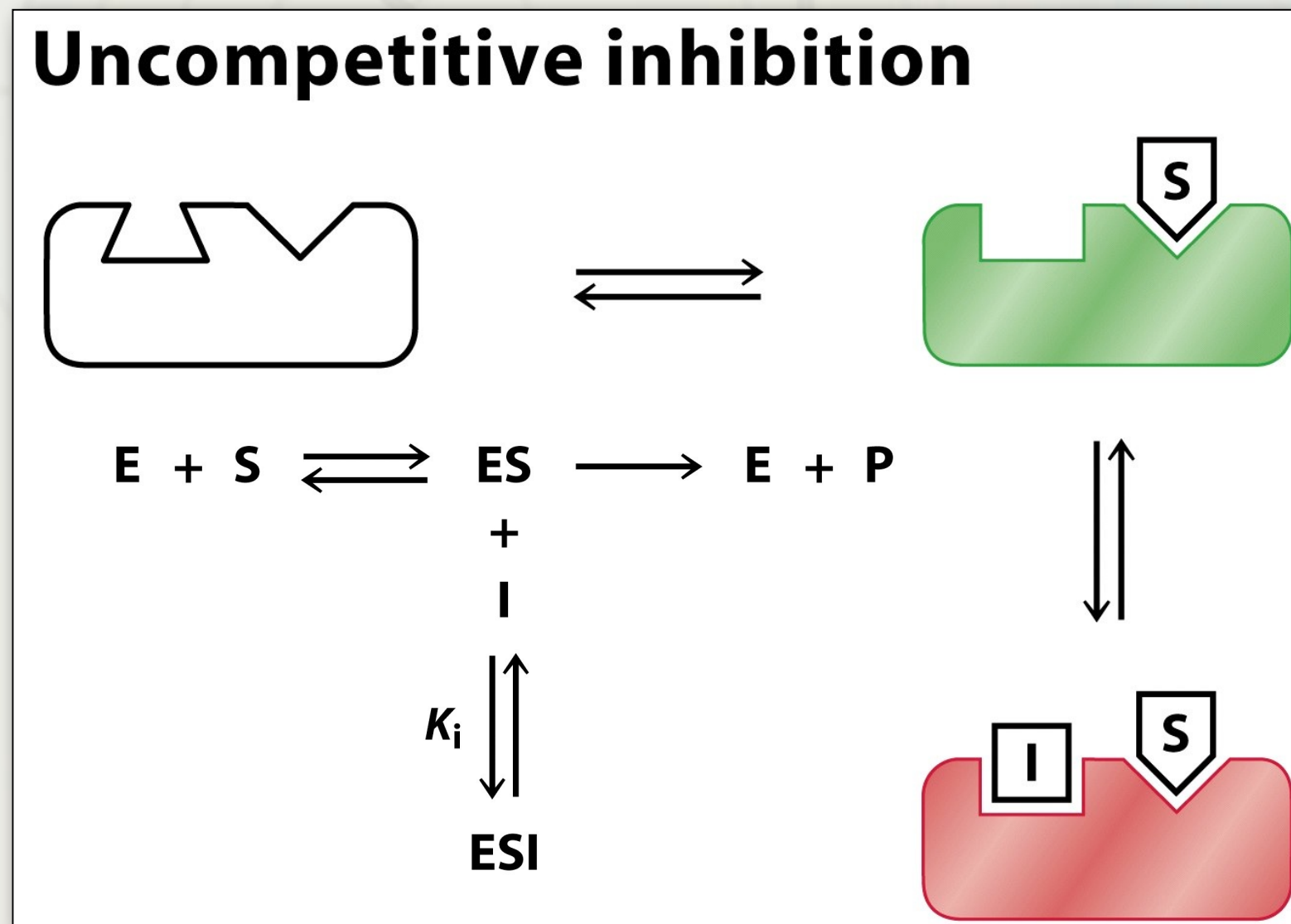
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# Enzyme Kinetics

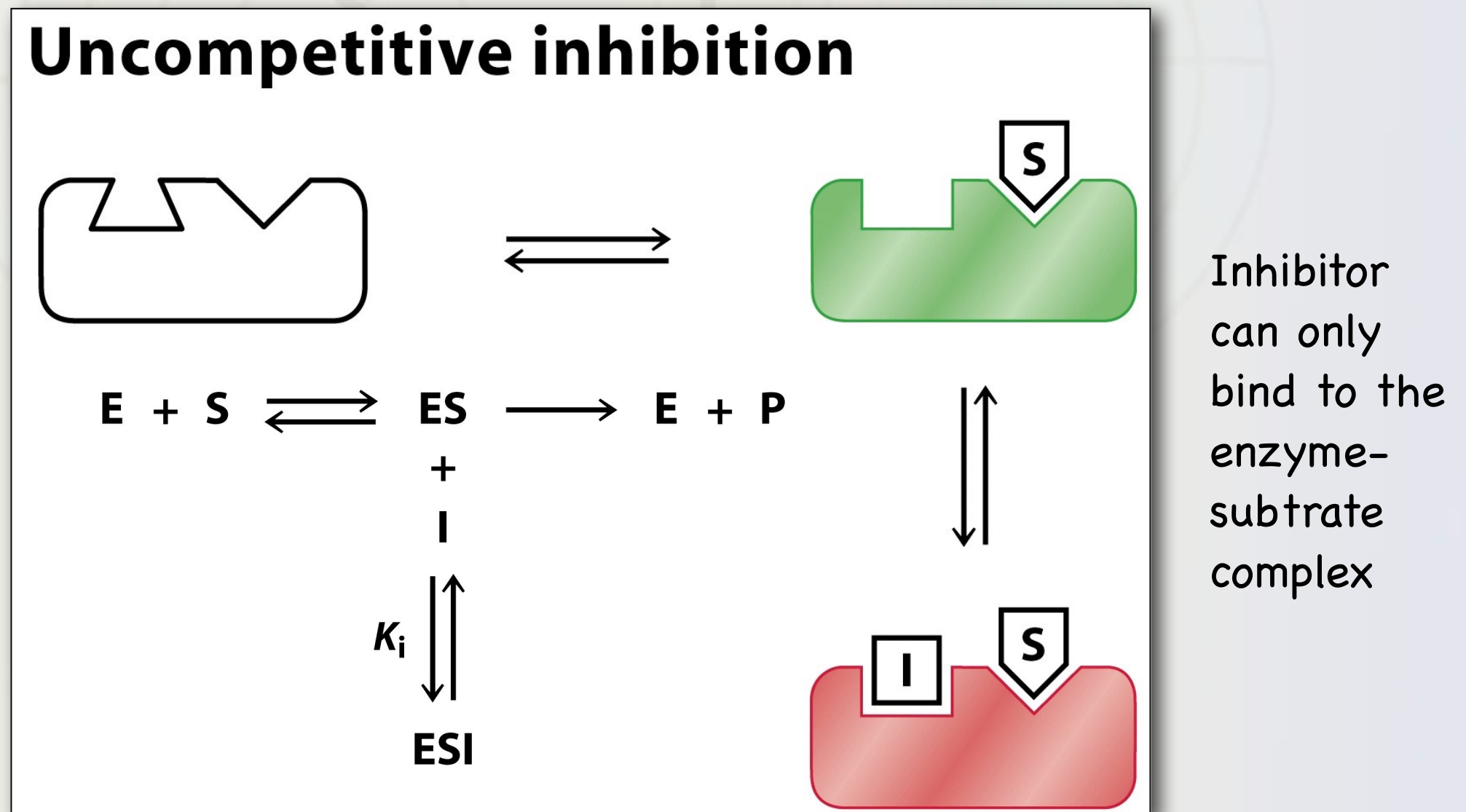
- Reversible Enzyme Inhibition
  - ✦ Uncompetitive inhibition



# Enzyme Kinetics

## • Reversible Enzyme Inhibition

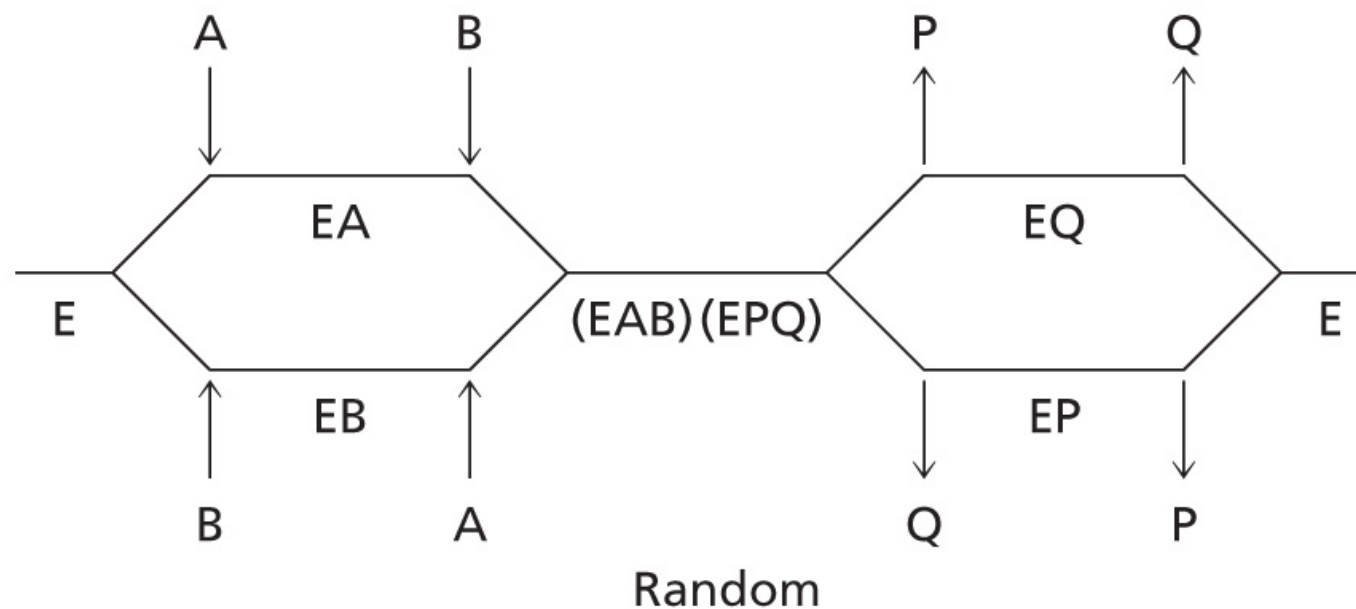
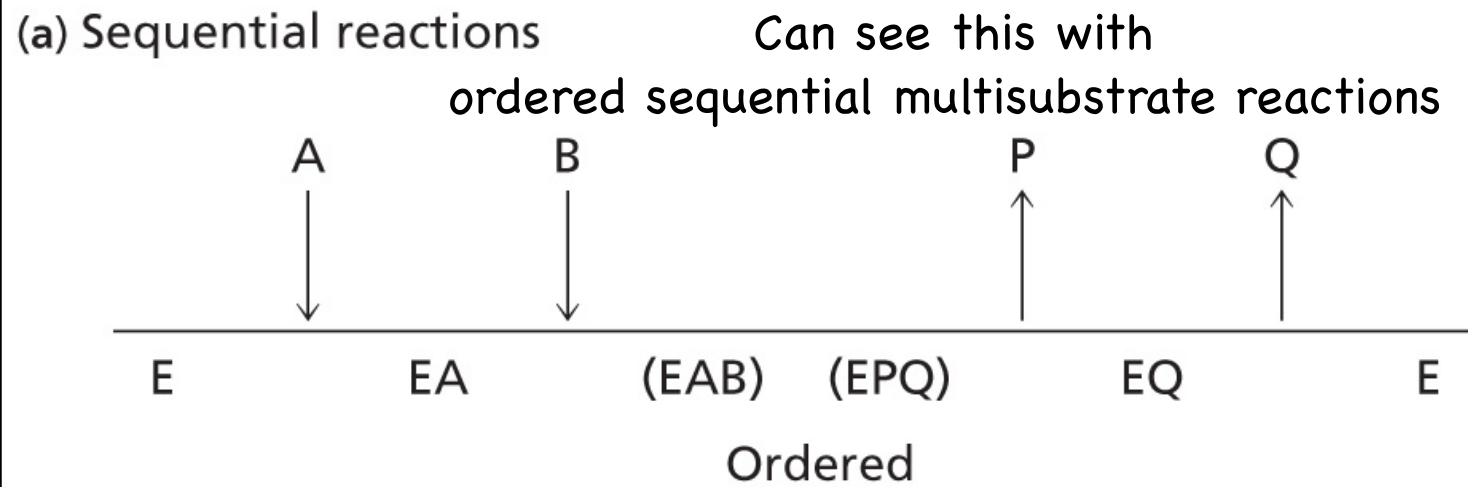
### ✦ Uncompetitive inhibition



# Enzyme Kinetics

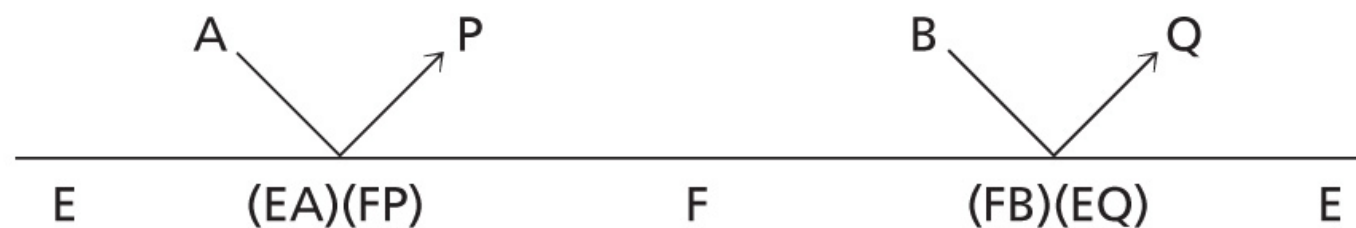
• Review

♦ Un



Inhibitor  
can only  
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enzyme-  
substrate  
complex

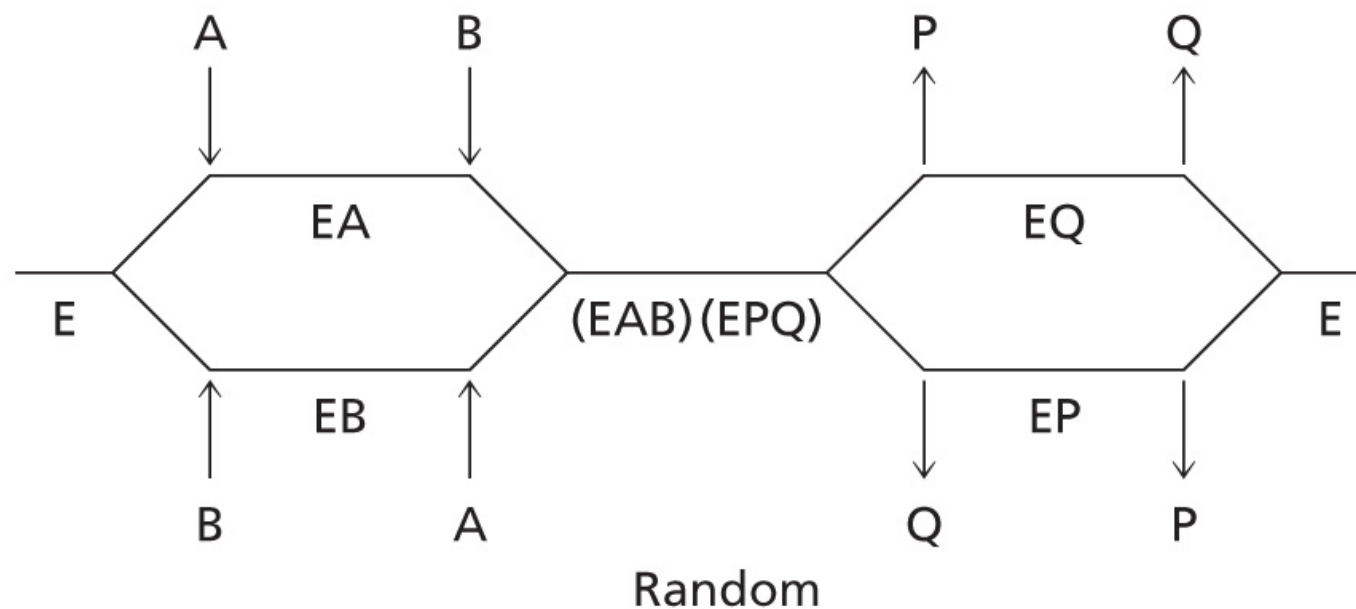
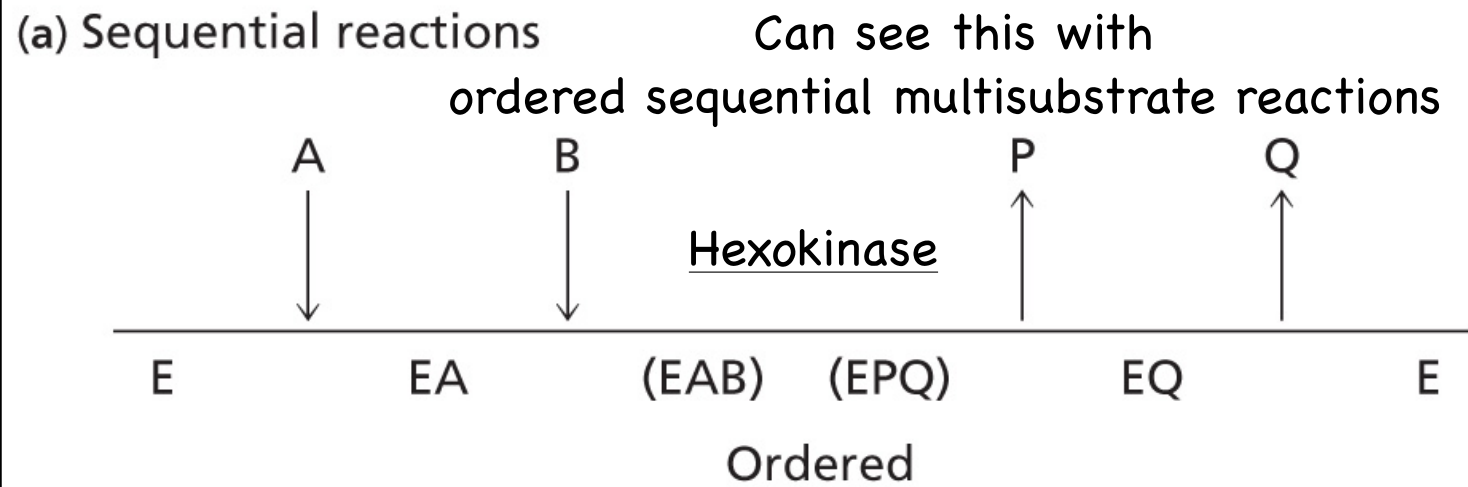
(b) Ping-pong reaction



# Enzyme Kinetics

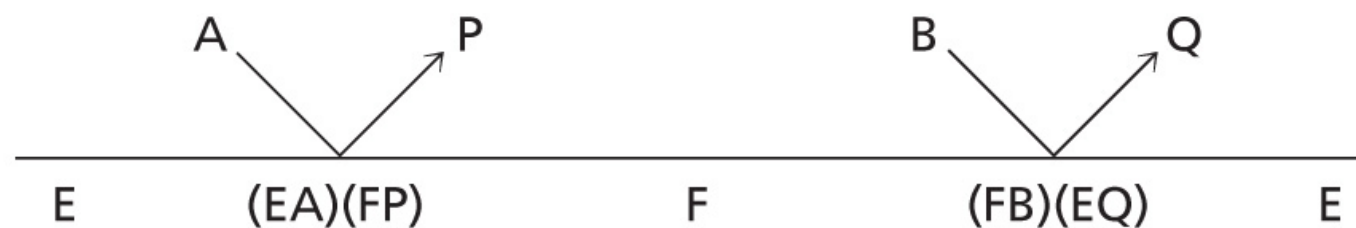
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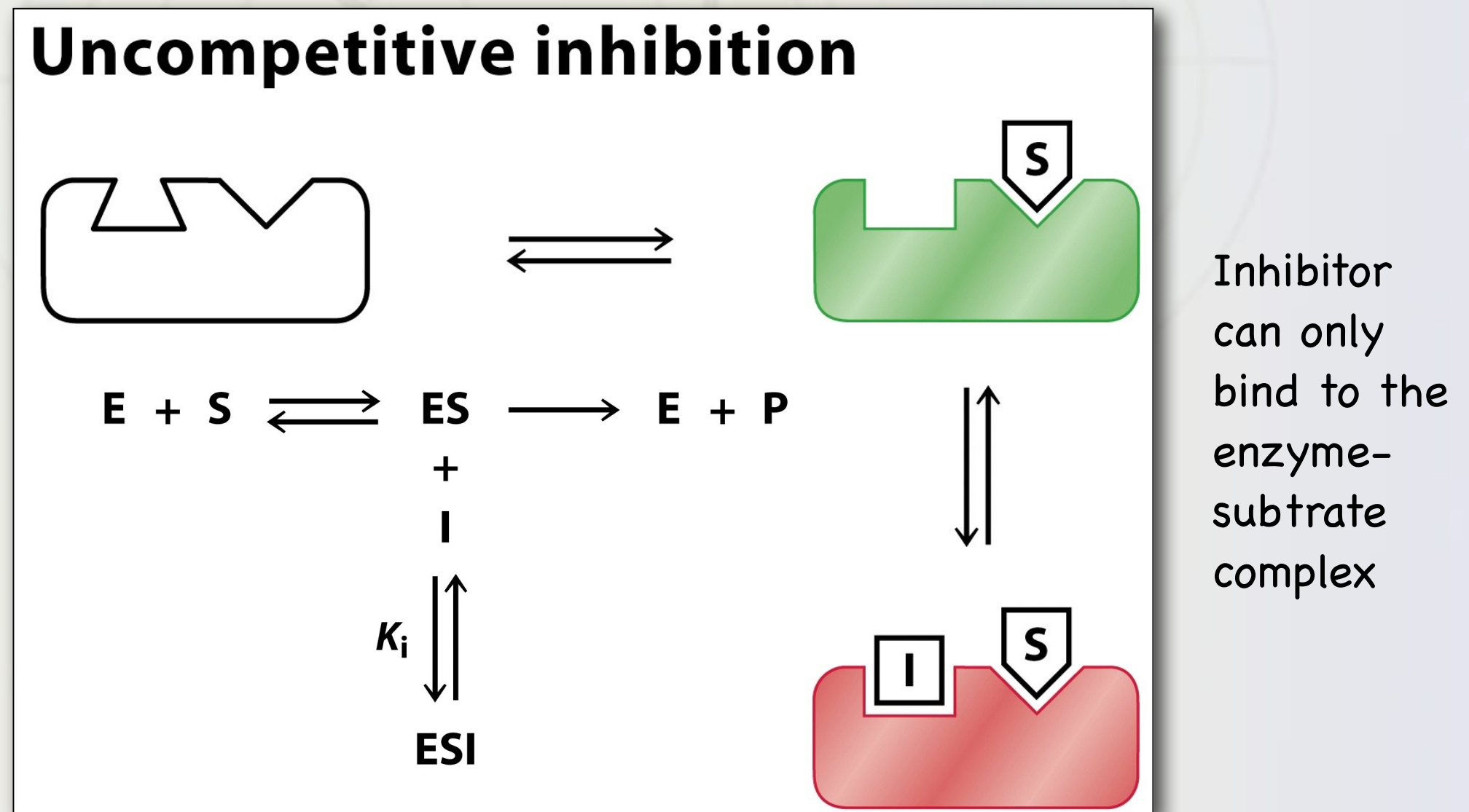




# Enzyme Kinetics

## •Reversible Enzyme Inhibition

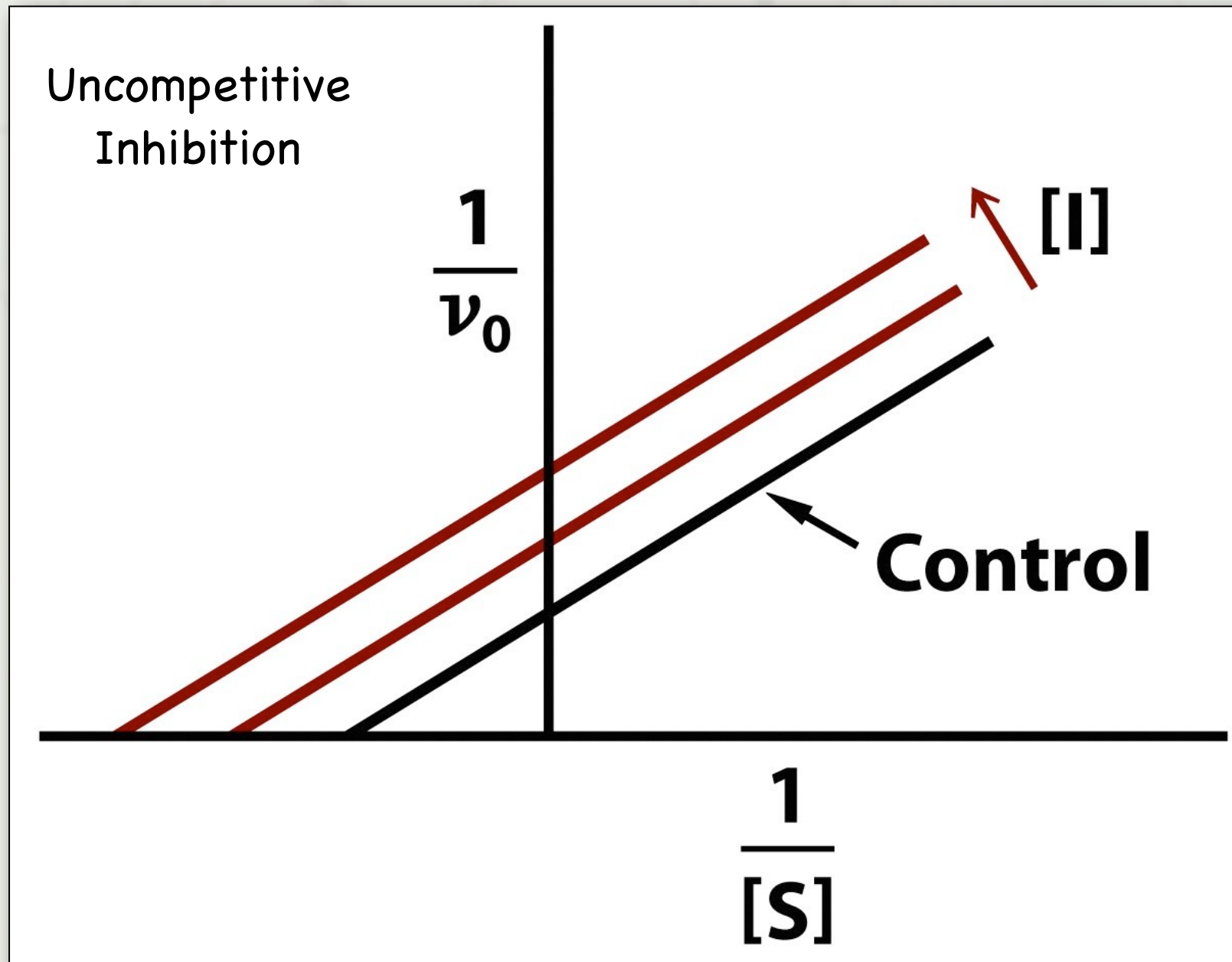
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# Enzyme Kinetics

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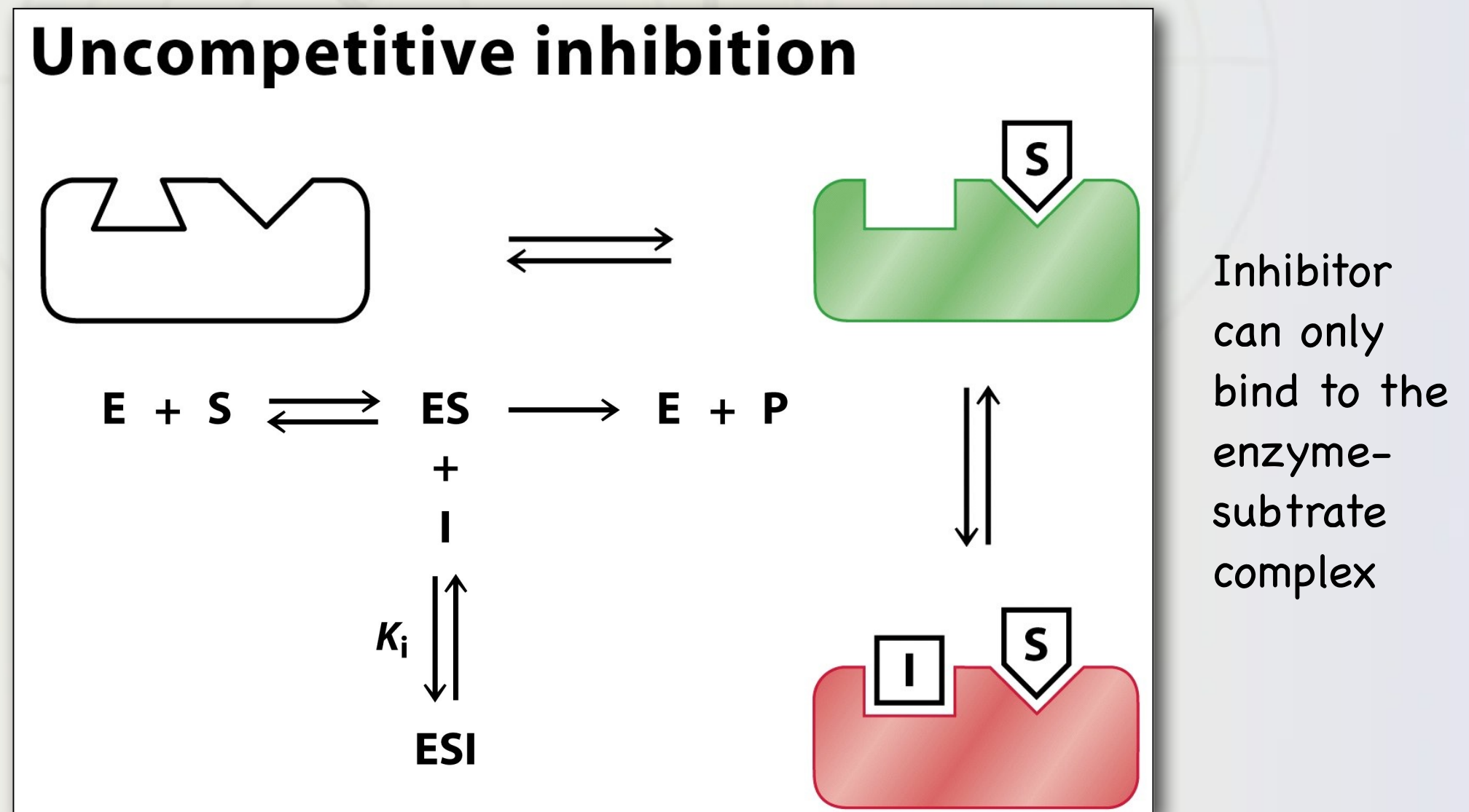


Inhibitor can only bind to the enzyme-substrate complex

# Enzyme Kinetics

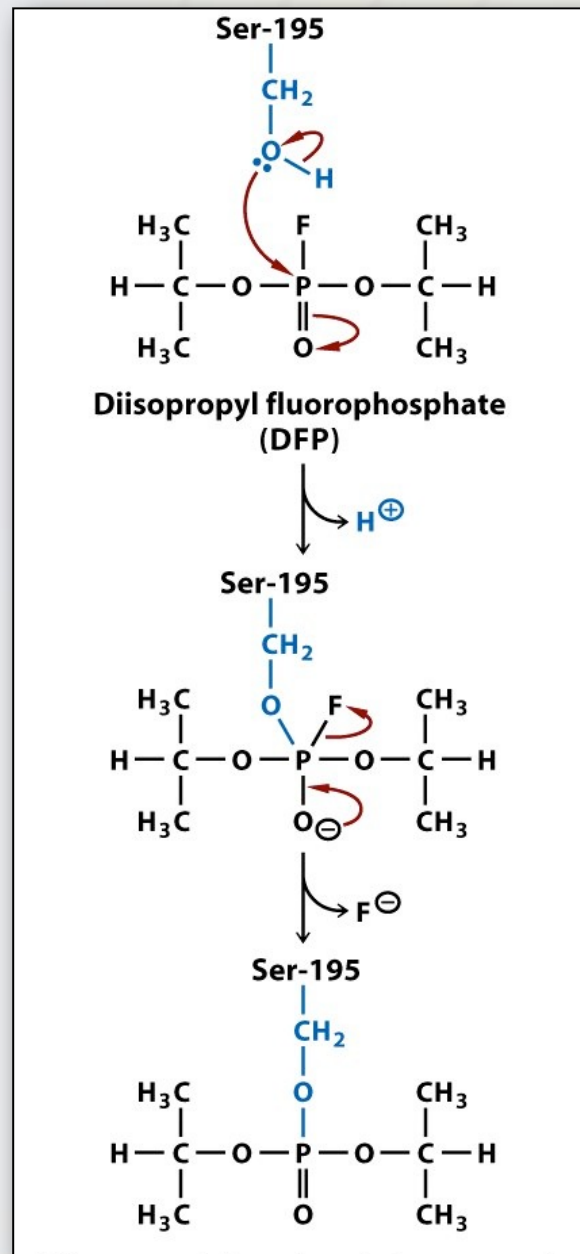
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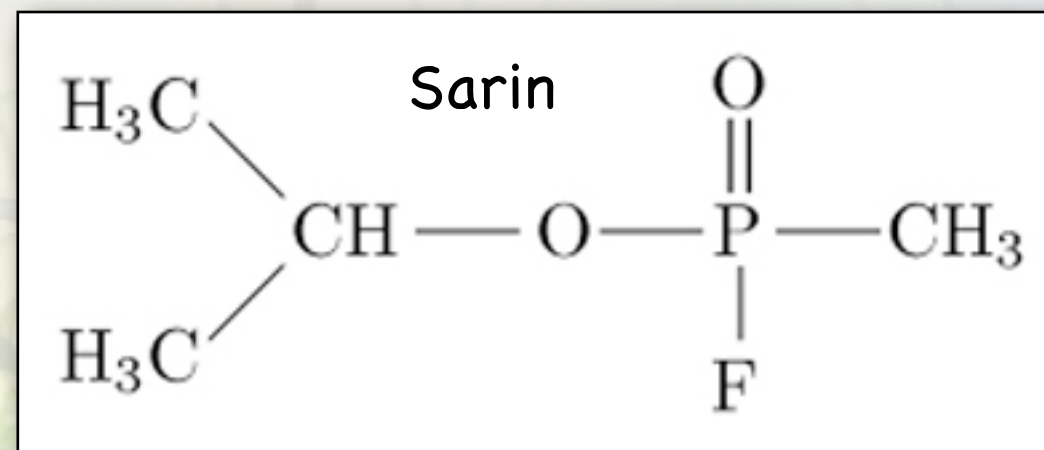
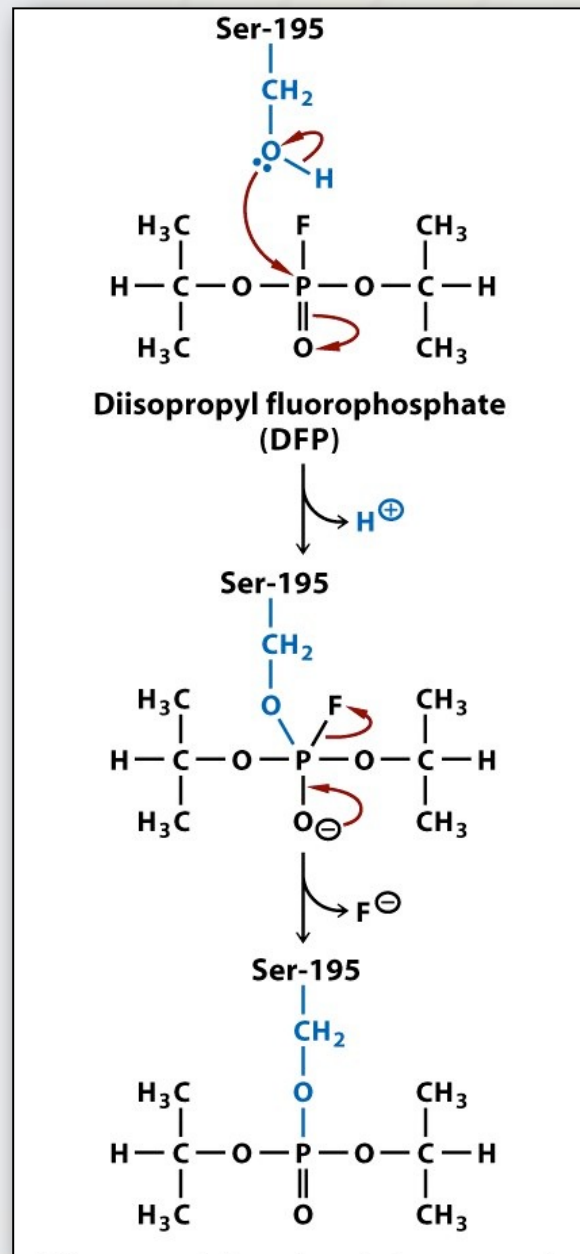
- Irreversible Enzyme Inhibition through covalent modification.



Inhibits serine proteases

# Enzyme Kinetics

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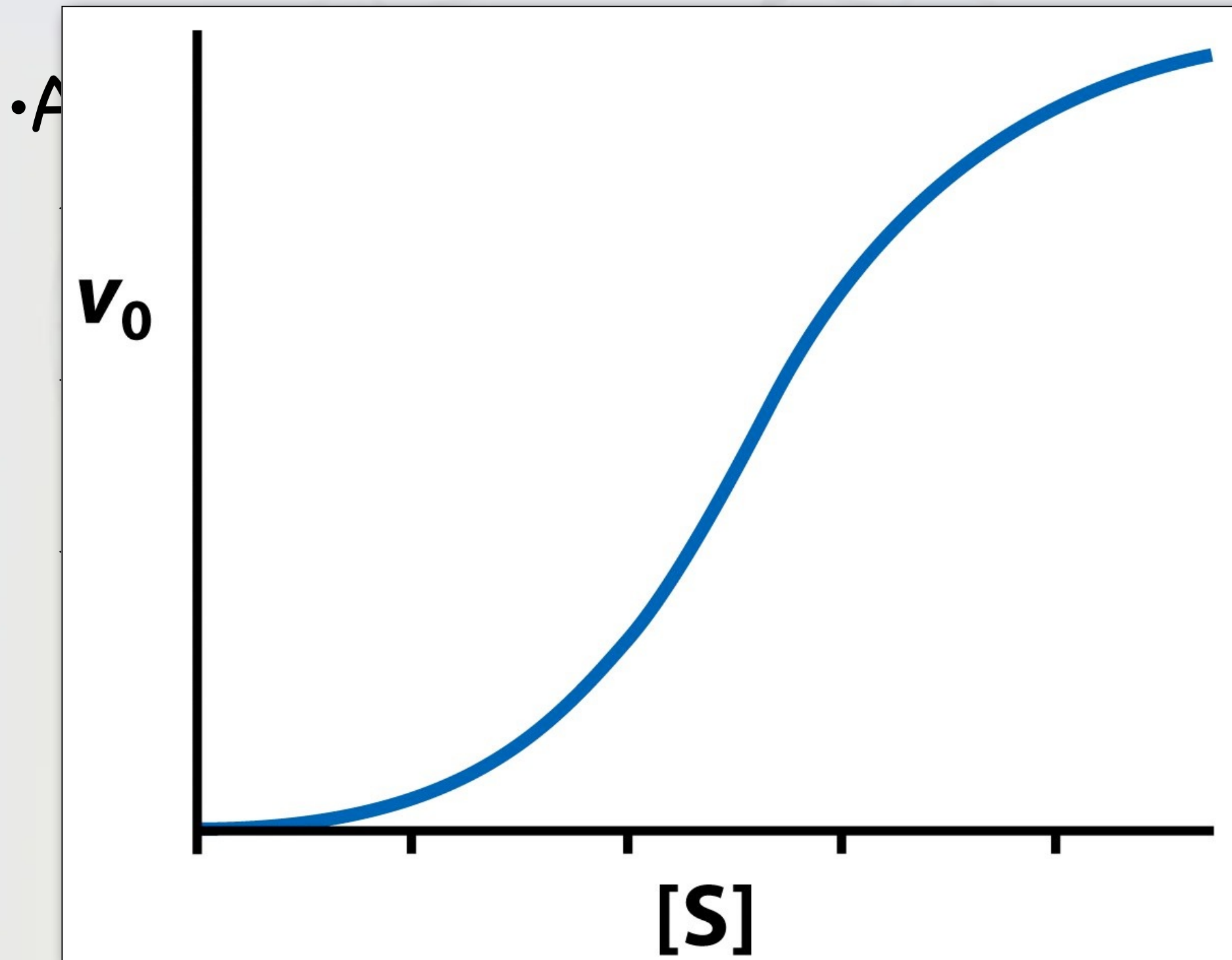


# Enzyme Kinetics

## •Allosteric Regulation

- ✦ Usually catalyze key control points in a metabolic pathway.
- ✦ Allosteric enzymes usually display cooperative substrate binding.
- ✦ Allosteric enzyme have a second regulatory binding site for inhibitors and activators
  - Noncompeptive binding
  - Phosphofructokinase provides a good example

# Enzyme Kinetics

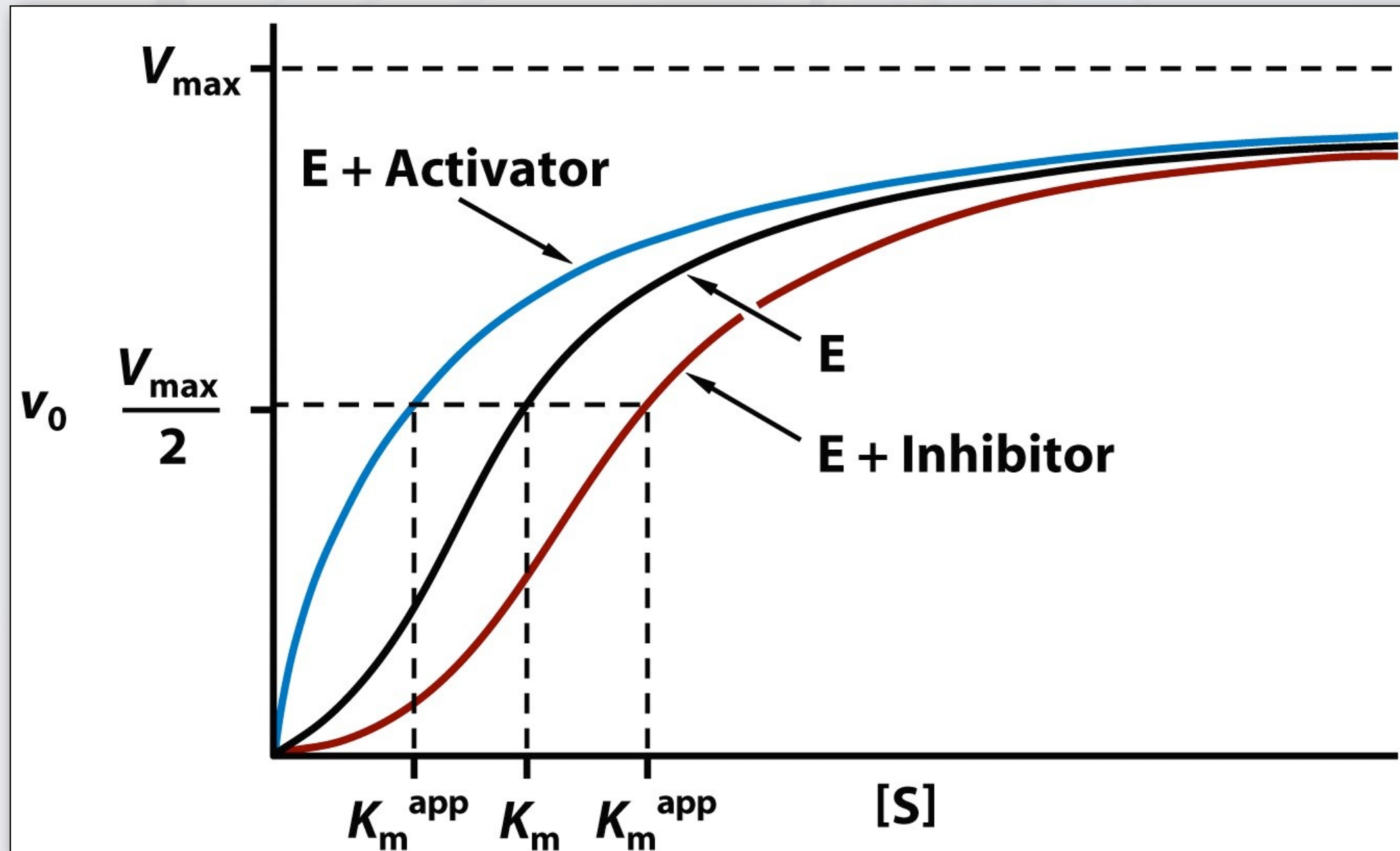


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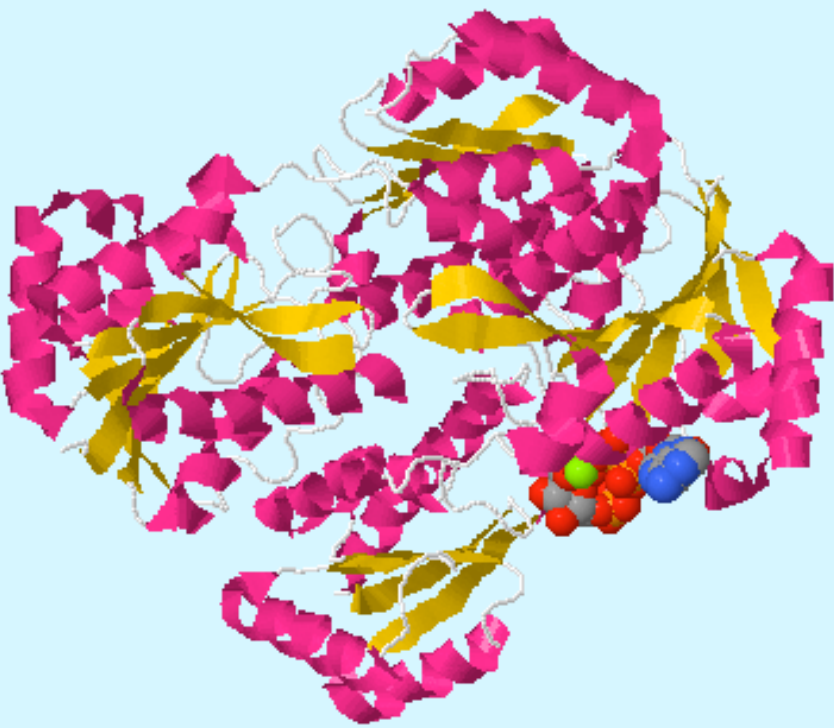
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# Enzyme Kinetics

Protein Structure - Phosphofructokinase (1PFK)



Jmol

**Tertiary Structure**

- The 3-dimensional fold
- [Show tertiary Structure](#)

---

**Primary Structure**

- Sequence of 320 amino acid residues
- [Show sequence](#)
- [Trace Primary Sequence](#)

---

**Secondary Structure**

- Periodic structures involving the backbone
- [Show secondary structure](#)
- ☒ show all
- ☐  $\alpha$ -helix
- ☐  $\beta$ -sheet

---

**Quaternary Structure**

- Association of multiple polypeptides
- [Highlight Subunit A](#)
- [Highlight Subunit B](#)

---

[Restrict to Subunit A](#)

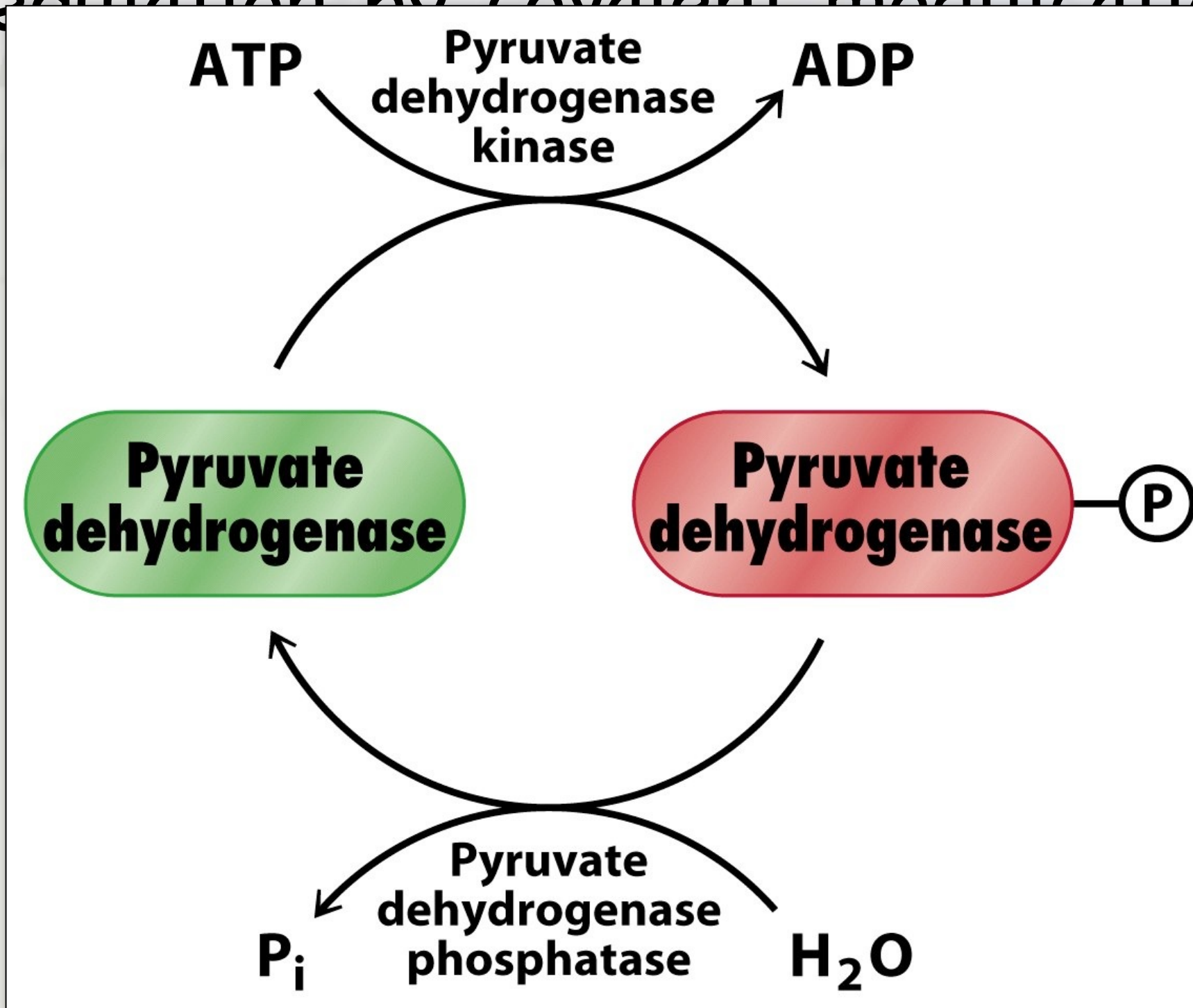
- ☒ Product: Fructose-1,6-bisphosphate
- ☒ Product: ADP
- ☐ Allosteric activator: ADP

# Enzyme Kinetics

- Regulation by covalent modification
  - ✦ Provides a longer term level of regulation than allosteric regulation.
  - ✦ Is reversible
  - ✦ Is often linked to hormonal control of metabolism

# Enzyme Kinetics

- Regulation by covalent modification



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  - ✦ Is reversible
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## Problem:

The cytochrome  $P_{450}$  family of monooxygenases enzymes are involved in the clearance of foreign compounds (including drugs) from our body. A member of this family,  $P_{450}$ -3A4, is known to metabolize midazolam, a sedative, to a hydroxylated product. The kinetic data give below are for this reaction.

[Midazolam] { $\mu\text{M}$ }	$v_o$ { $\text{pmol L}^{-1} \text{ min}^{-1}$ }	$v_o$ with 0.1 $\mu\text{M}$ ketoconazole { $\text{pmol L}^{-1} \text{ min}^{-1}$ }
1	100	11
2	156	18
3	222	27
4	323	33

- Determine the  $K_M$  and  $V_{\max}$  for the uninhibited enzyme using a Lineweaver-Burk plot.
- Ketoconazole, an antifungal, is known to cause adverse drug-drug interactions when administered with midazolam. Using the data in the table, determine the type of inhibition that ketoconazole exerts on the  $P_{450}$ -catalyzed hydroxylation of midazolam



# Next Up

- Lecture 4, Part II
  - Reaction Mechanisms for enzyme catalyzed reactions (Chapter 6)