HW \& LEARNING GOALS \#2: Disequilibrium, kinetics, and the Chapman Cycle (part 1)

1. "Disequilibrium" in the stratosphere: Consider the reaction $\mathbf{3 O}_{2} \rightarrow \mathbf{2} \mathbf{O}_{3}$
i) $\Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}$ for $\mathrm{O}_{3}$ is $163.4 \mathrm{~kJ} / \mathrm{mol}$, use this to calculate $\Delta \mathrm{G}_{\mathrm{RXN}}$ for the reaction above.
ii) Use the result from "i" to Calculate Kp from $\Delta \mathrm{G}$ (assume 225 K - T at 25 km ).
iii) Estimate the pressure at 25 km in altitude (from the graph handed out in class), and realizing that $\mathrm{X}_{\mathrm{O} 2}=.21$, calculate the partial pressure of $\mathrm{O}_{2}$, and in turn (using Kp from ii) the partial pressure of $\mathrm{O}_{3}$ (as predicted by EQ chemistry).
iv) Now, let's calculate mixing ratios (observed and predicted) and compare. a) To calculate "predicted" $\mathrm{X}_{\mathrm{O} 3}$ use the partial pressure from "iii" and the total pressure. b) To calculate "observed" use $\left[\mathrm{O}_{3}\right]$ from the overhead in class $\left(\left[\mathrm{O}_{3}\right]\right.$ or $\mathrm{C}_{03}=5 \times 10^{12} \mathrm{~mole} / \mathrm{cm}^{3}$, and total number density $[\mathrm{M}]$ or $\left.\mathrm{C}_{\mathrm{M}}=8.3 \times 10^{17} \mathrm{molec} / \mathrm{cm}^{3}\right)$. c) Do they compare well? Are you surprised? What is going on in the stratosphere that would drive the atm out of equilibrium?
2. General questions about reaction rates (some of this is 104 review - some is new...):
a) State the factors that affect the rate of a chemical reaction (that is non-photochemical), and which are included in the rate constant (k).
b) What factors affect the rate of a photochemical reaction, and which of these are included in a photochemical rate constant (J)? (I will explain this a bit further in the key ...)
c) Why does a combination reaction (e.g. $A+B->C$ ) require an additional molecule ("M") to collide with the 2 reacting molecules for the reaction to occur?
d) For the reactions below: i) write the general expressions for the rate laws, ii) identify the individual reaction orders (i.e. "__ order in "A"), iii) state the overall reaction orders (i.e. " order overall), and iv) specify the proper units for the rate constants when concentrations are expressed in molculec/ $\mathrm{cm}^{3}$ (a.k.a. "number density").
i) $\mathrm{A}+\mathrm{hv} \rightarrow 2 \mathrm{~B}$
ii) $\mathrm{A}+\mathrm{B} \rightarrow \mathrm{C}+\mathrm{D}$
iii) $\mathrm{A}+\mathrm{B}+\mathrm{M} \rightarrow \mathrm{C}+\mathrm{M}^{*}$
(Note that, in general, you cannot equate reaction orders with stoichiometric reaction coefficients. However, we can do this for atmospheric reactions since they are almost always gas-phase, "elementary" (single-step) reactions).
3. The Chapman Cycle - kinetic considerations:
a) List the reactions that comprise the Chapman cycle, and write expressions for their rate laws, and label them with the net loss or gain of "odd oxygen" (i.e. in units of "Ox").
b) Add the reactions together (double \#2) to show that collectively, the reactions of the Chapman cycle cause no "net" chemistry, merely a sort of "cyclical engine" that converts light to heat.
c) Calculate the rates of each reaction, using the following data:
$\mathrm{J}_{1}=3.7 \times 10^{-27} \mathrm{sec}^{-1}$
$\mathrm{k}_{2}=3.0 \times 10^{-34} \mathrm{~cm}^{6} / \mathrm{molec}^{2} \mathrm{sec}$
$\mathrm{J}_{3}=5.4 \times 10^{-4} \mathrm{sec}^{-1}$
$\mathrm{k}_{4}=8.4 \times 10^{-16} \mathrm{~cm}^{3} / \mathrm{molec} \mathrm{sec}$

$$
\begin{aligned}
& {\left[\mathrm{O}_{3}\right]=5 \times 10^{12} \mathrm{molec} / \mathrm{cm} 3} \\
& {[\mathrm{M}]=8.3 \times 10^{17} \mathrm{molec} / \mathrm{cm} 3} \\
& \mathrm{X}_{\mathrm{O}}=1.0 \times 10^{-11} \\
& \mathrm{X}_{\mathrm{O} 2}=0.21
\end{aligned}
$$

d) Examine the values of the reaction rates above, what about these data justifies the notion of an "Ox" family?
e) An altitude-specific estimate of the rate constant $\left(\mathrm{J}_{1}\right)$ for step \#1 in the cycle $\left(\mathrm{O}_{2}\right.$ photolysis in the lingo of the field) is $\sim 10^{-11} \mathrm{sec}$. ${ }^{-1}$ at 30 km . Use this to calculate the lifetime of $\mathrm{O}_{2}\left(\tau_{o_{2}}\right)$. Compare this to the lifetime calculated using reaction \#2 (and data above). Is the rationale in "d" still valid?
4. Tropospheric chemistry preview: The main process by which most compounds are degraded in the lower atmosphere is by reaction with OH , via a "hydrogen abstraction" reaction, e.g.

$$
\mathrm{HX}+\mathrm{OH} \rightarrow \mathrm{H}_{2} \mathrm{O}+\mathrm{X}
$$

The mixing ratio of $\mathrm{OH}\left(\mathrm{X}_{\mathrm{OH}}\right)$ is $6 \times 10^{-14}$ at 0 km (and the total number density $[\mathrm{M}]$ is $2.7 \times 10^{19}$ $\mathrm{molec} / \mathrm{cm}^{3}$ ). Complete each reaction below, and use the rate data below to calculate the lifetimes of each organic (carbon-containing) compound below (methane, propane, and formaldehyde...).

$$
\begin{array}{ll}
\text { a) } \mathrm{CH}_{4}+\mathrm{OH} \rightarrow+ & \left(\mathrm{k}=6.6 \times 10^{-15} \mathrm{~cm}^{3} / \mathrm{molecule} \mathrm{sec}\right) \\
\text { b) } \mathrm{C}_{3} \mathrm{H}_{8}+\mathrm{OH} \rightarrow+ & \left(\mathrm{k}=1.1 \times 10^{-12} \mathrm{~cm}^{3} / \mathrm{molecule} \mathrm{sec}\right) \\
\text { c) } \mathrm{H}_{2} \mathrm{CO}+\mathrm{OH} \rightarrow+ & \left(\mathrm{k}=1.0 \times 10^{-11} \mathrm{~cm}^{3} / \mathrm{molecule} \mathrm{sec}\right)^{*}
\end{array}
$$

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[^0]:    * Photochemistry is a significant $\mathrm{H}_{2} \mathrm{CO}$ loss pathway too! Ignore this fact for now...

